

PREUVE *ZERO-KNOWLEDGE* POUR NP  
RELATIVISTES ET RÉALISABLES

Claude Crépeau



McGill

PREUVE *ZERO-KNOWLEDGE* POUR NP  
RELATIVISTES ET RÉALISABLES  
(COHÉRENTE MALGRÉ L'INTRICATION)

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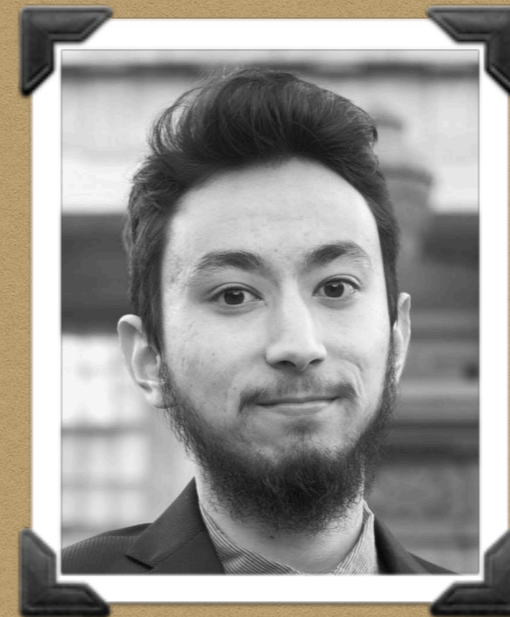
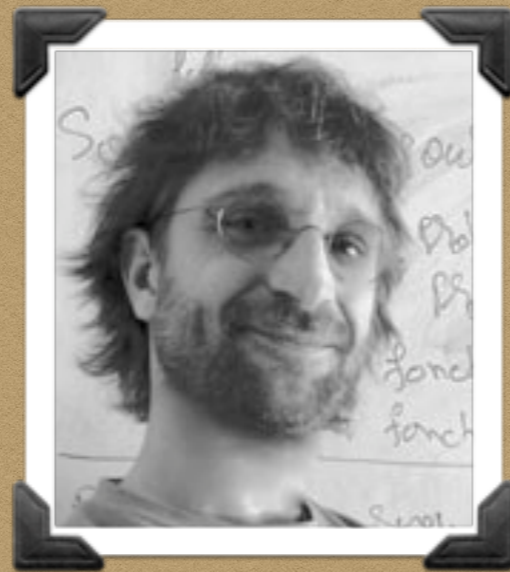
McGill

Arnaud Yoh Massenet-Oshima

Louis Salvail

Lucas Shigeru Stinchcombe

Nan Yang



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# INTRODUCTION

*(P-V-D)*

# PERSONNAGES



# PERSONNAGES



prouveur



# PERSONNAGES



prouveur



vérificateur

# PERSONNAGES



prouveur



vérificateur

# PERSONNAGES



prouveur



vérificateur



distingueur

# INTRODUCTION

*(ZK) IPs*



Goldwasser



Micali



Rackoff

1985





Goldwasser

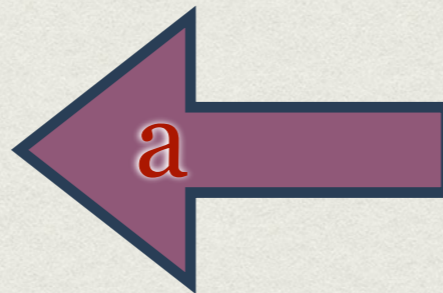


Micali



Rackoff

1985





Goldwasser



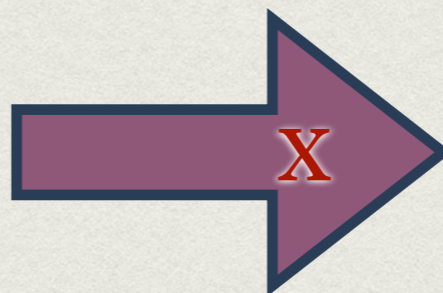
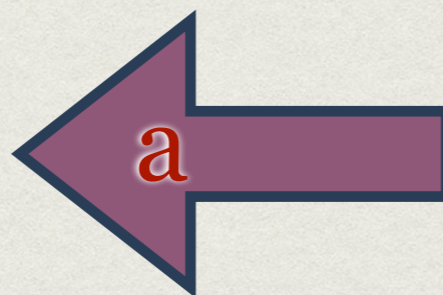
Micali



Rackoff

1985

W





Goldwasser

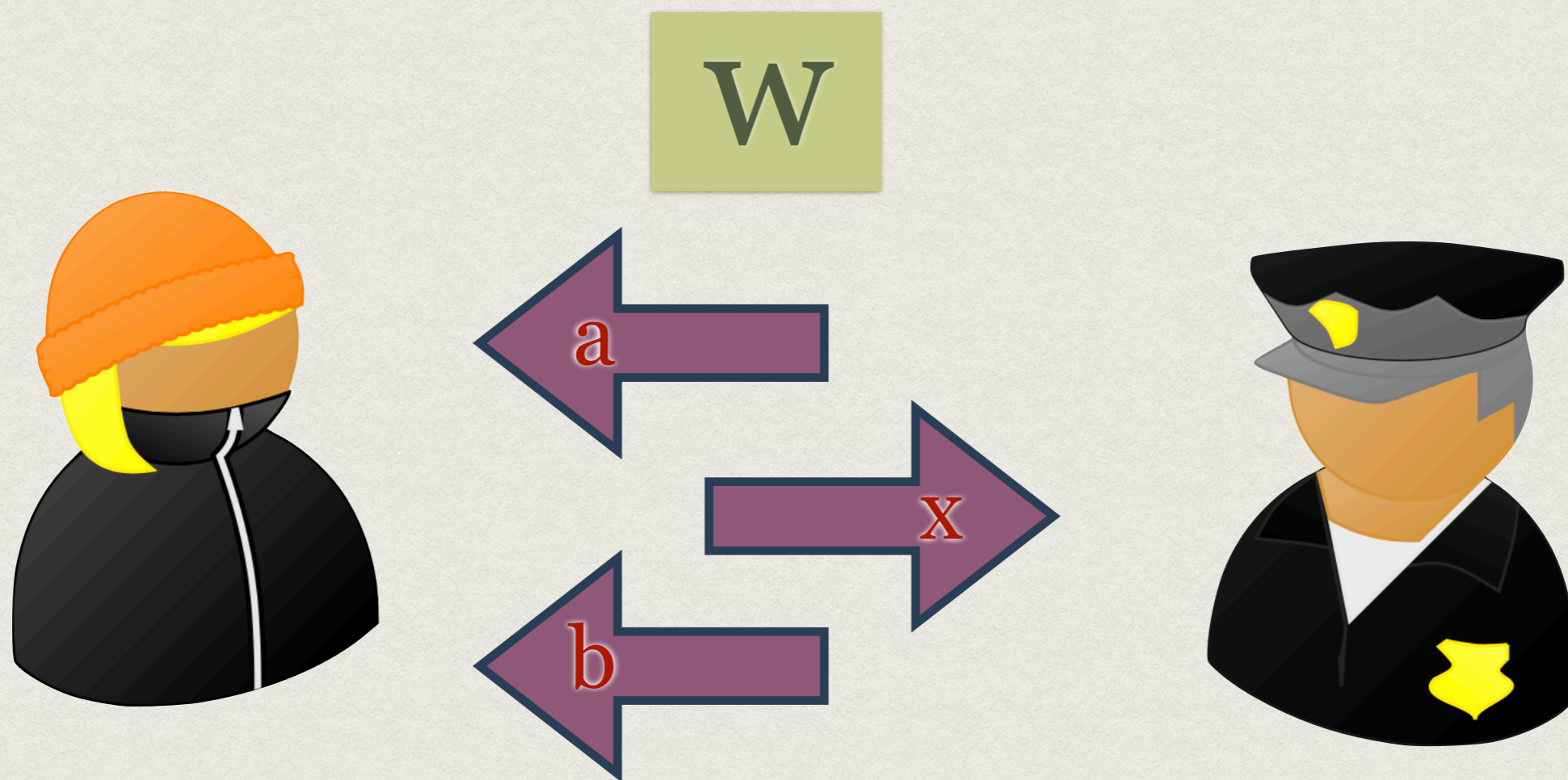


Micali



Rackoff

1985







Goldwasser

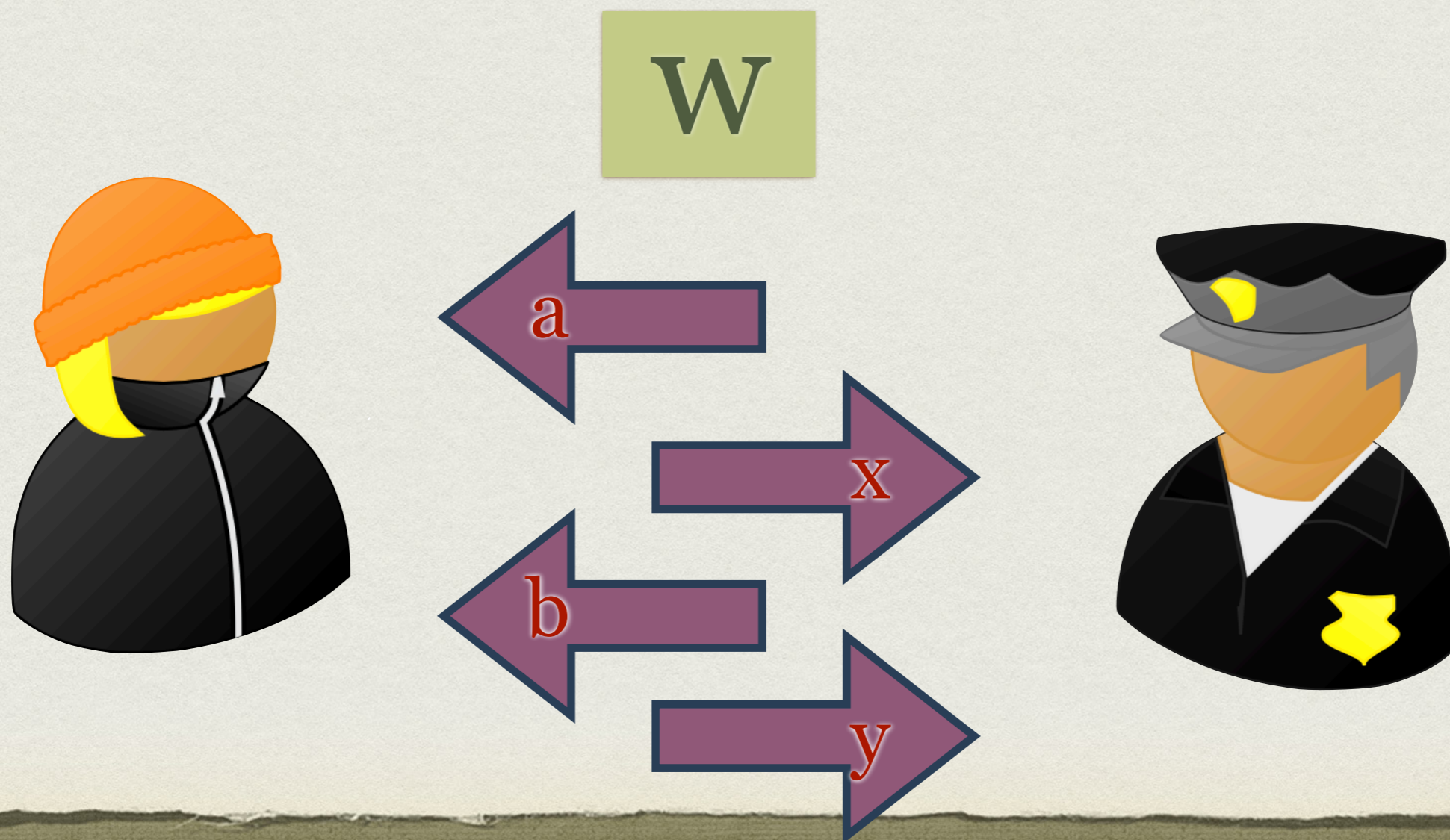


Micali



Rackoff

1985





Goldwasser



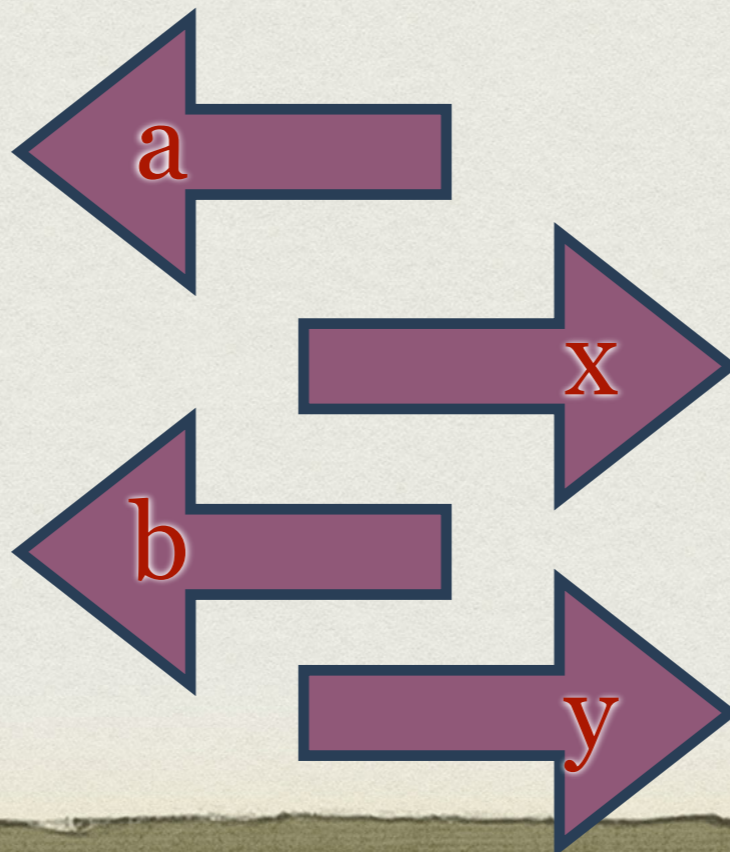
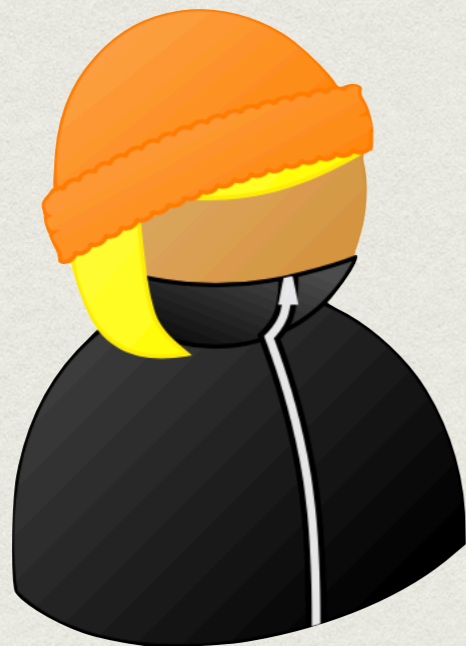
Micali



Rackoff

1985

wεL





Goldwasser



Micali



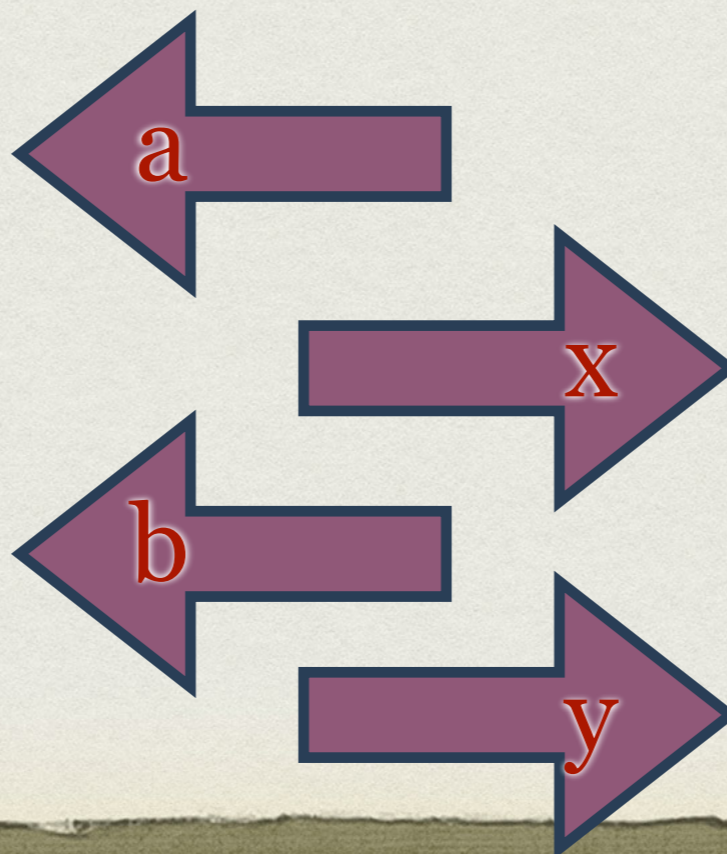
Rackoff

1985

$L \in IP$

$w \in L$

W





Goldwasser



Micali



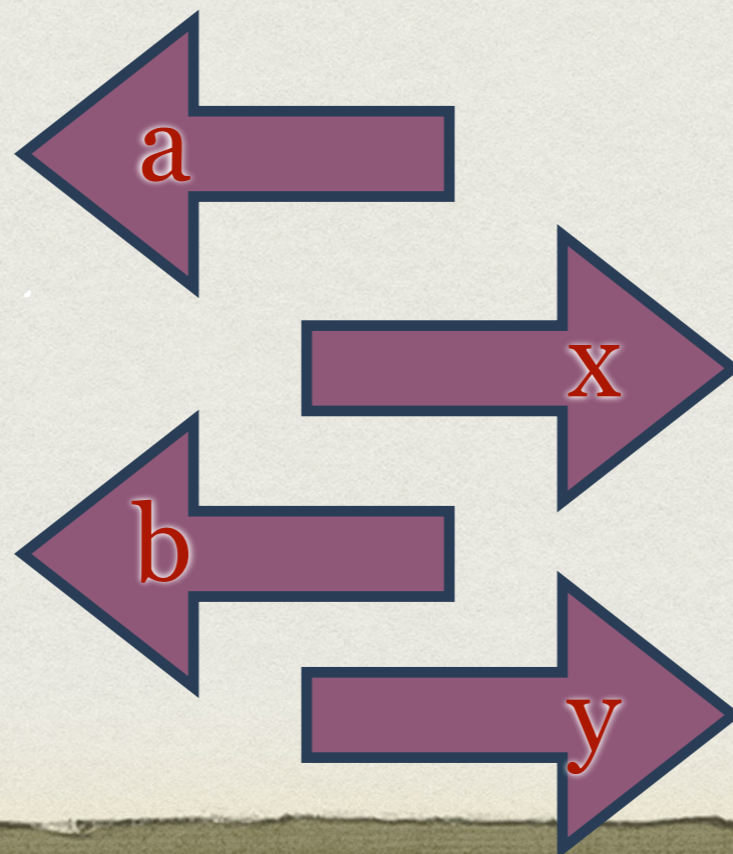
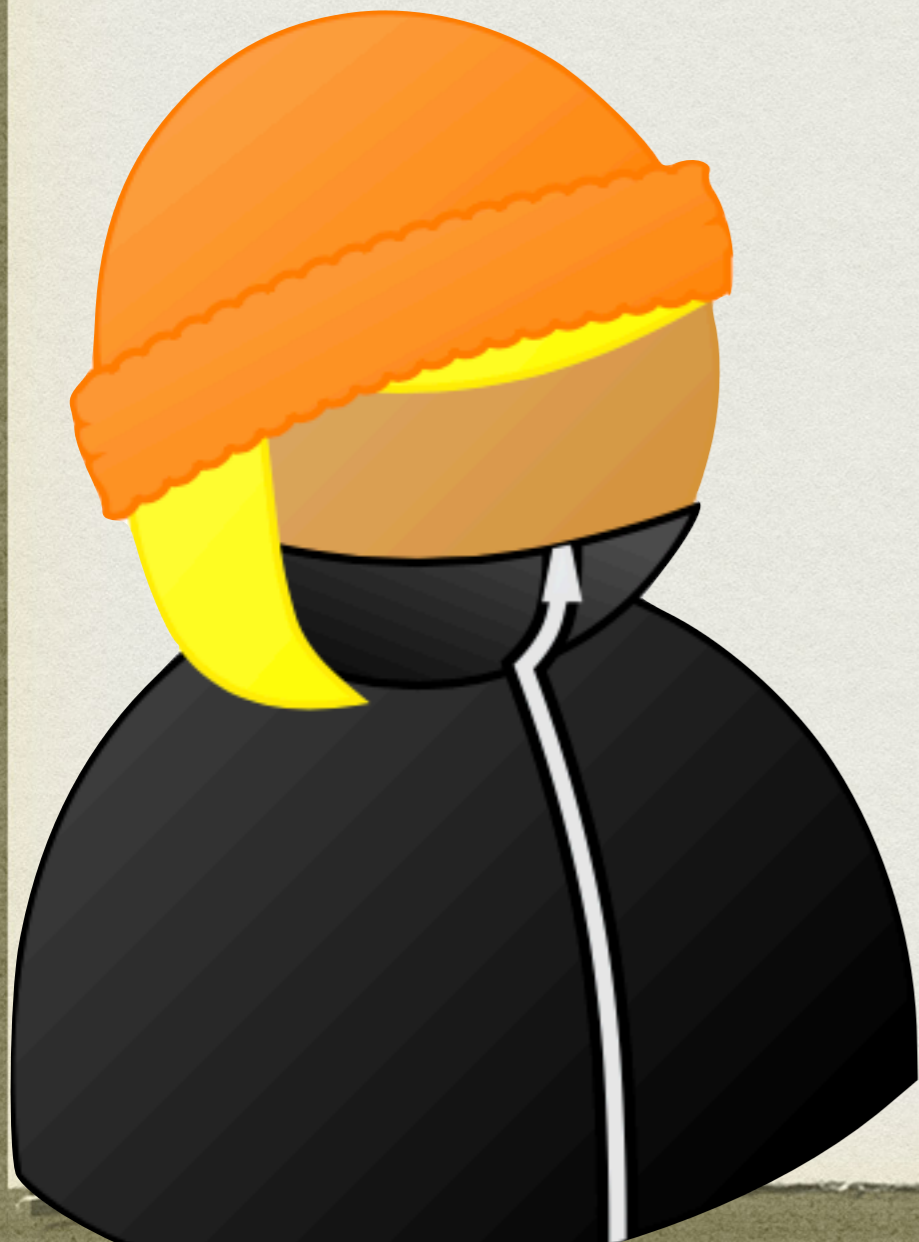
Rackoff

1985

$L \in IP$

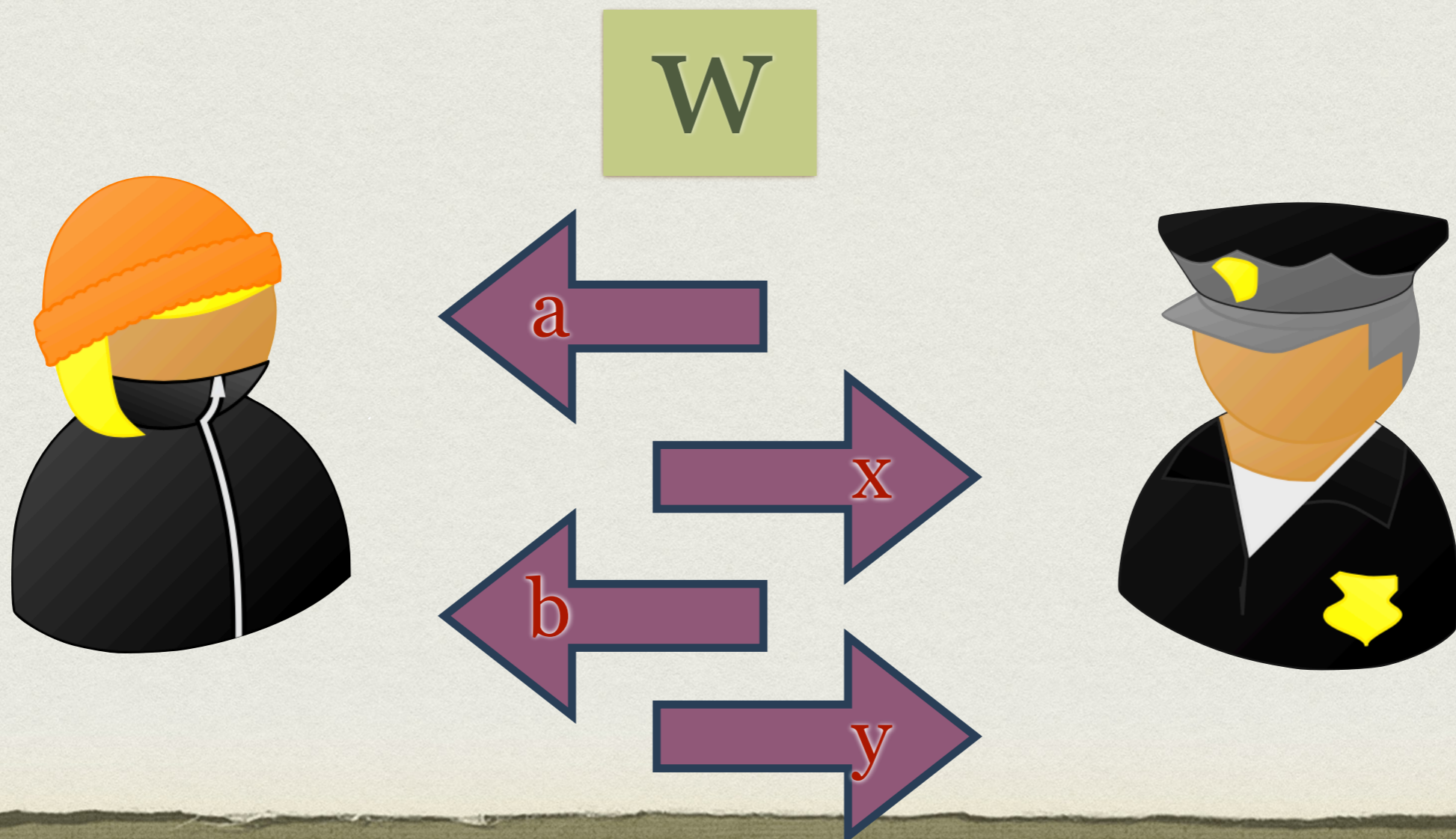
$w \in L$

$w$



# COMPLÉTUDE

$\exists$  ,  $\exists$  ,  $\forall w \in L$ ,  $\text{Prob}[(\text{worker icon} : \text{police officer icon}) \text{ accèpte}] \geq 1 - \epsilon$

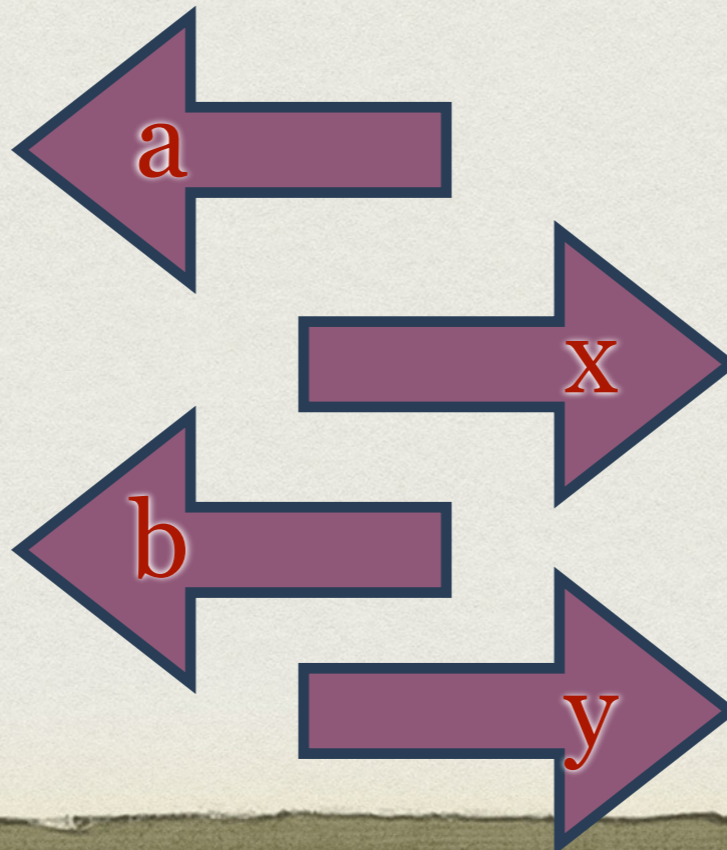


# COMPLÉTUDE

$w \in L$

$\exists$  ,  $\exists$  ,  $\forall w \in L$ ,  $\text{Prob}[(\text{worker icon} : \text{police icon}) \text{ accepte}] \geq 1 - \epsilon$

W

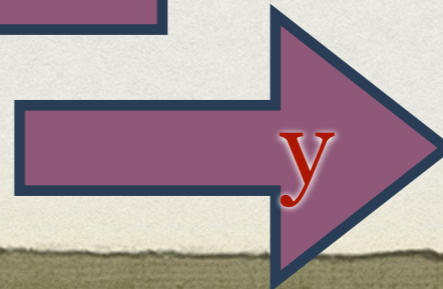
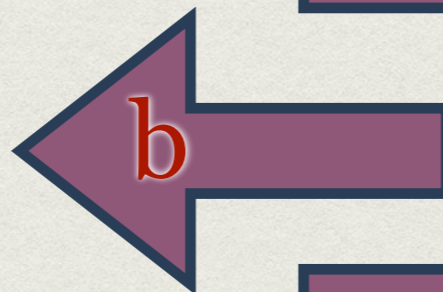
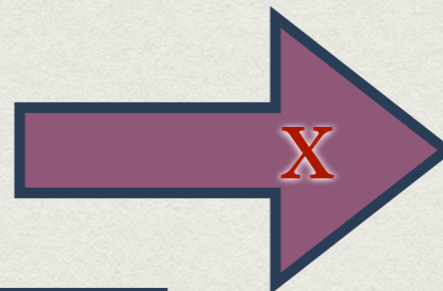
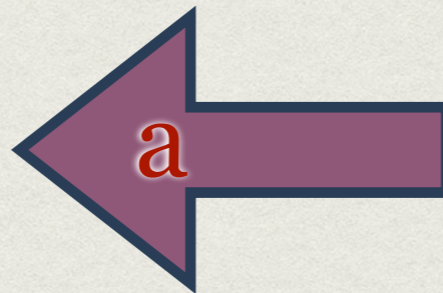
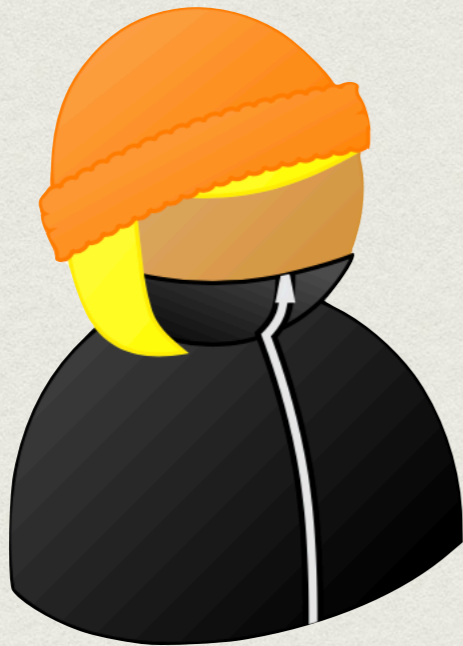


# COMPLÉTUDE

$w \in L$

$\exists$  ,  $\exists$  ,  $\forall w \in L$ ,  $\text{Prob}[(\text{worker icon} : \text{police icon}) \text{ accepte}] \geq 1 - \epsilon$

$w$

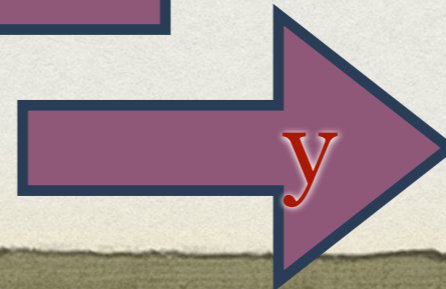
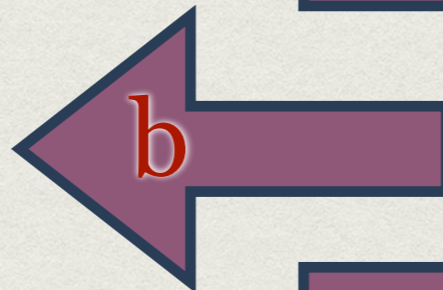
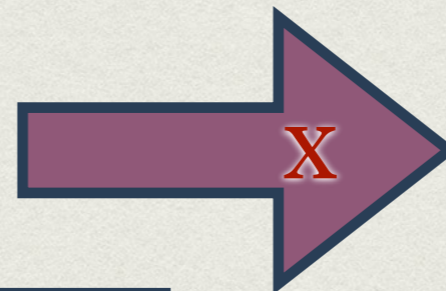
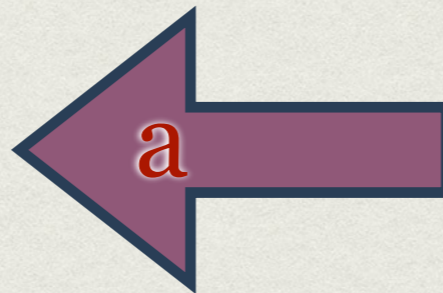
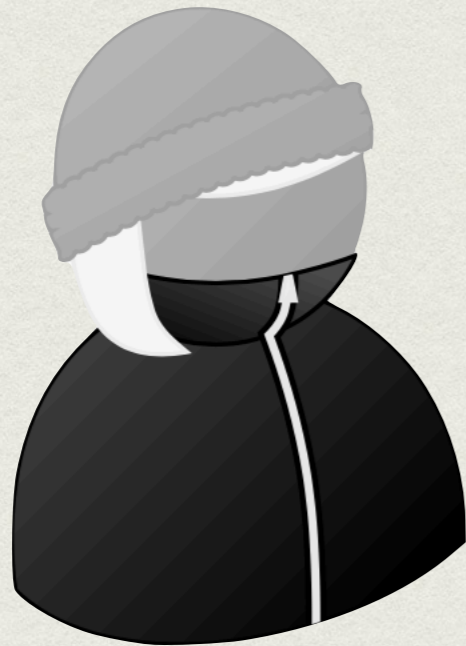


accepte

# COHÉRENCE

$\exists$  , et  $\forall$  ,  $\forall w \notin L$ ,  $\text{Prob}[(\text{hacker icon} : \text{police icon}) \text{ accepte}] \leq \epsilon$

W



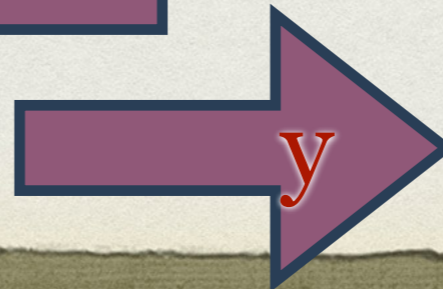
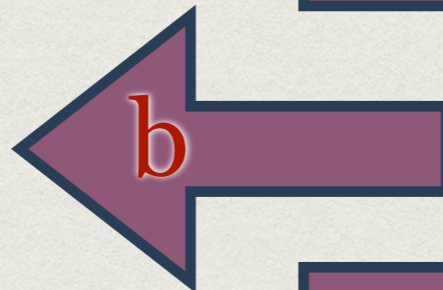
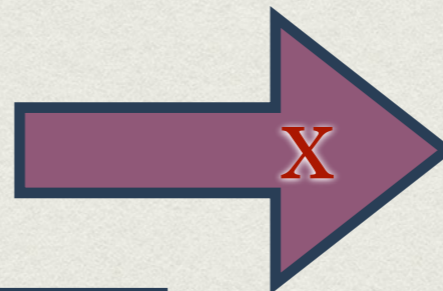
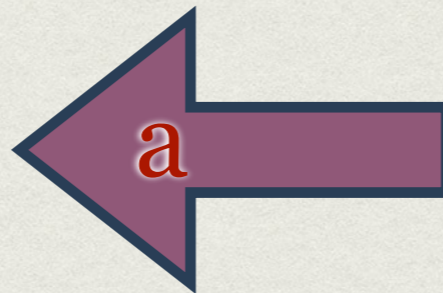


# COHÉRENCE

$w \notin L$

$\exists$  , et  $\forall$  ,  $\forall w \notin L$ ,  $\text{Prob}[(\text{hacker icon} : \text{police icon}) \text{ accepte}] \leq \epsilon$

W

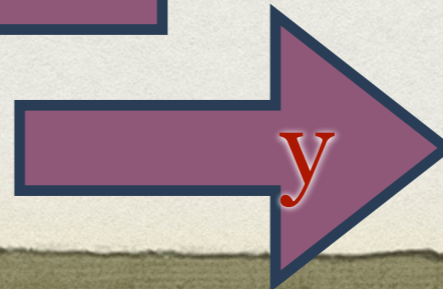
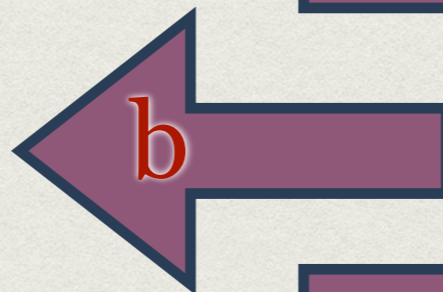
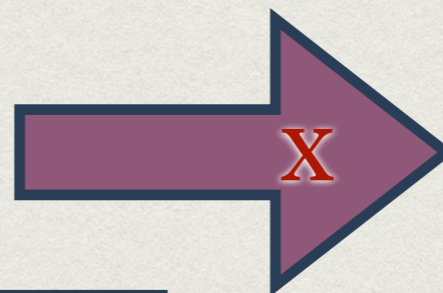
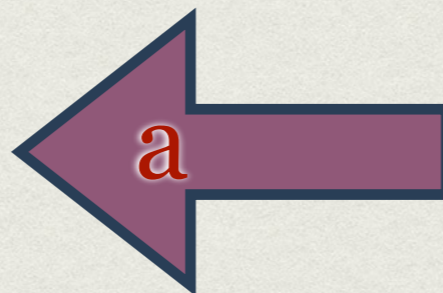


# COHÉRENCE

$w \notin L$

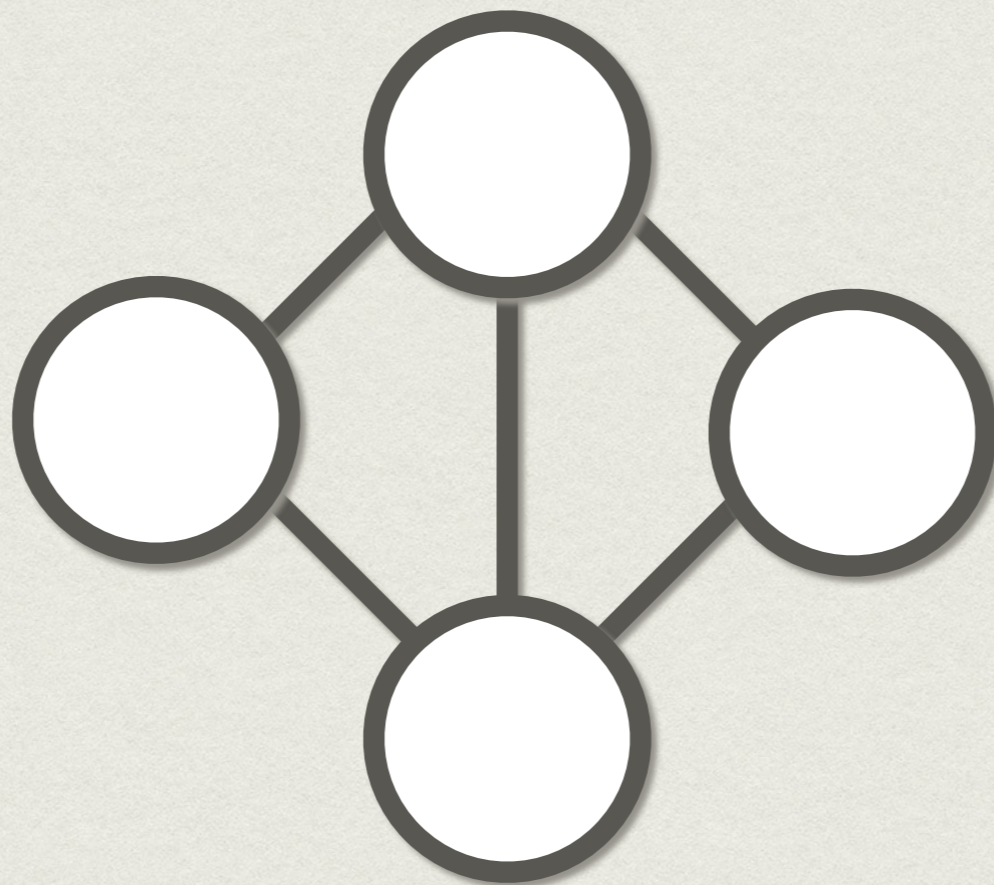
$\exists$  , et  $\forall$  ,  $\forall w \notin L$ ,  $\text{Prob}[(\text{hacker icon} : \text{police icon}) \text{ accepte}] \leq \epsilon$

$w$



rejète

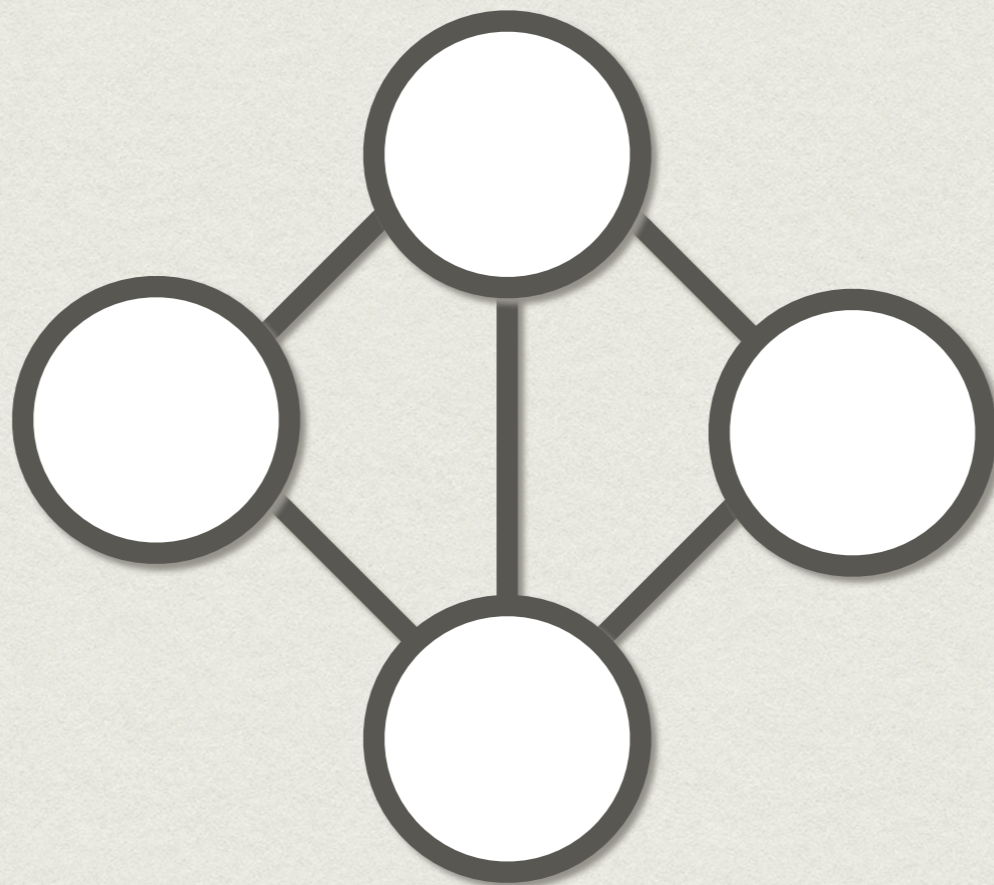
# 3-COL



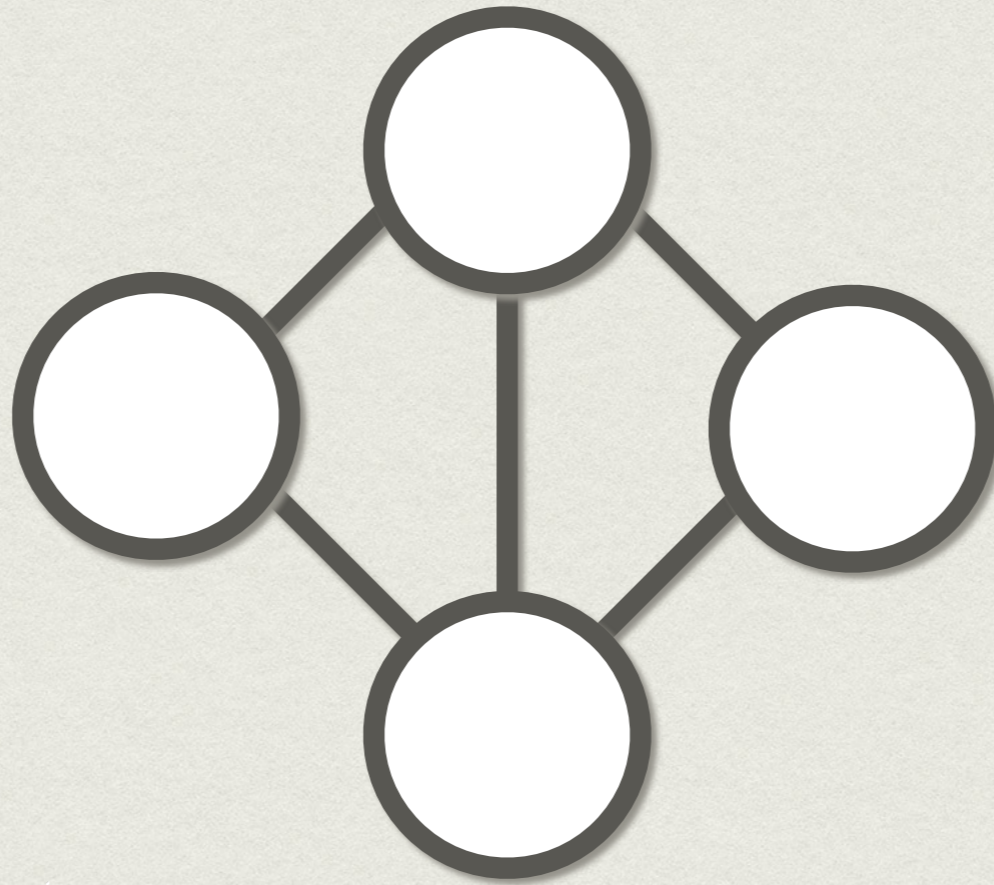
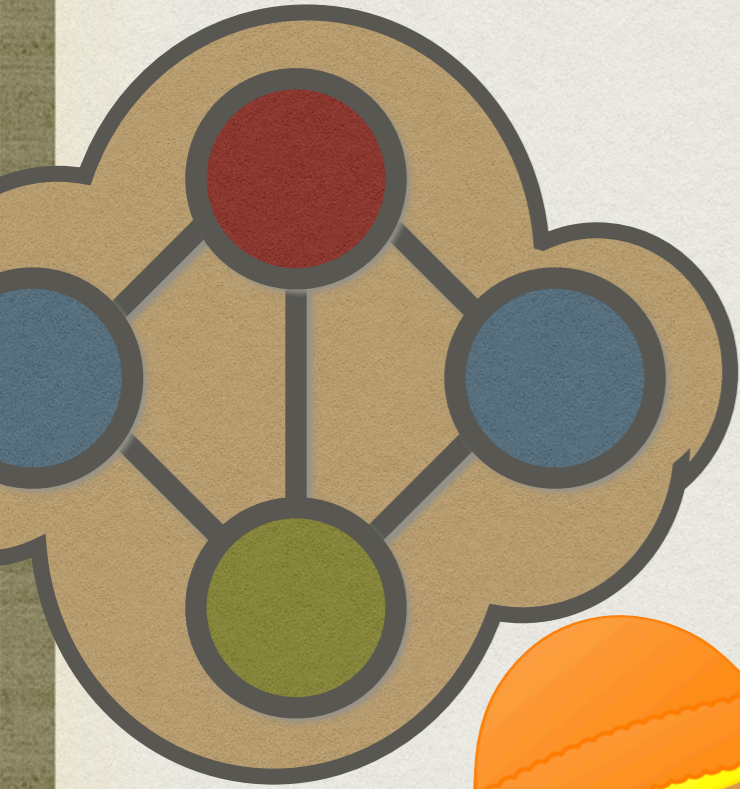
3-COL



# 3-COL

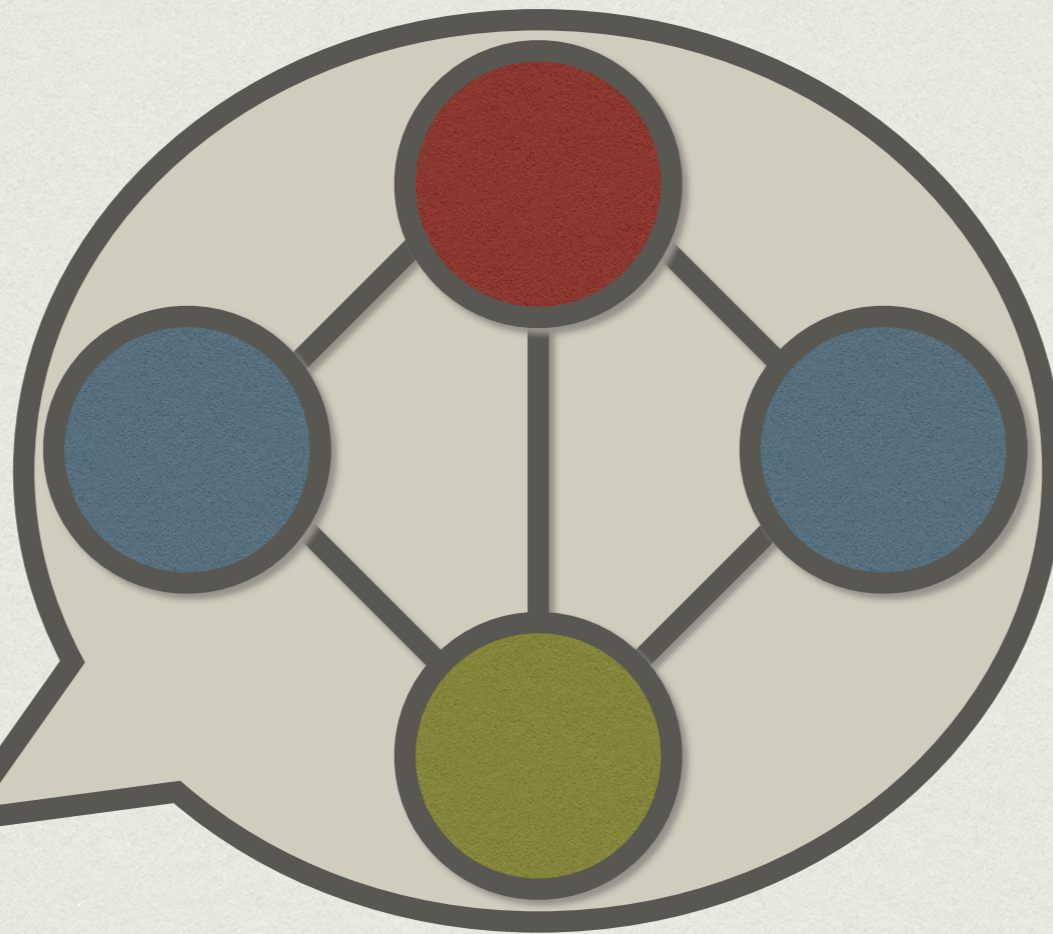
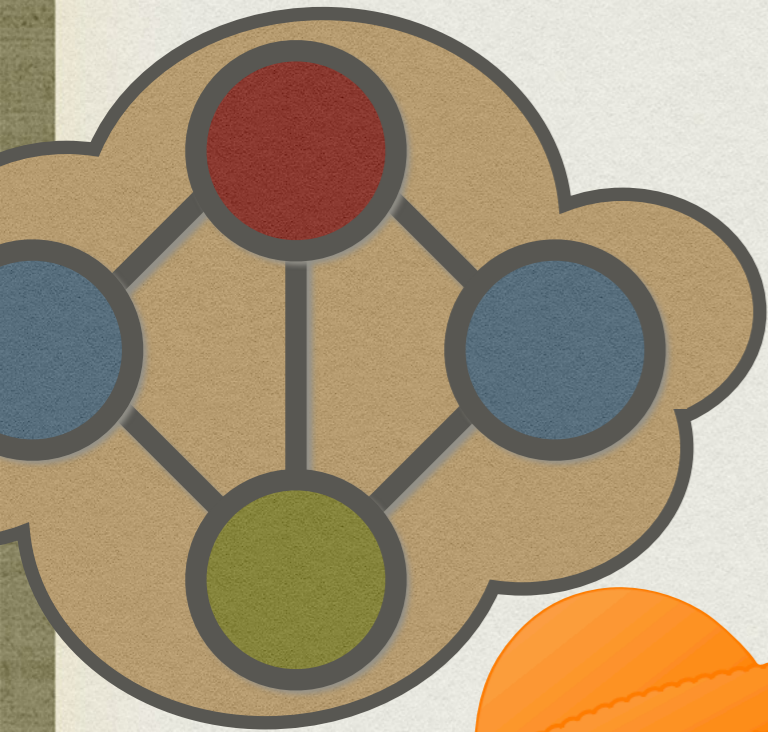


# 3-COL



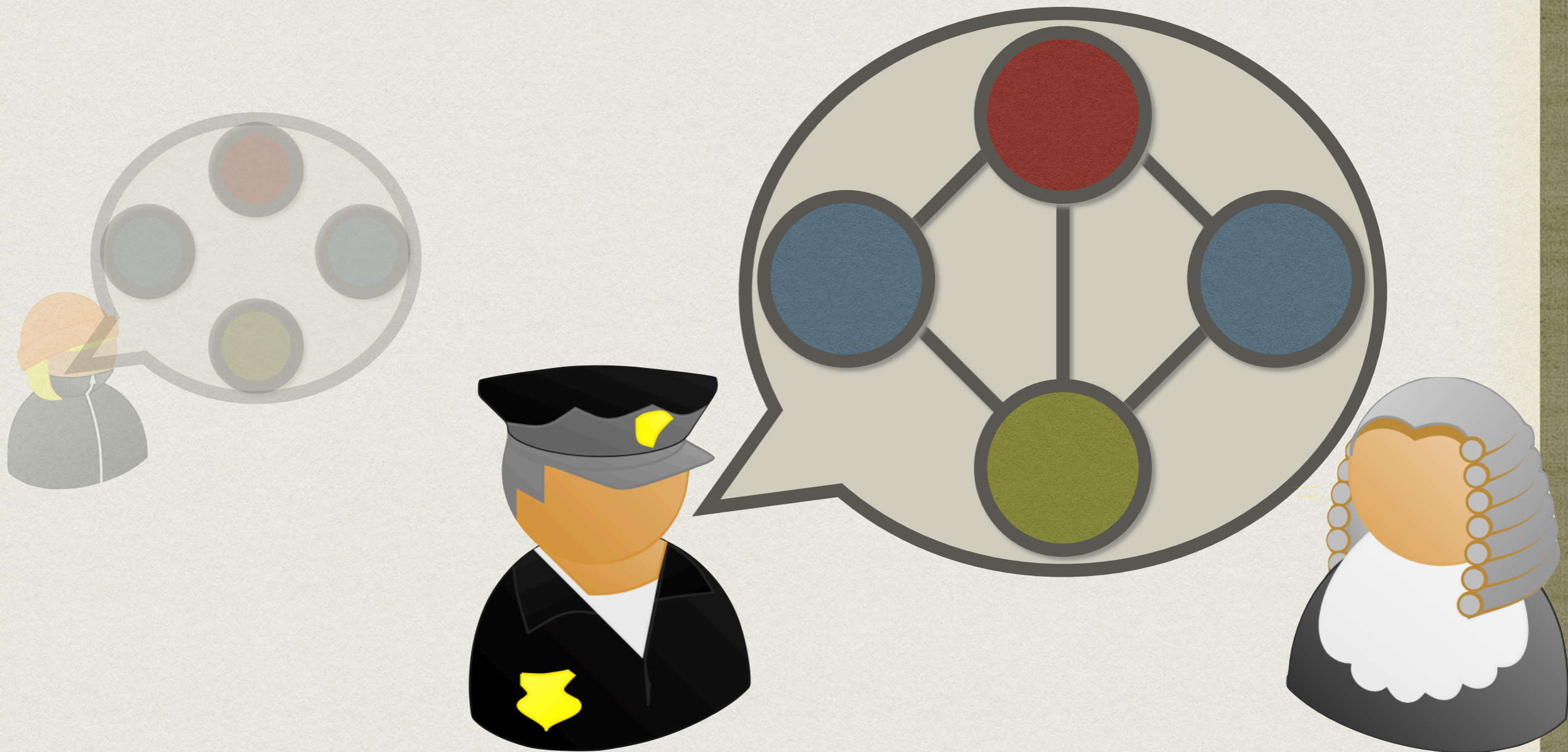
3-COL

COMPLÉTUDE



COHÉRENCE

# 3-COL



## TRANSFÉRABLE



# 3-COL (86)



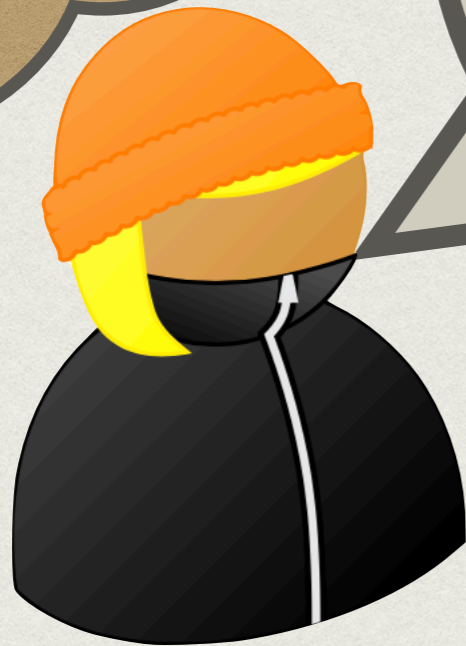
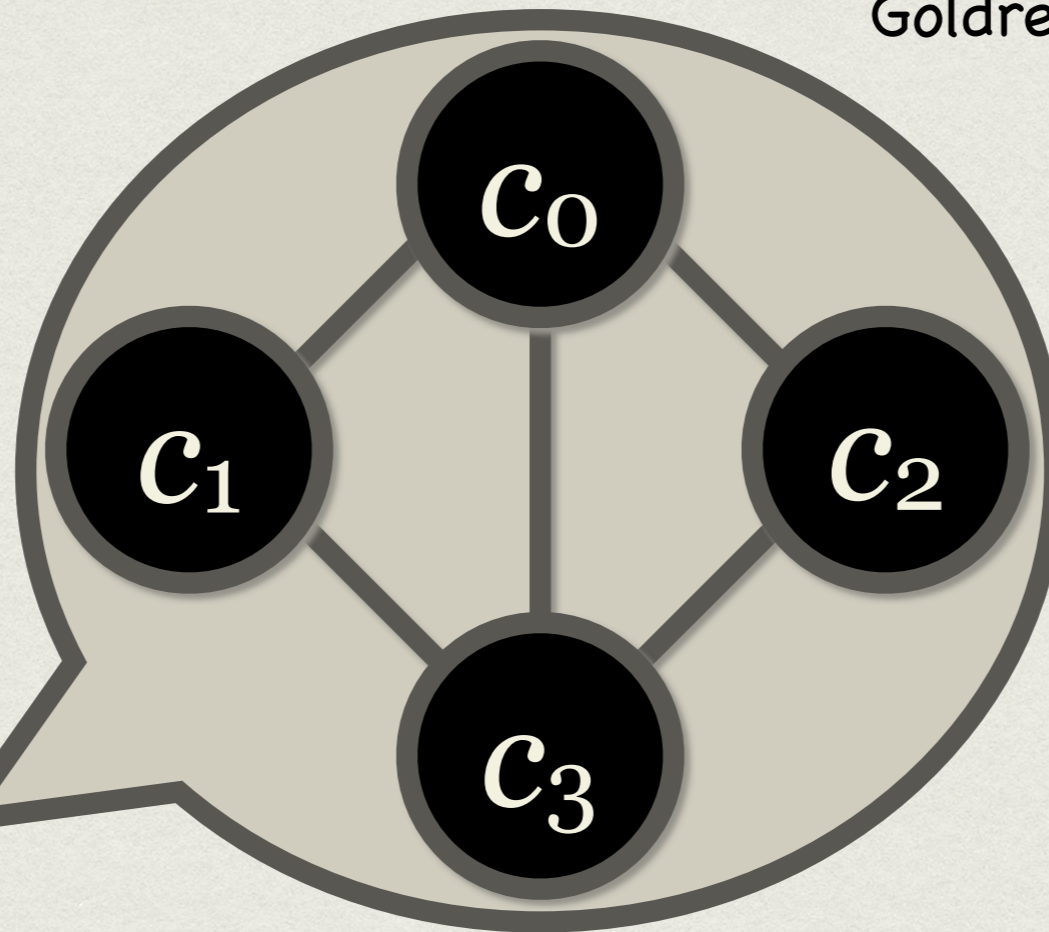
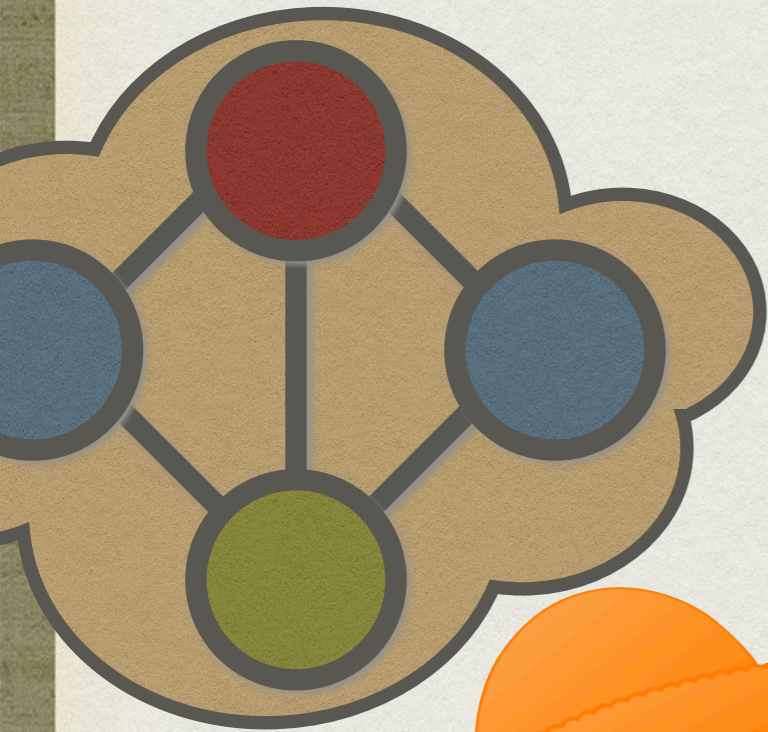
Goldreich



Micali



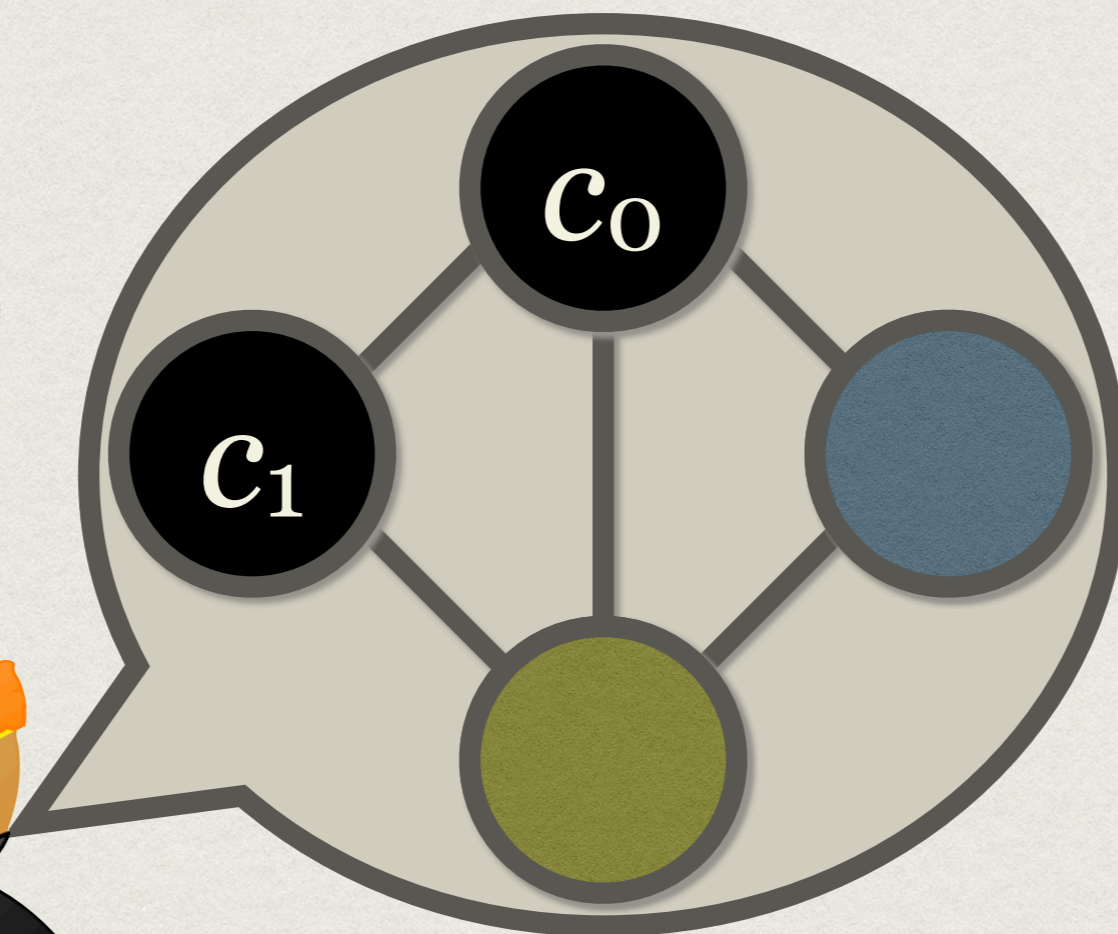
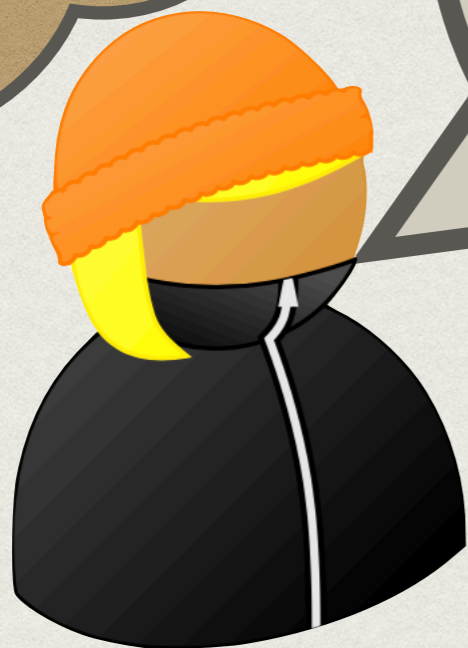
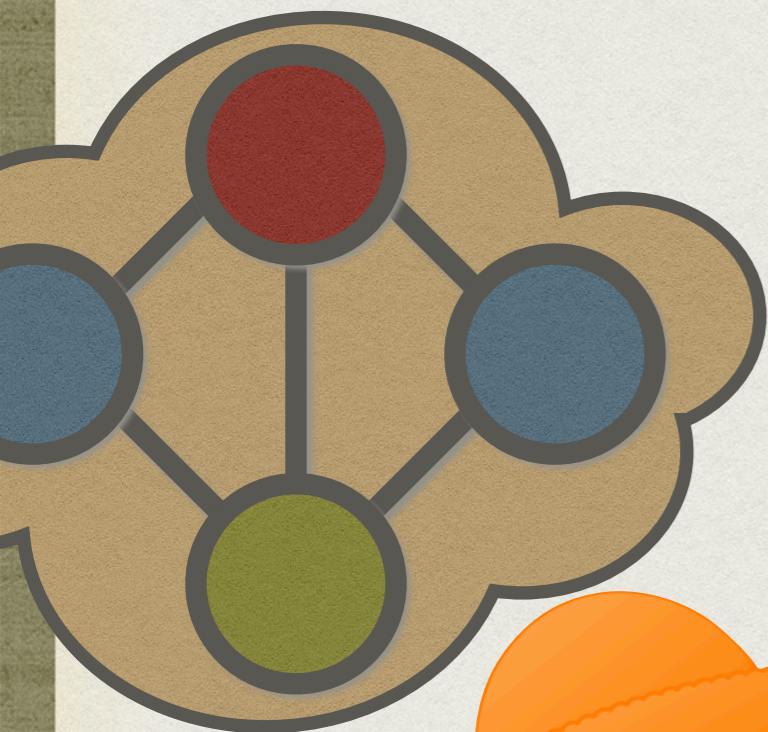
Wigderson



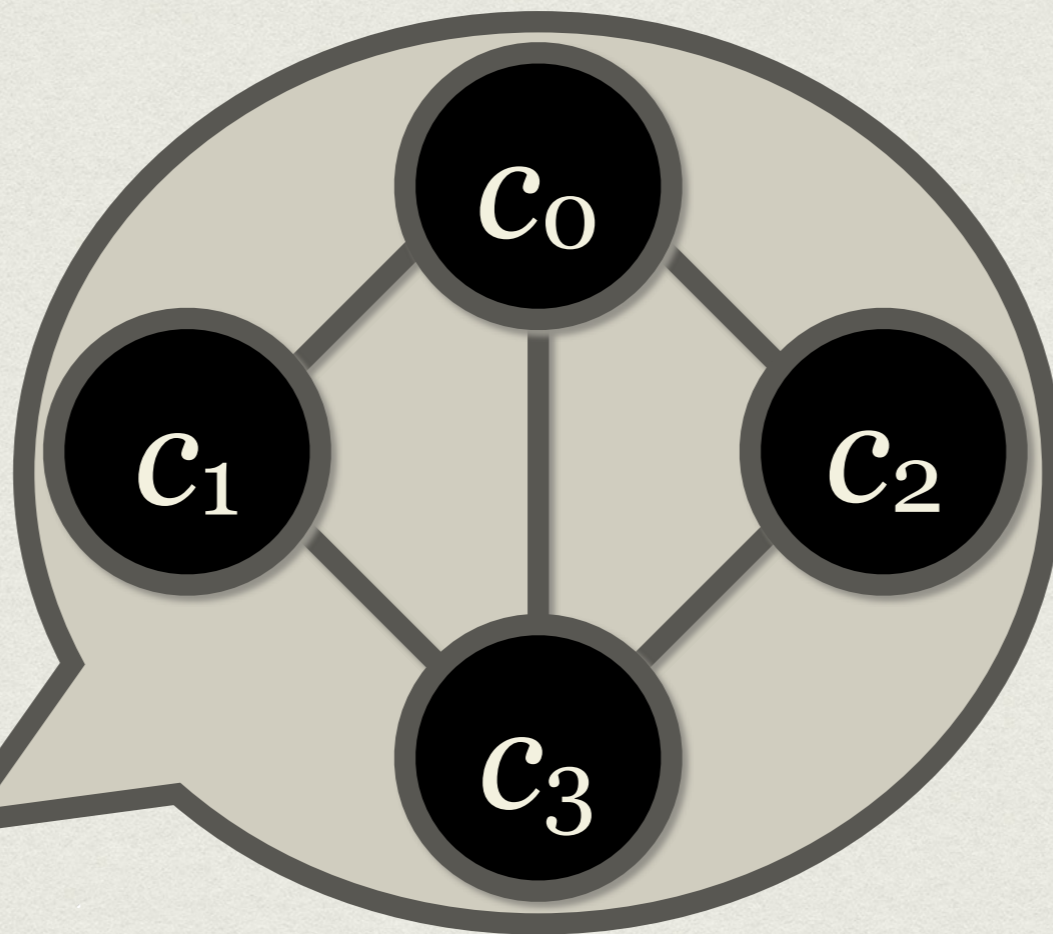
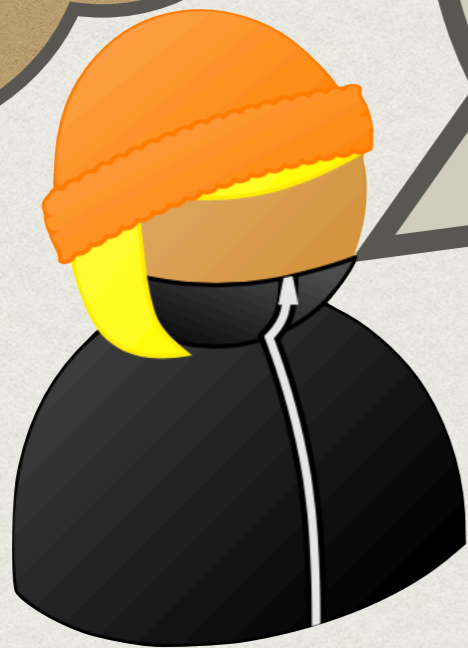
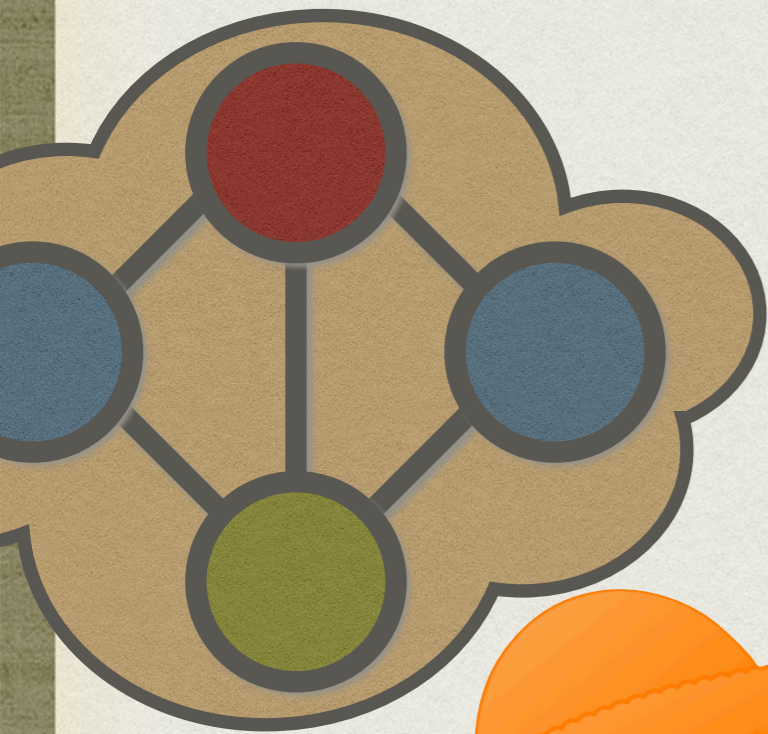
2-3



# 3-COL



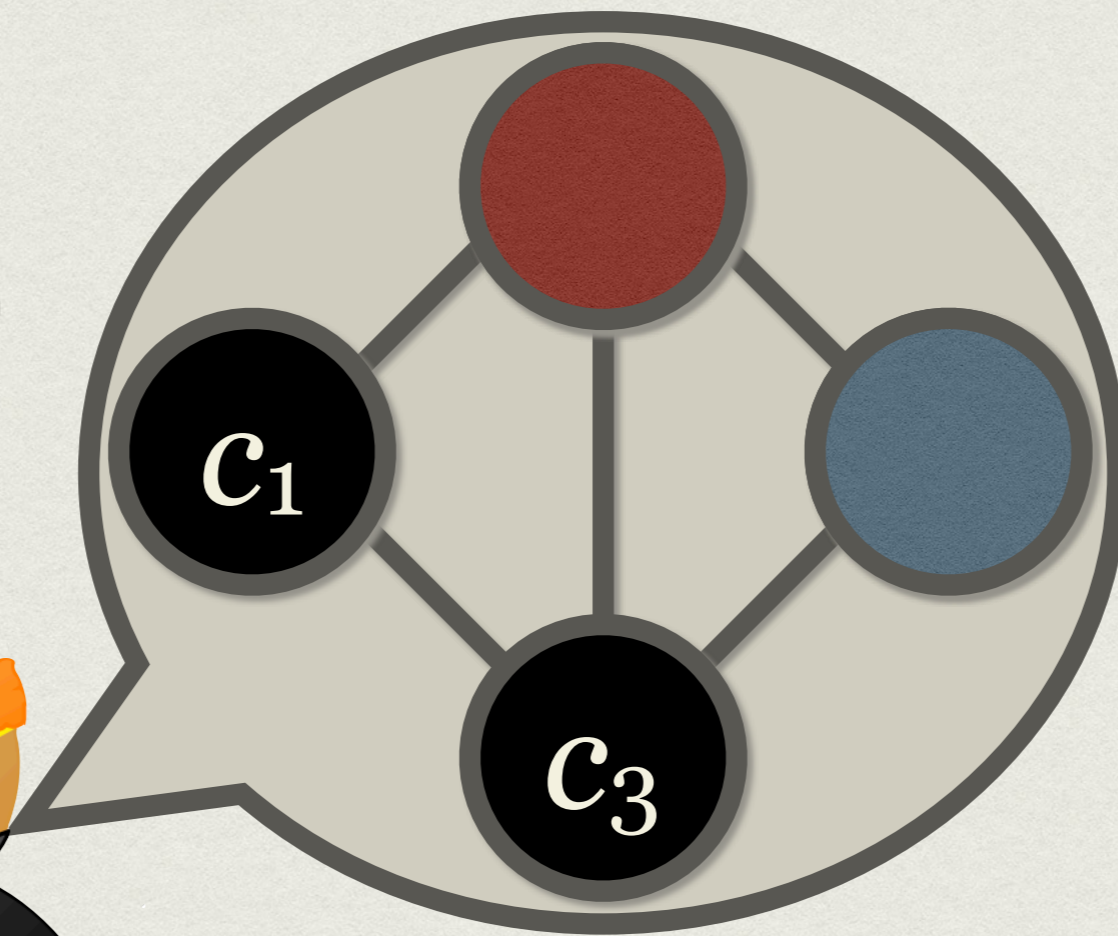
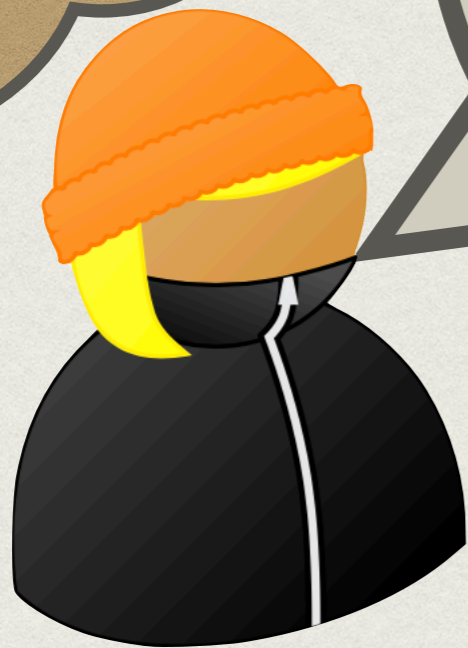
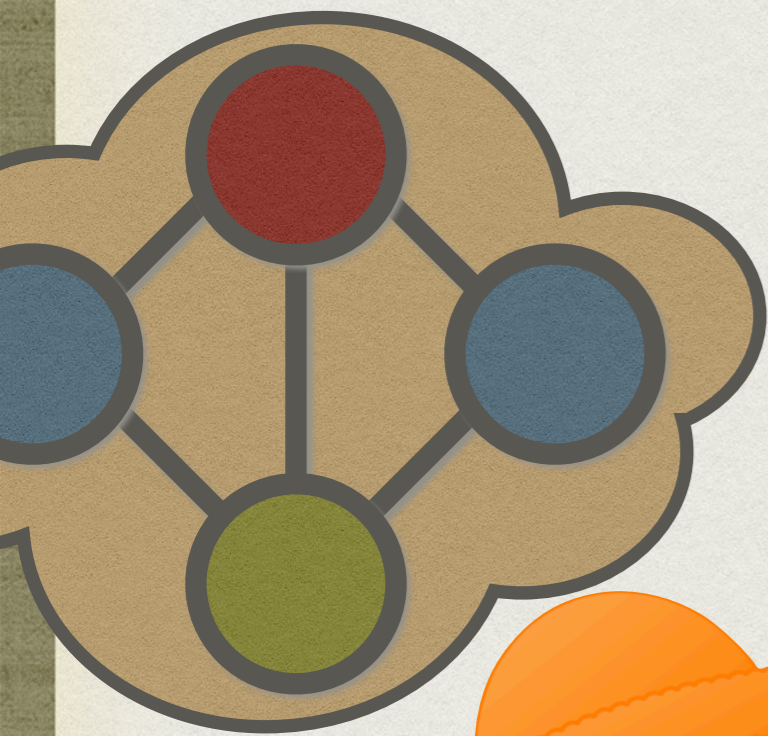
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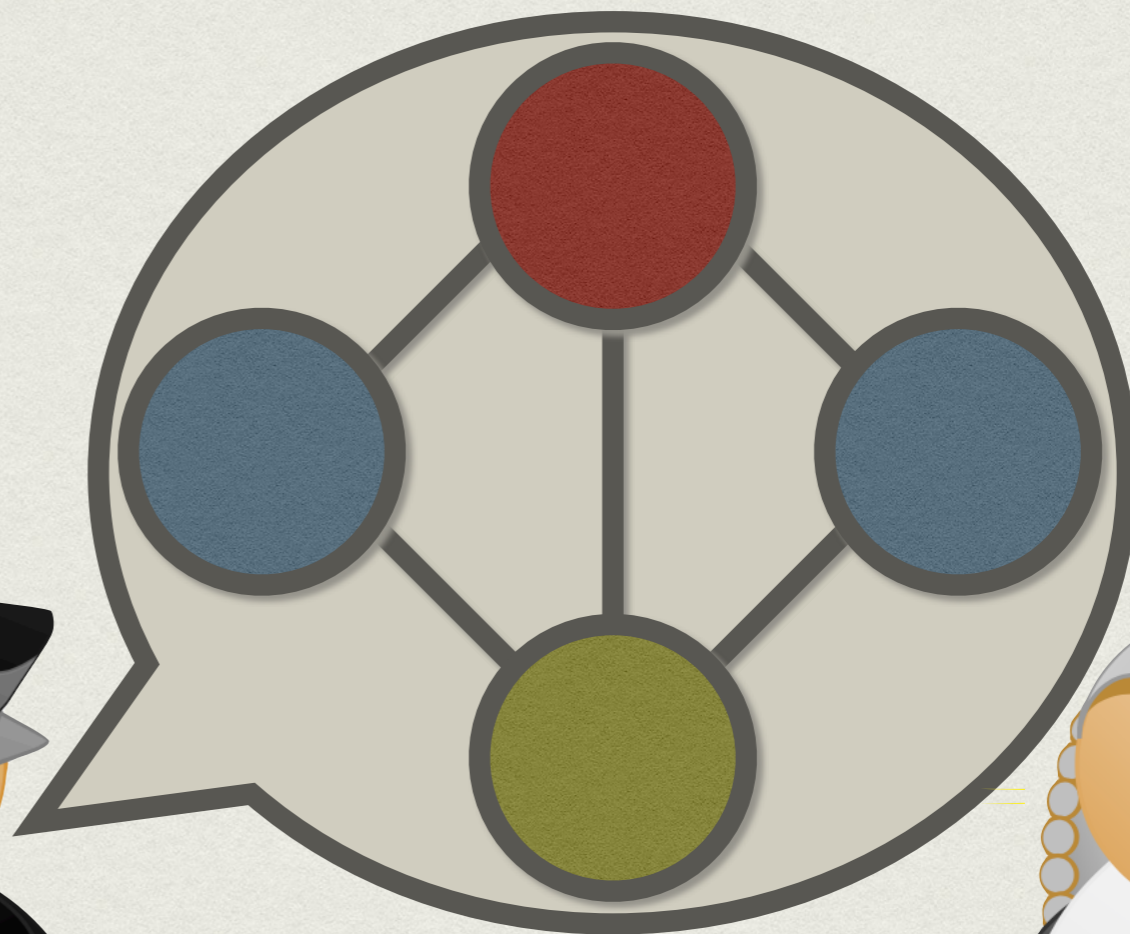
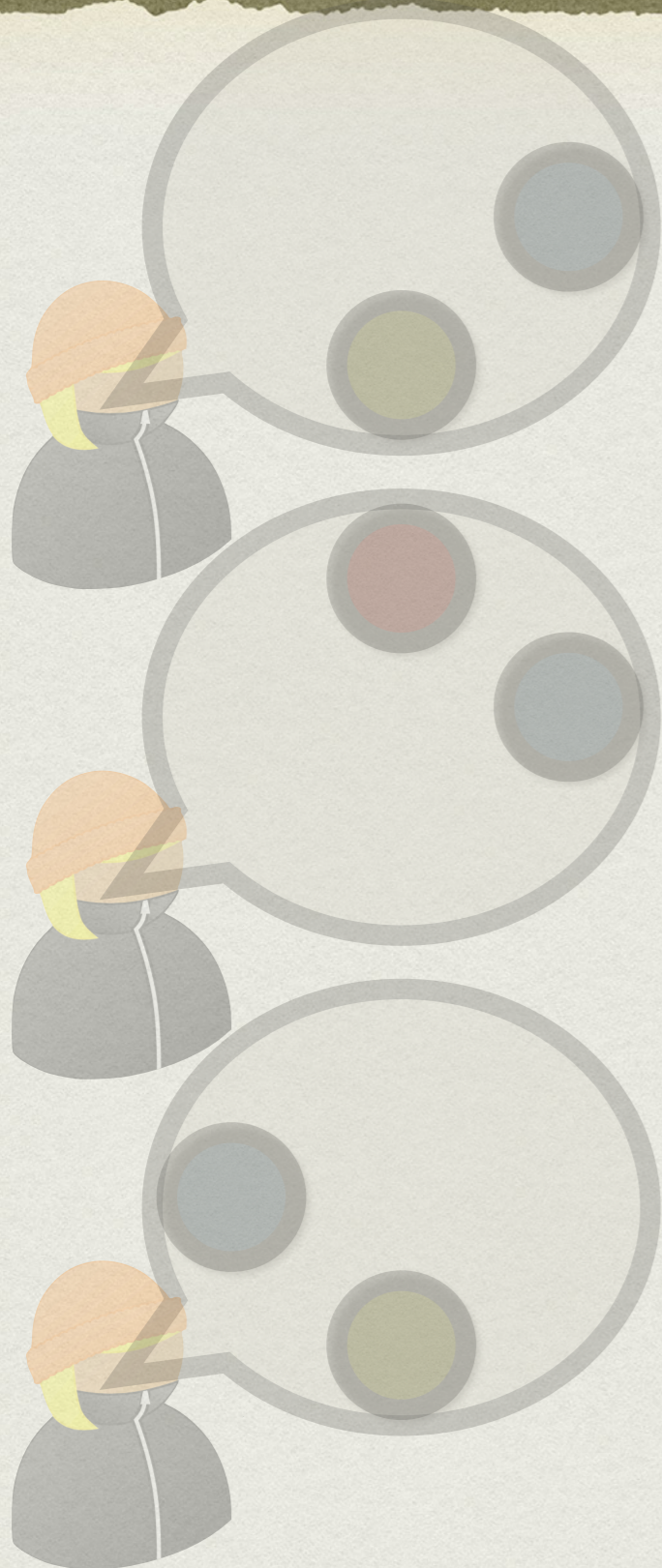
0-2



# 3-COL

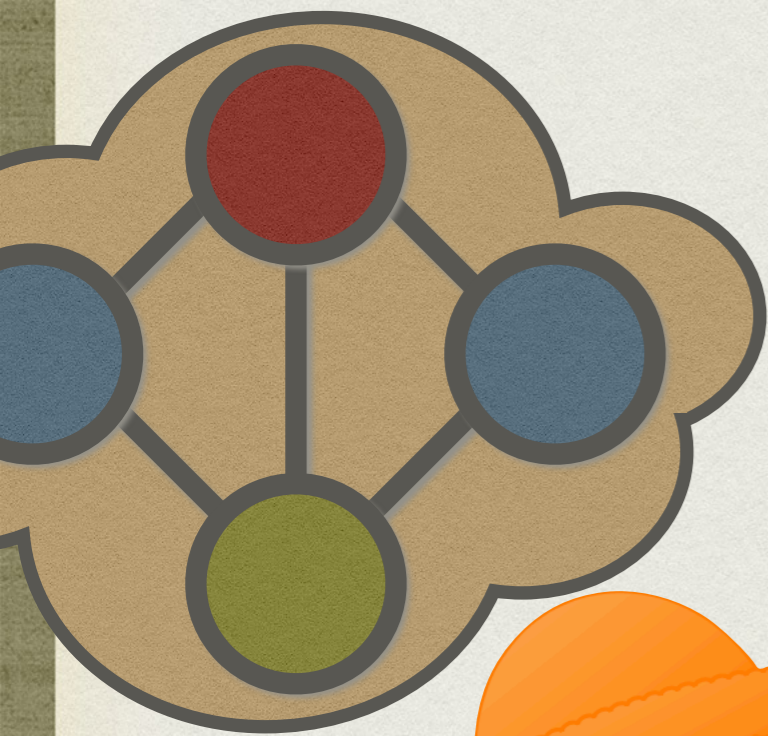


3-COL

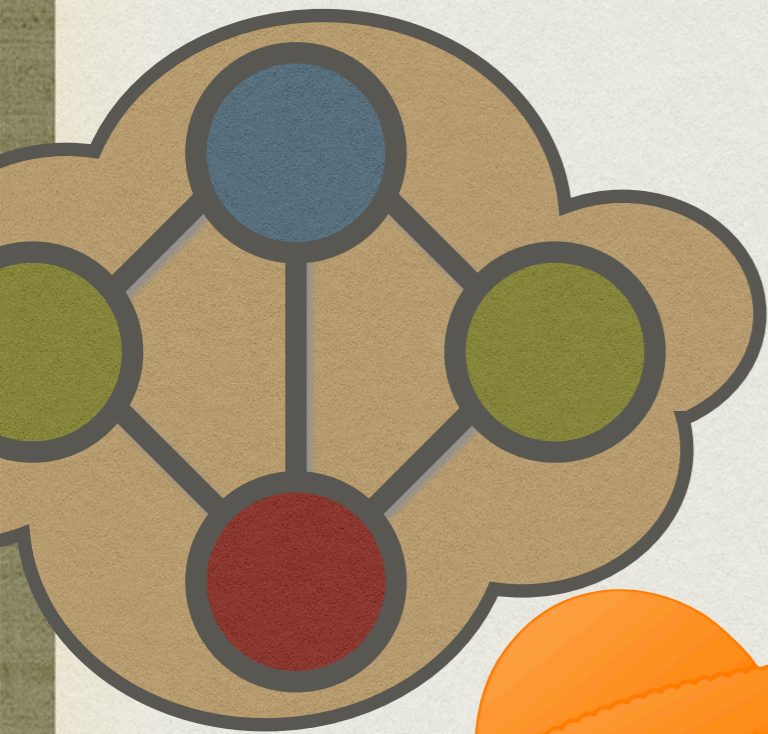


TRANSFÉRABLE

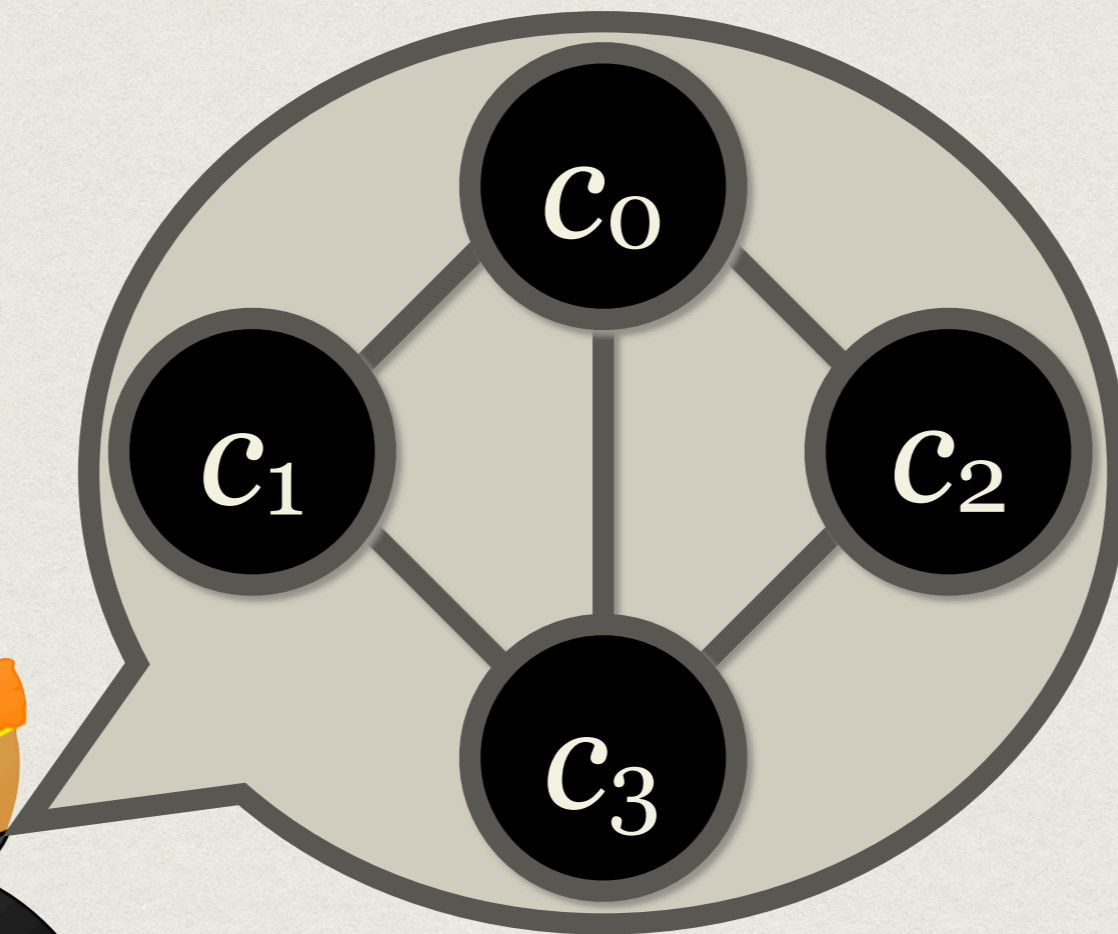
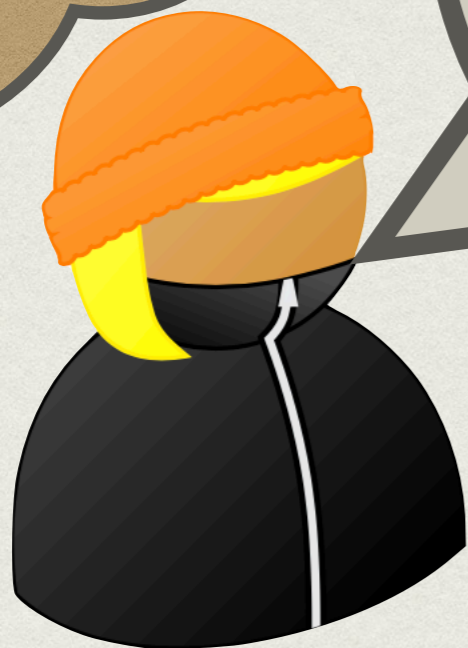
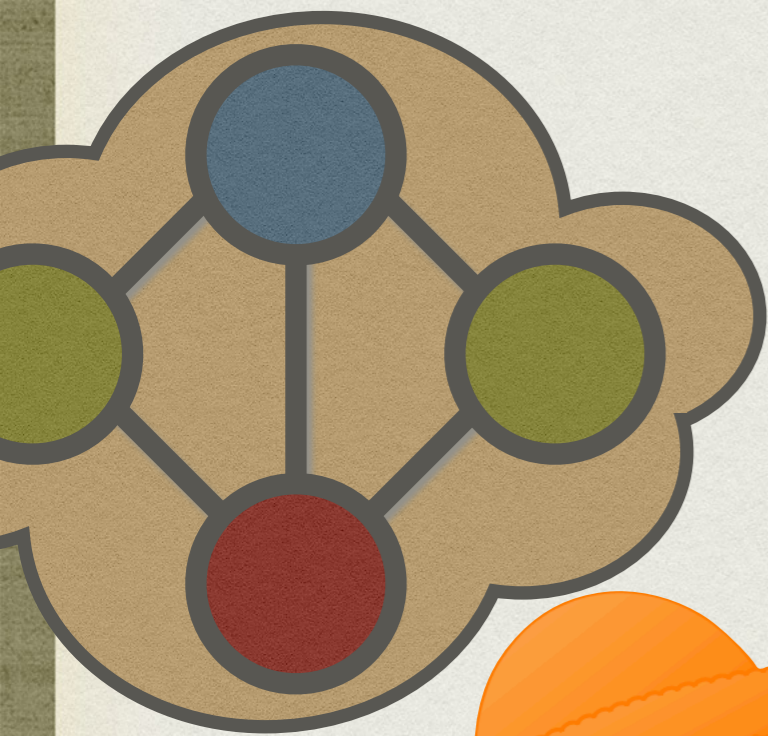
3-COL



3-COL

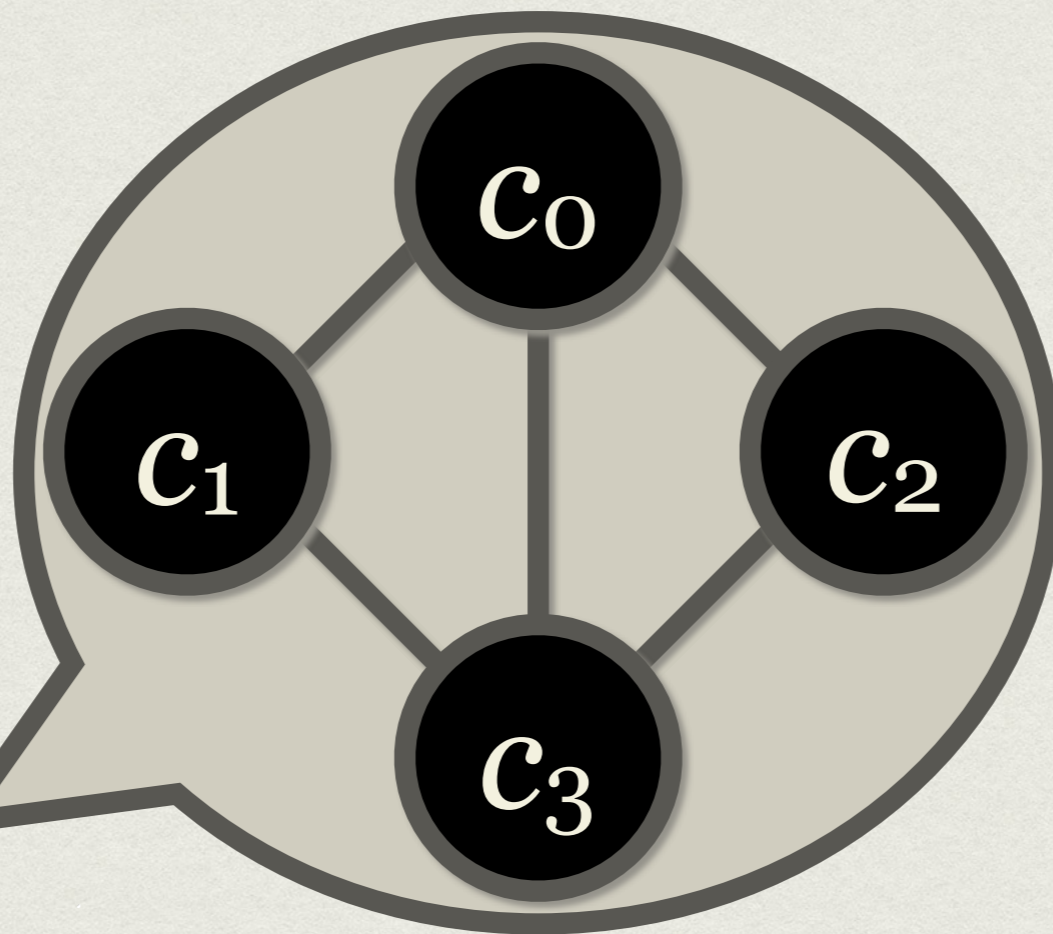
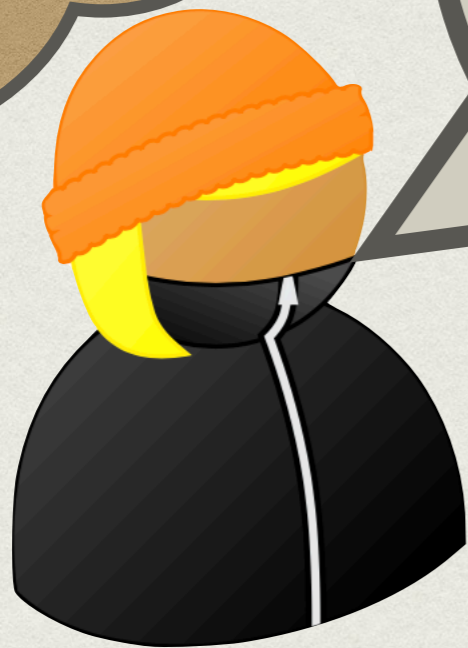
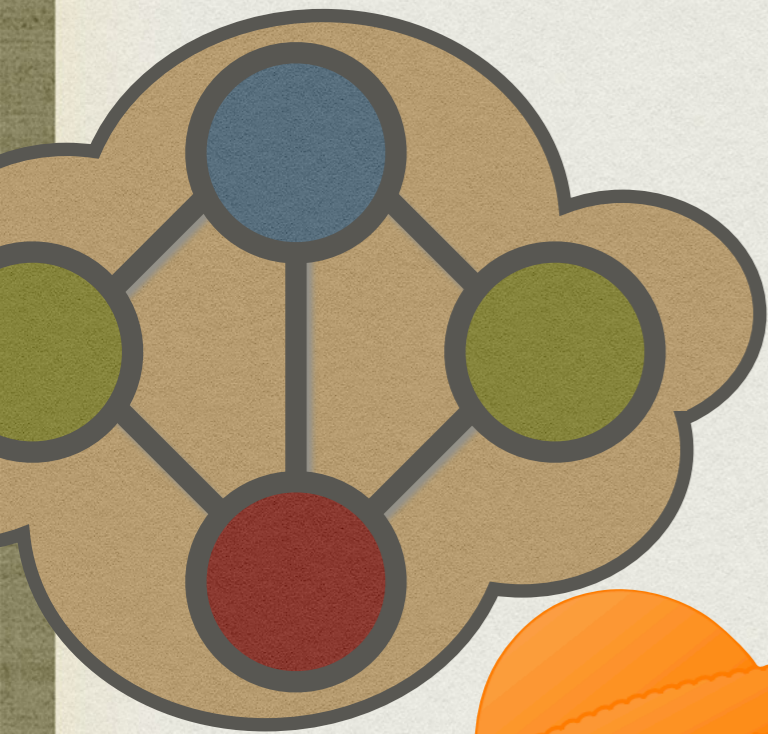


# 3-COL





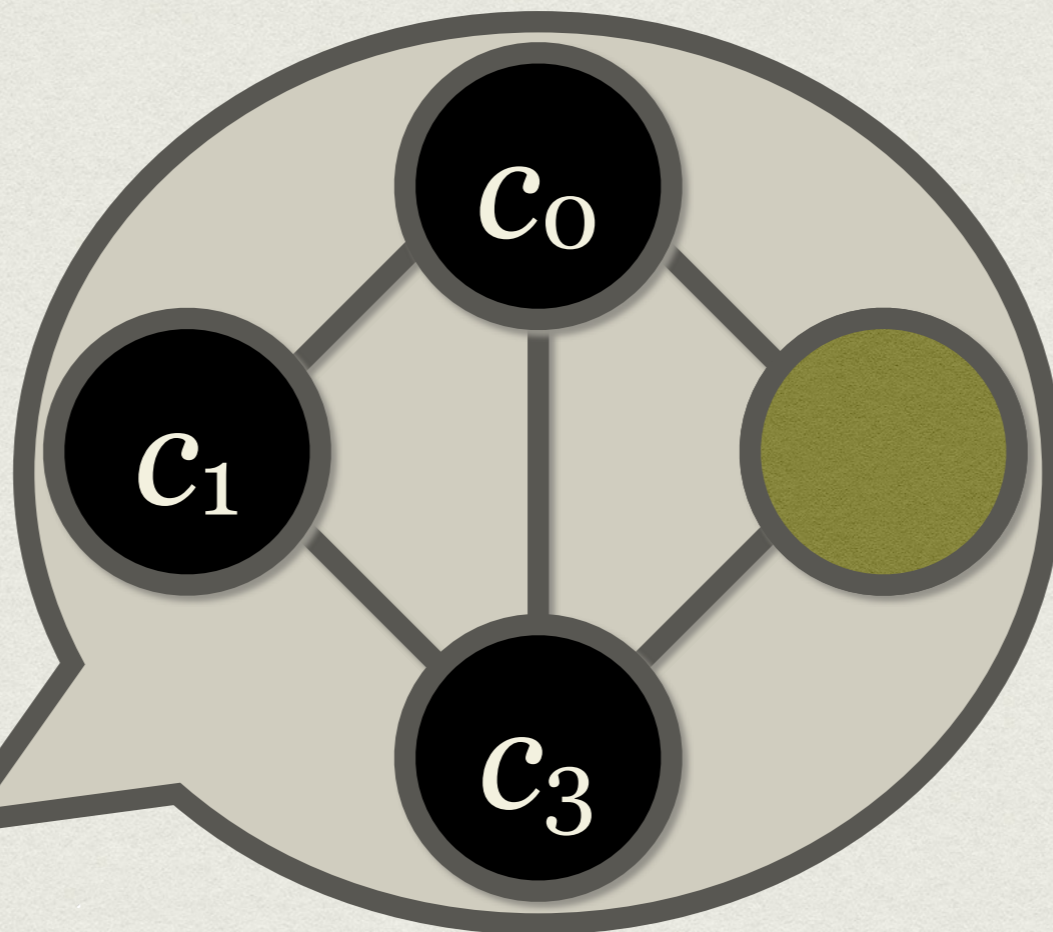
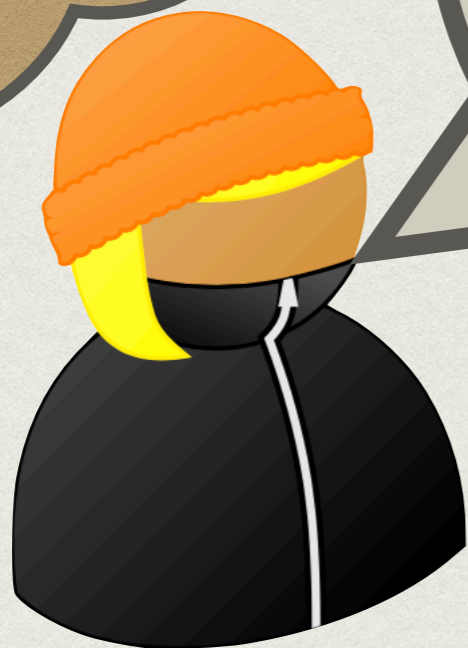
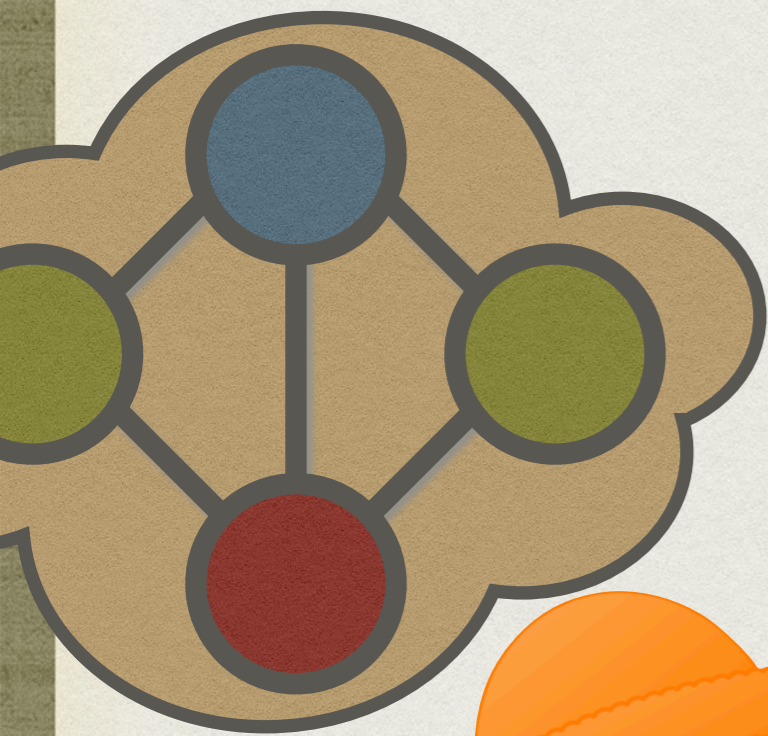
# 3-COL



2-3



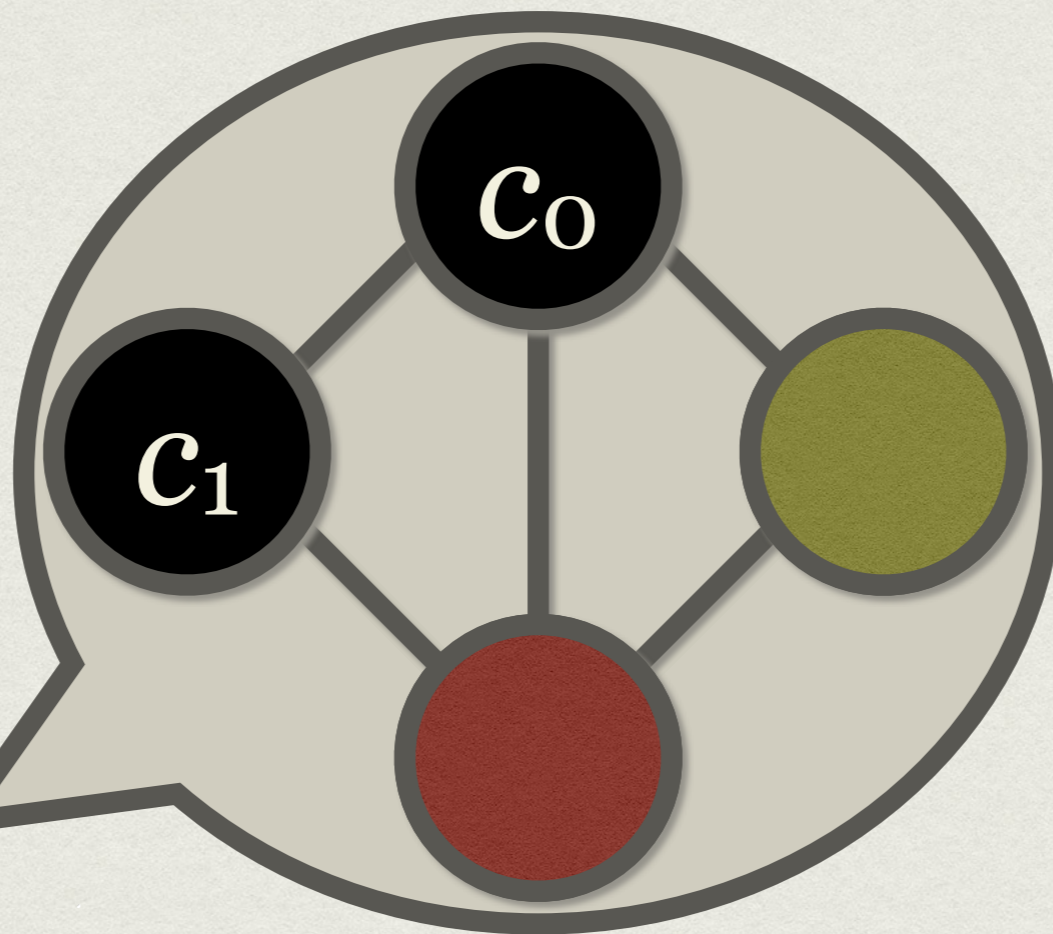
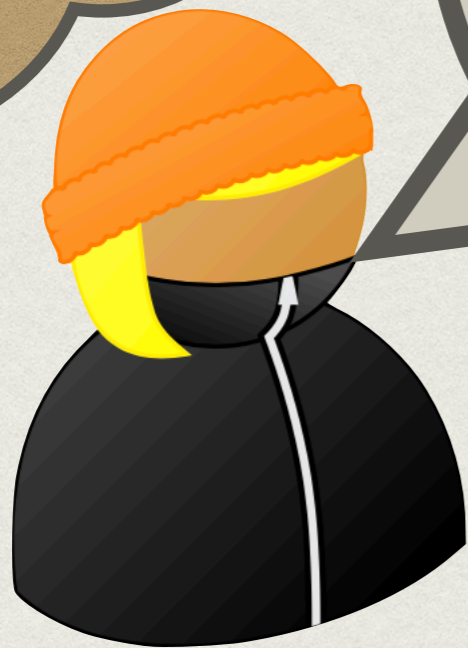
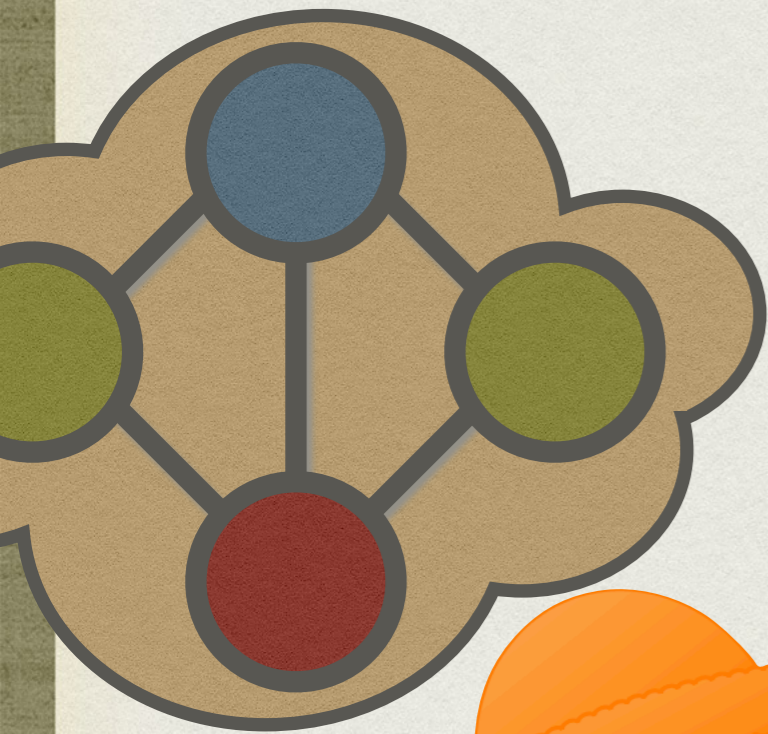
# 3-COL



2-3



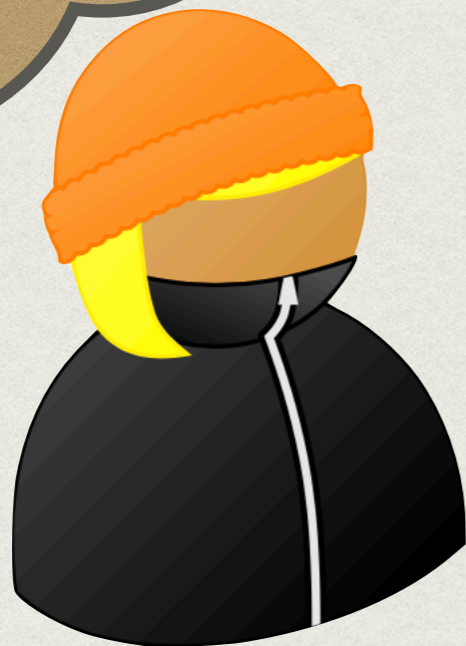
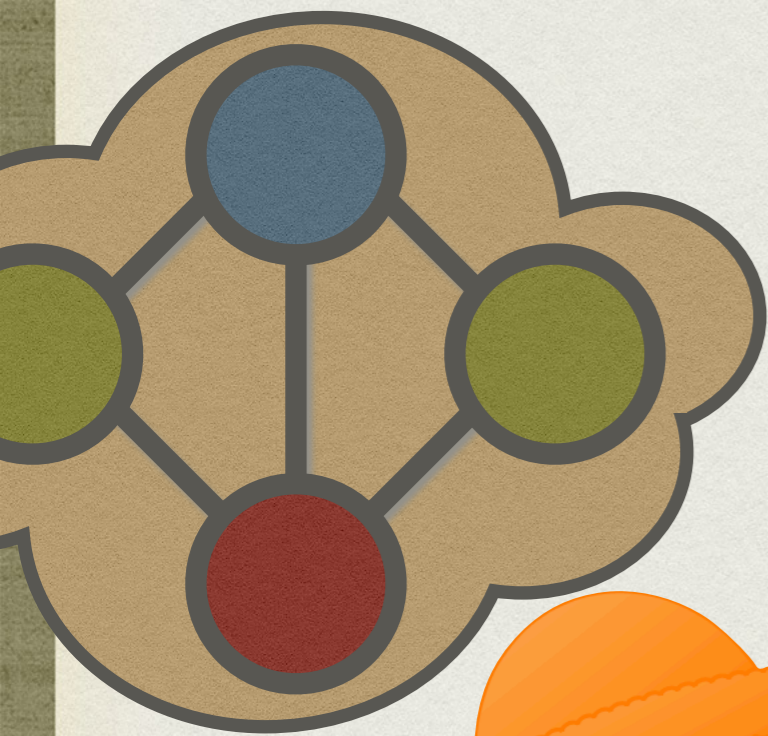
# 3-COL



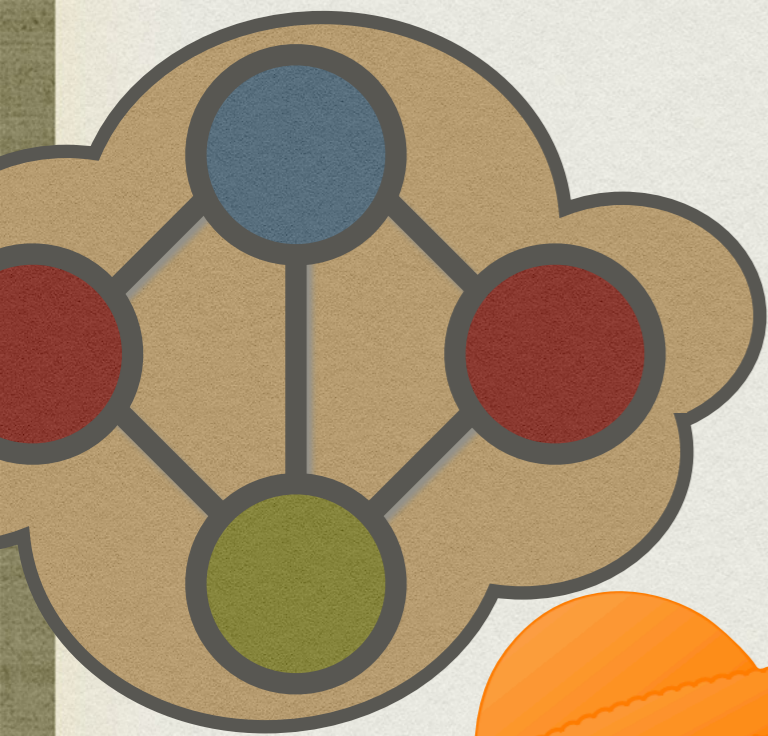
2-3



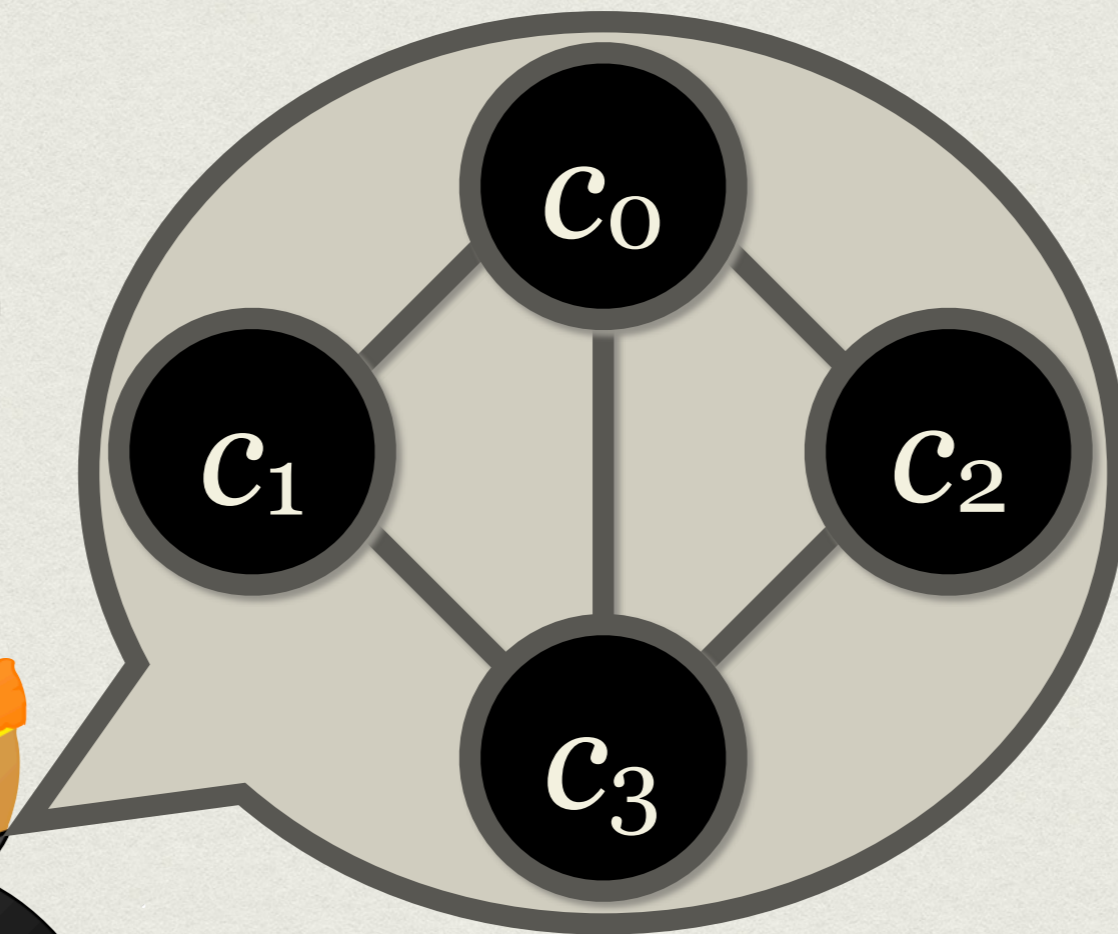
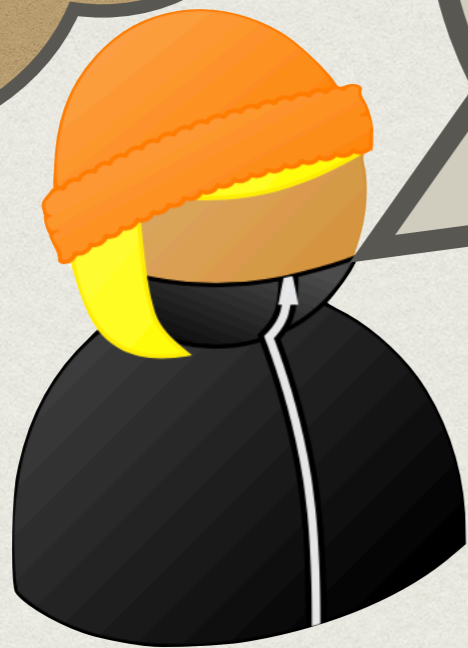
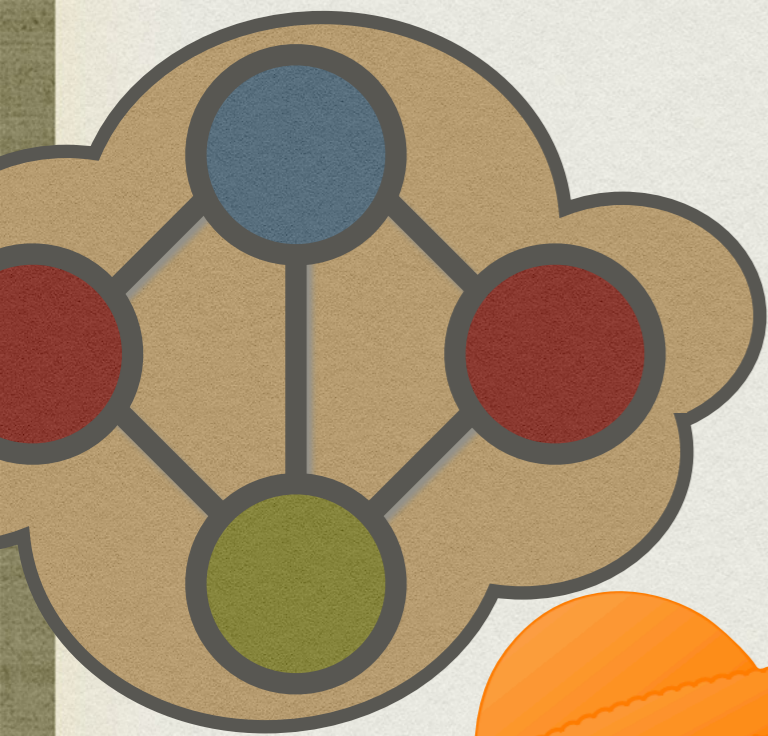
3-COL



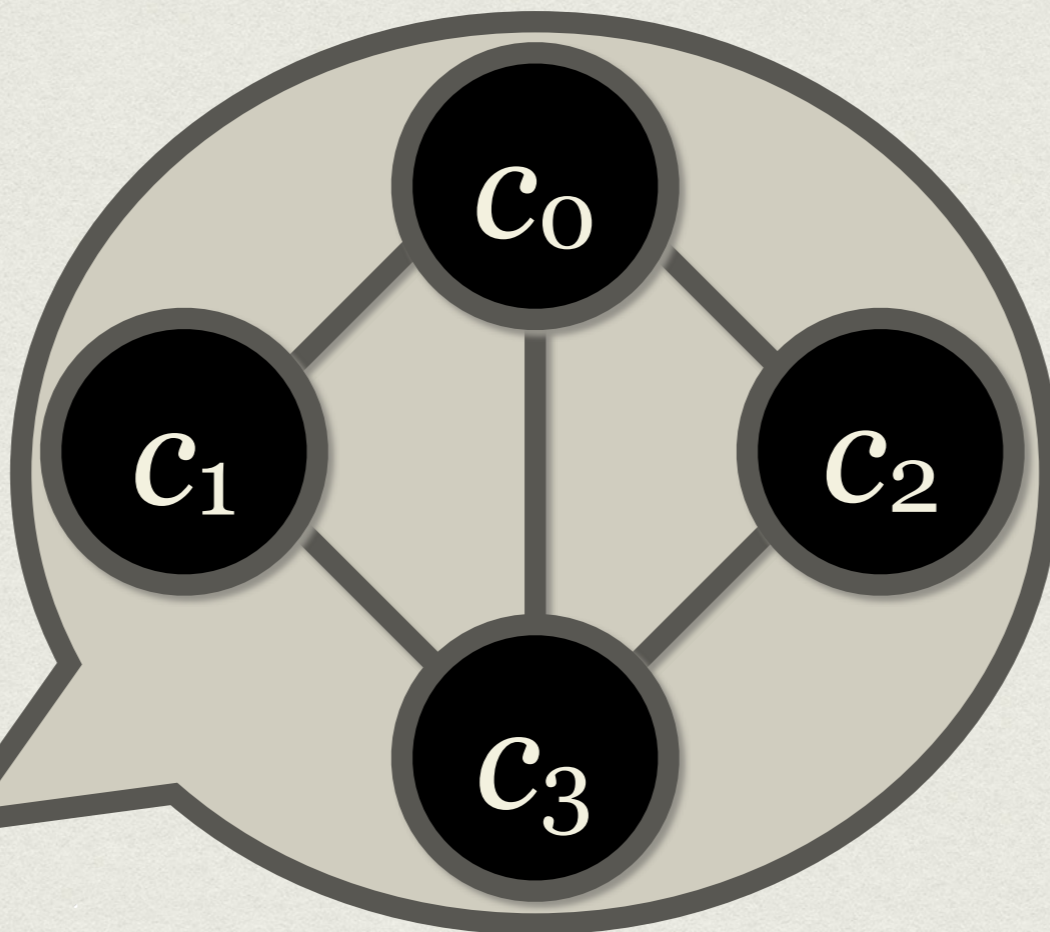
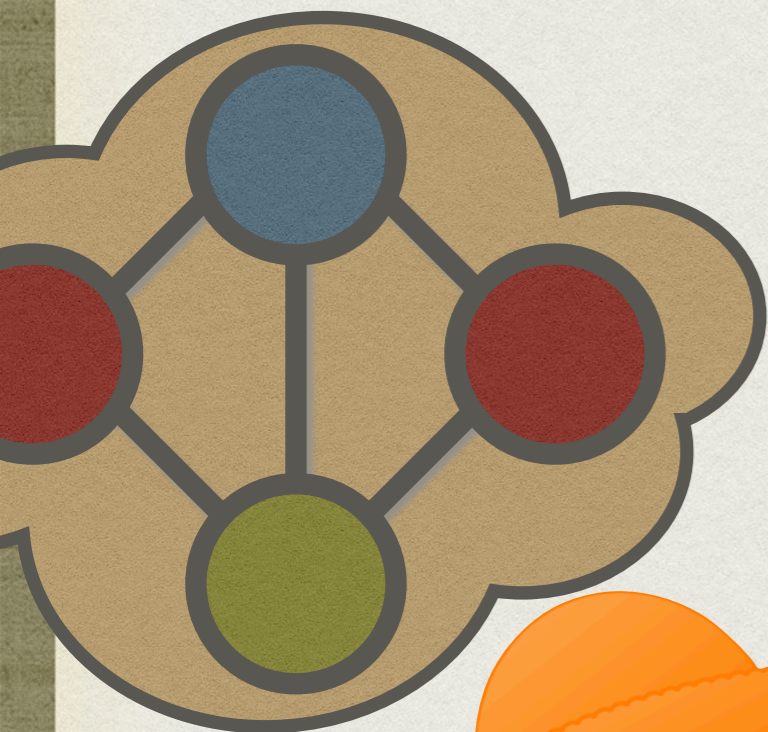
3-COL



# 3-COL



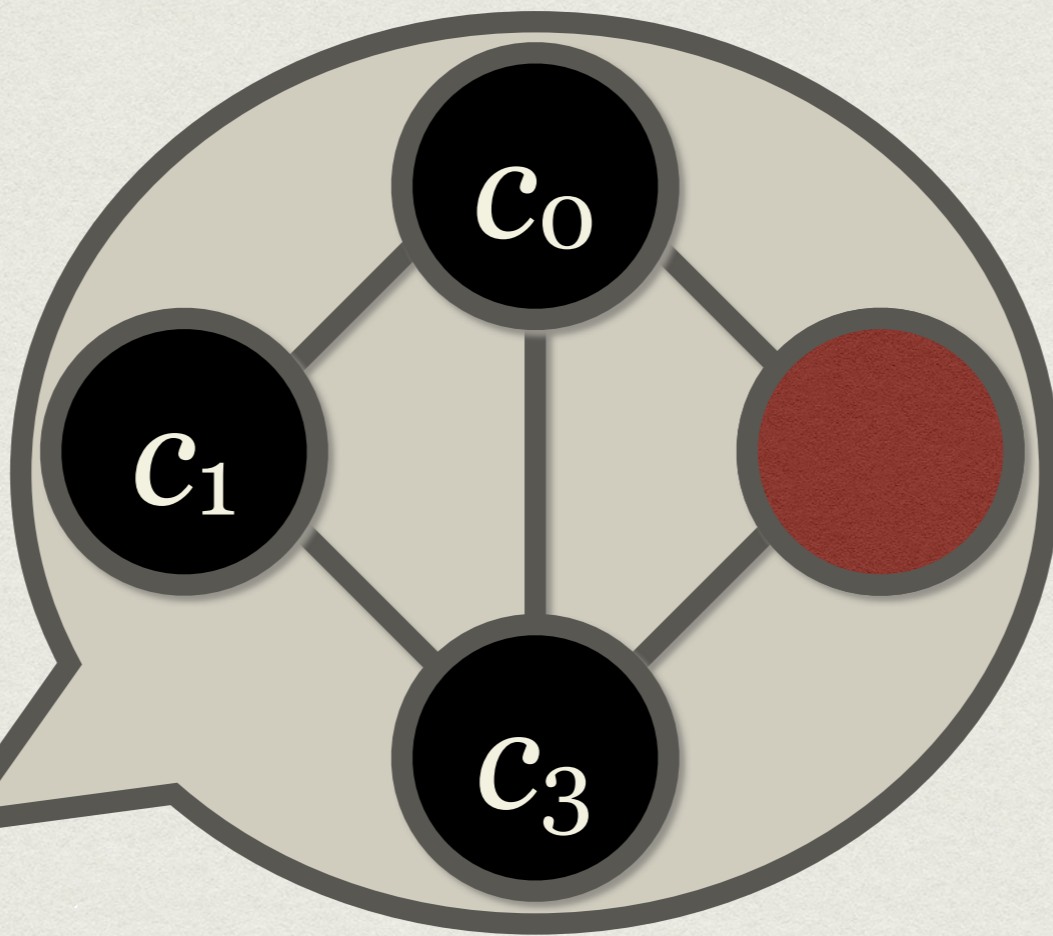
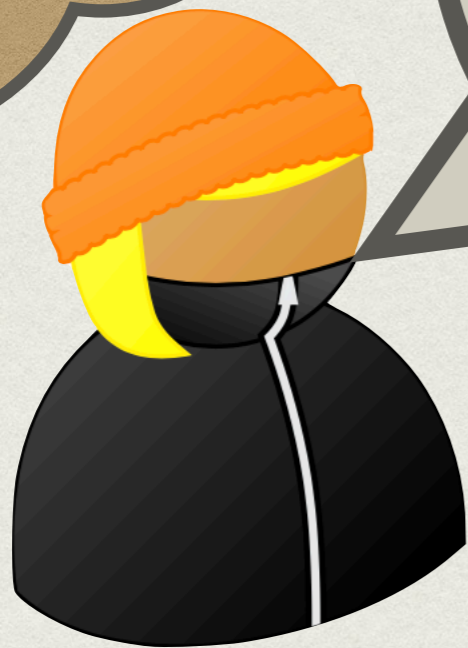
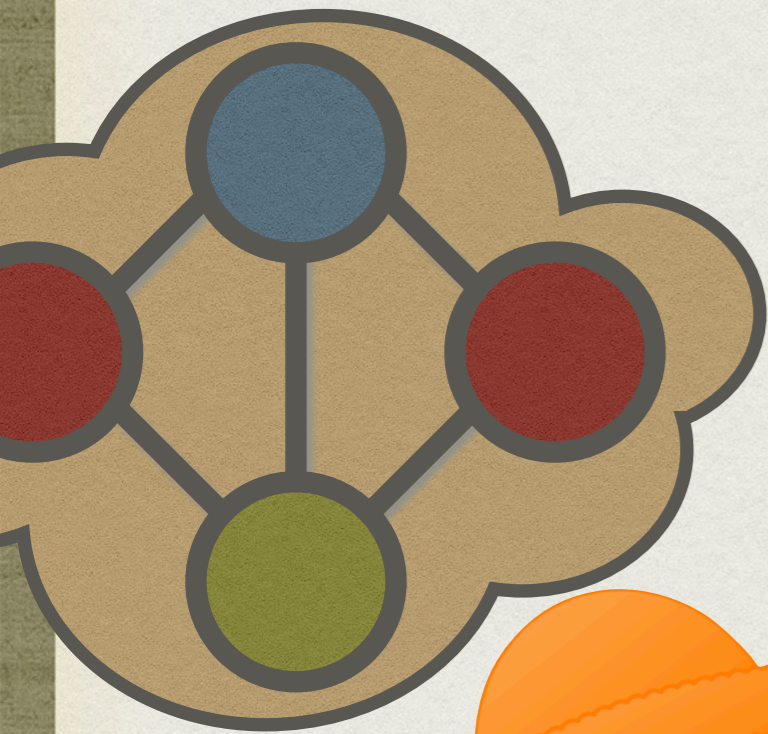
# 3-COL



0-2



# 3-COL

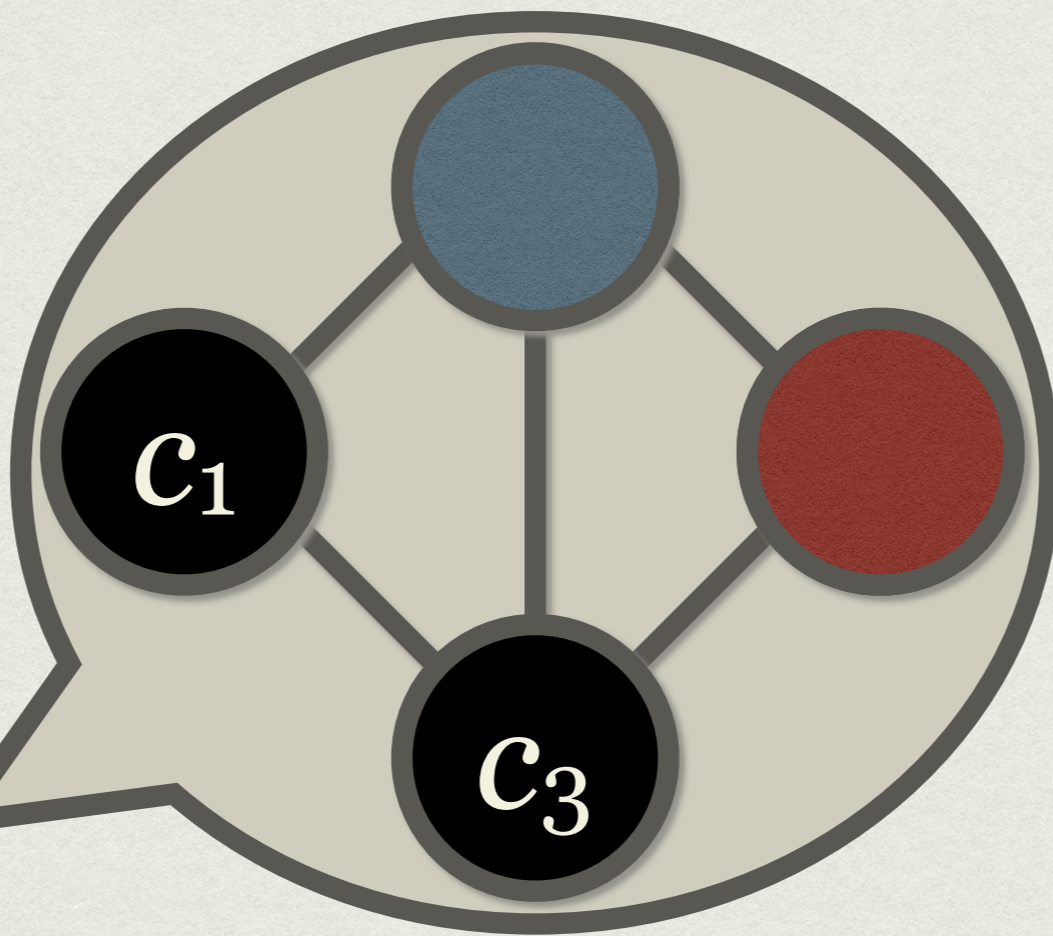
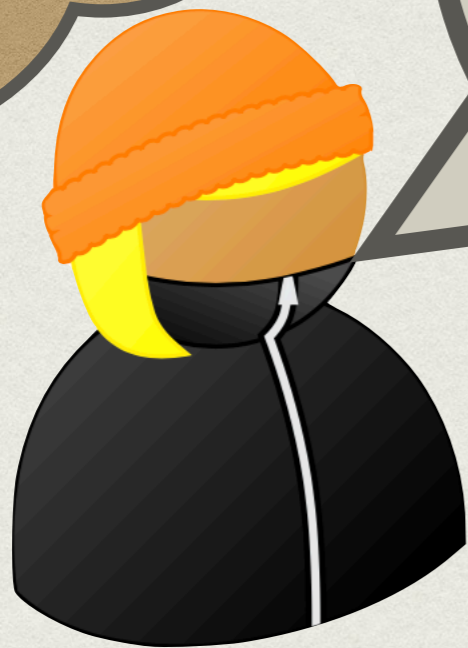
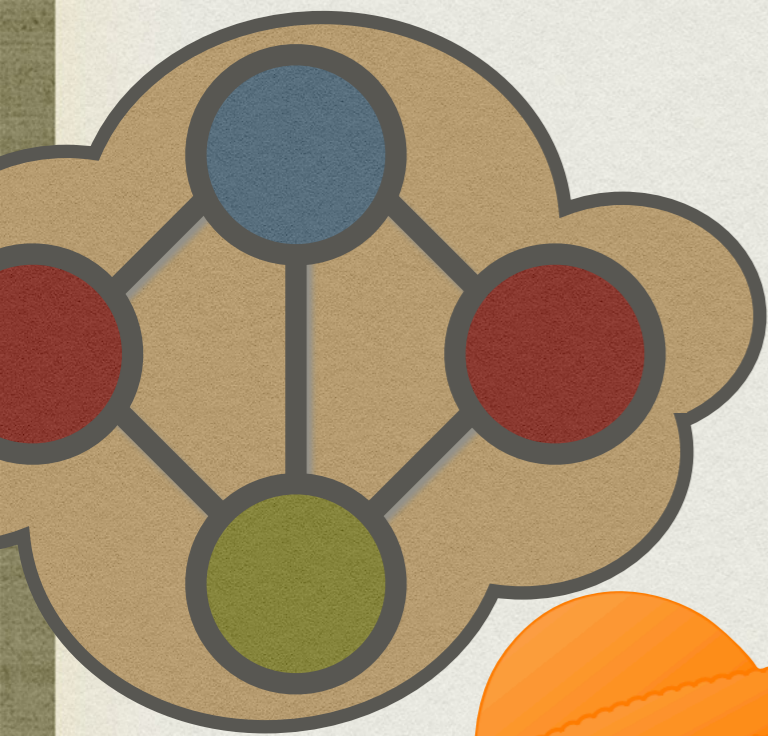


0-2





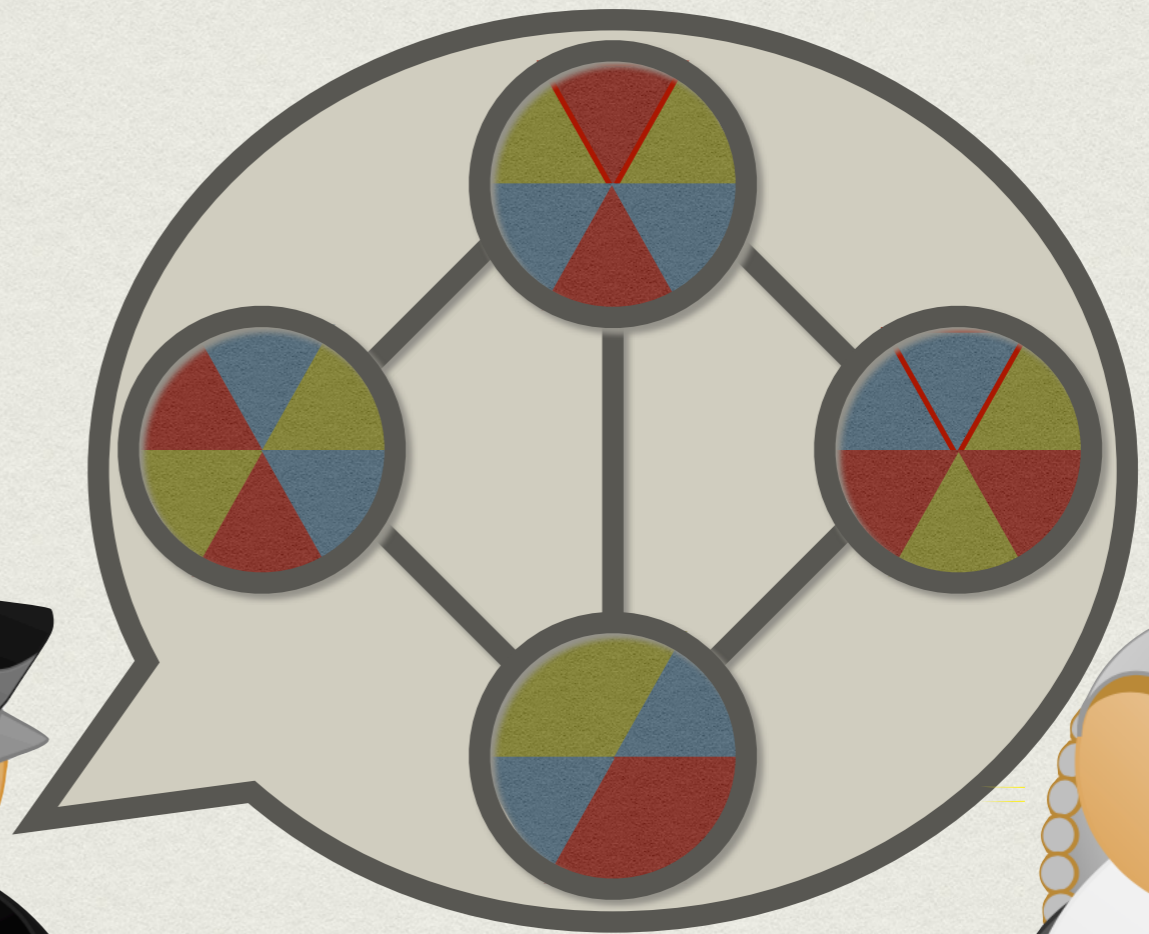
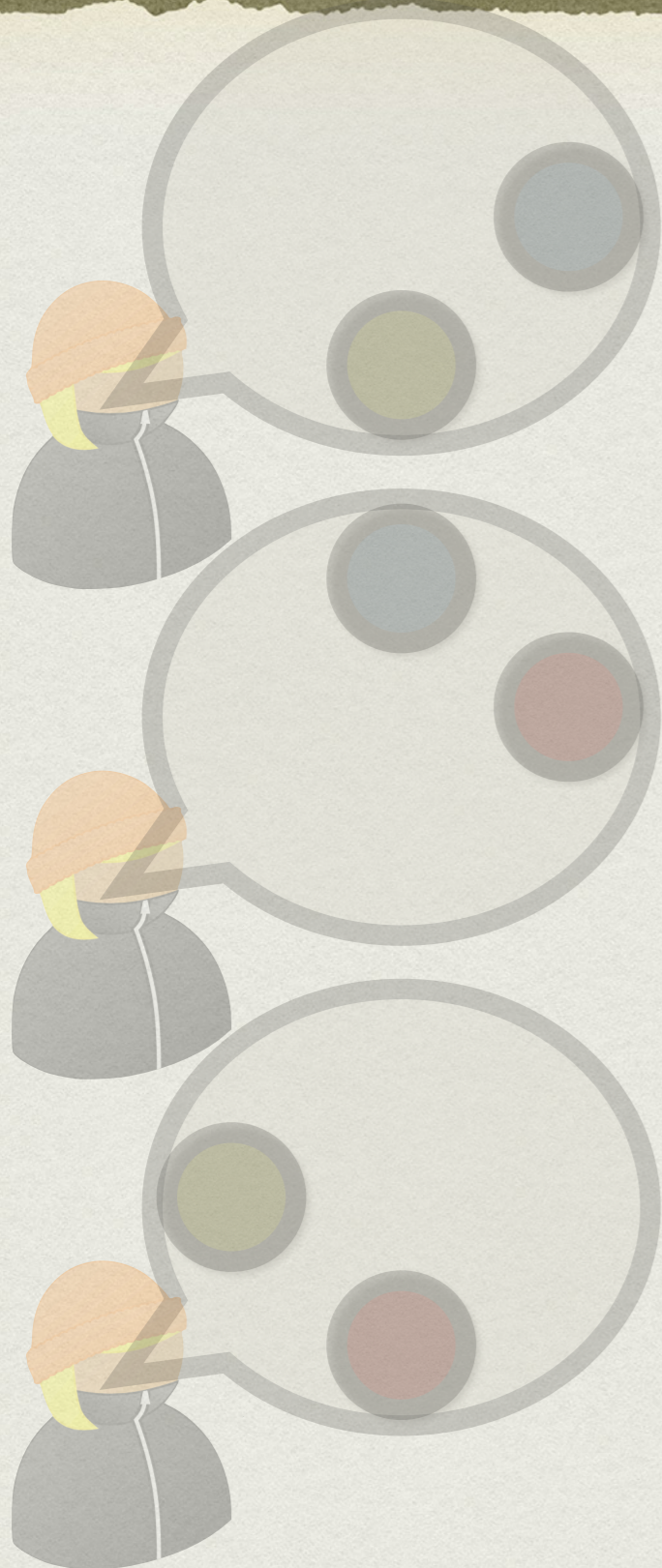
# 3-COL



0-2



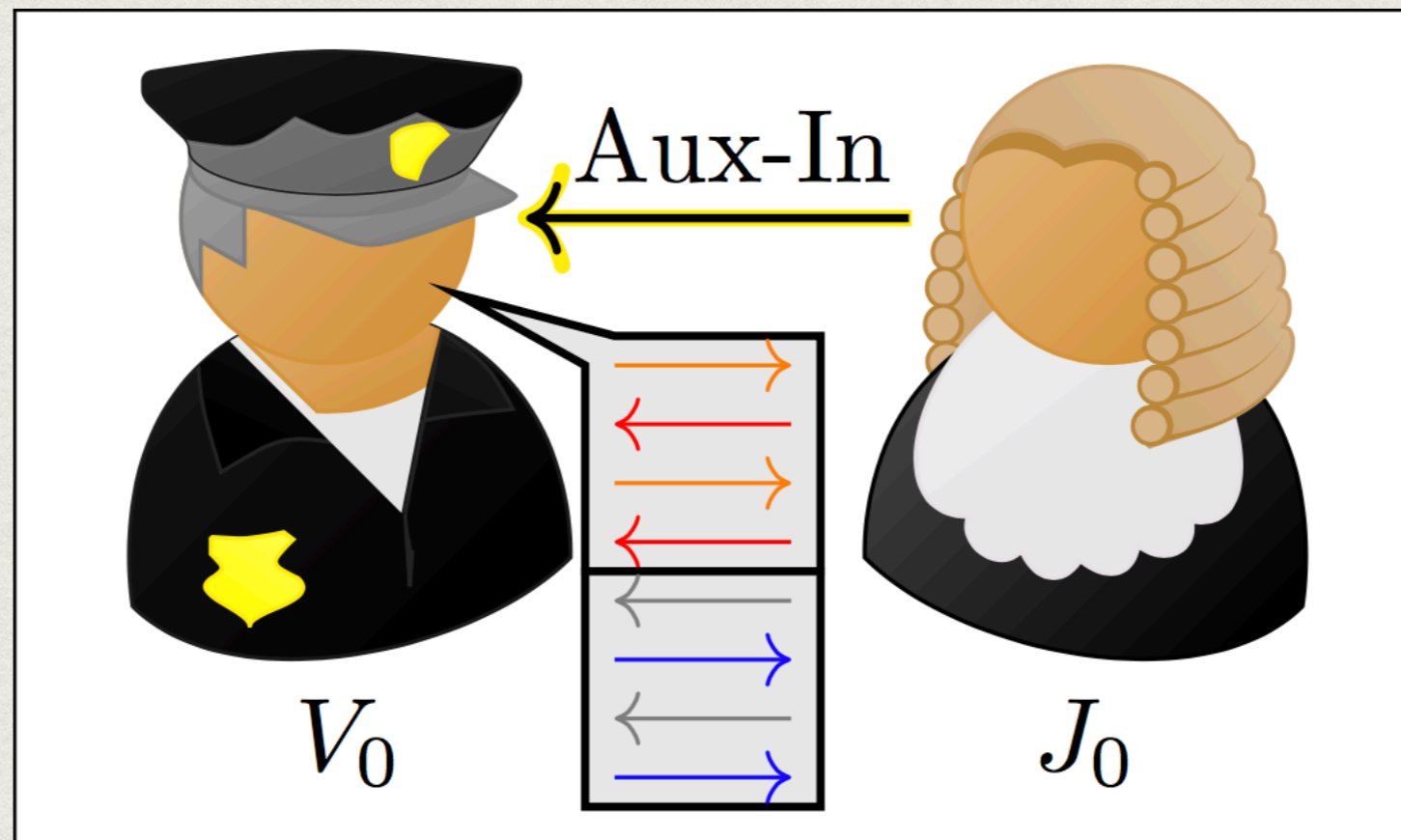
# 3-COL



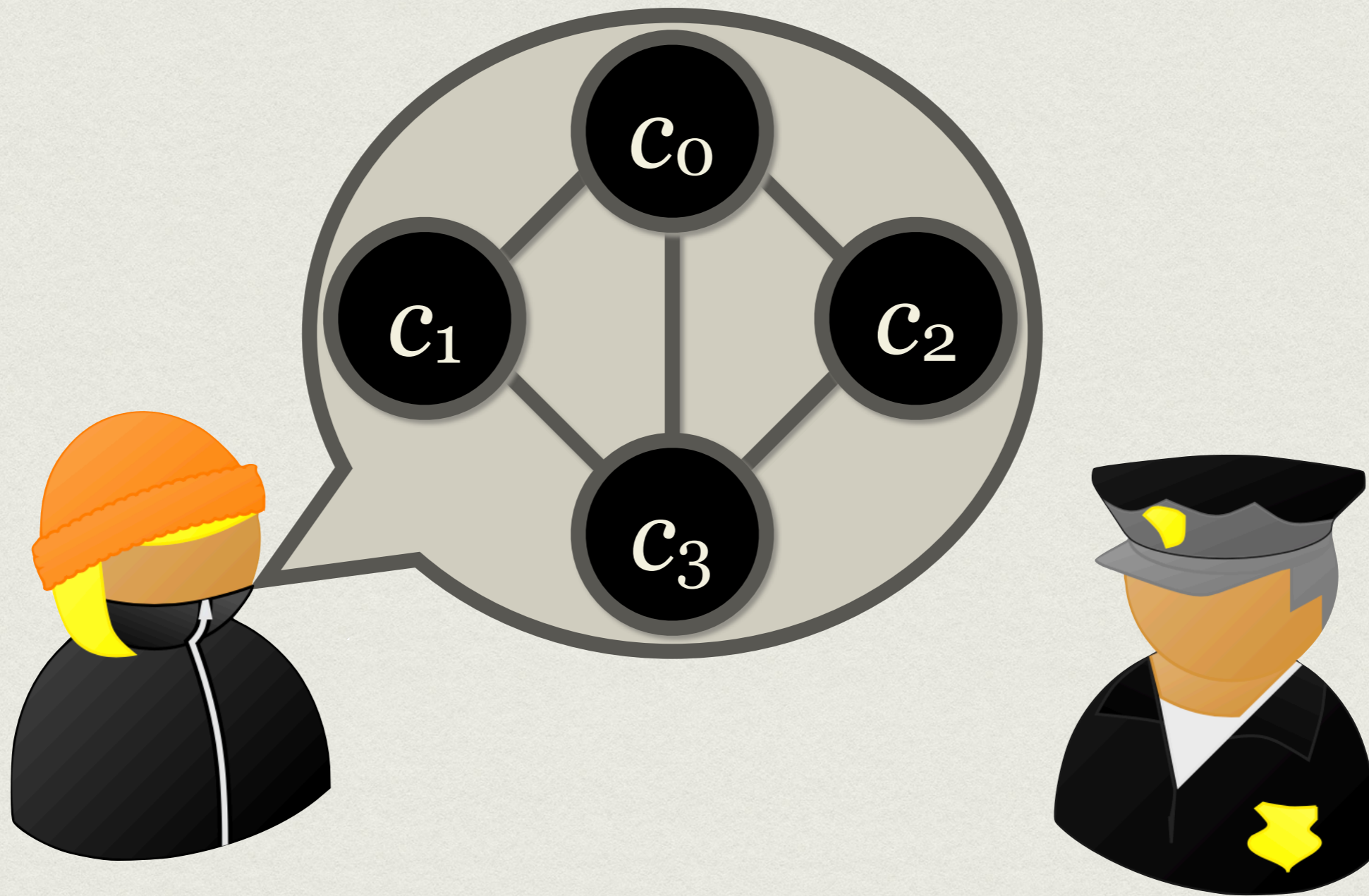
**NON TRANSFÉRABLE !**

# ZERO-KNOWLEDGE

⇒ NON TRANSFÉRABLE

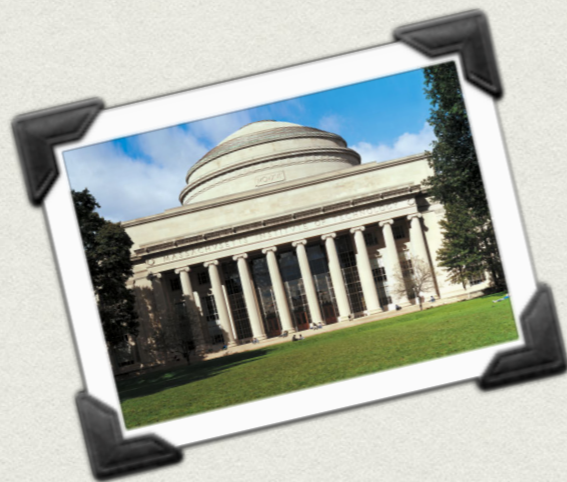


# MISE-EN-GAGE ??



# INTRODUCTION

*(ZK)MIPs*



BGKW88






BGKW88

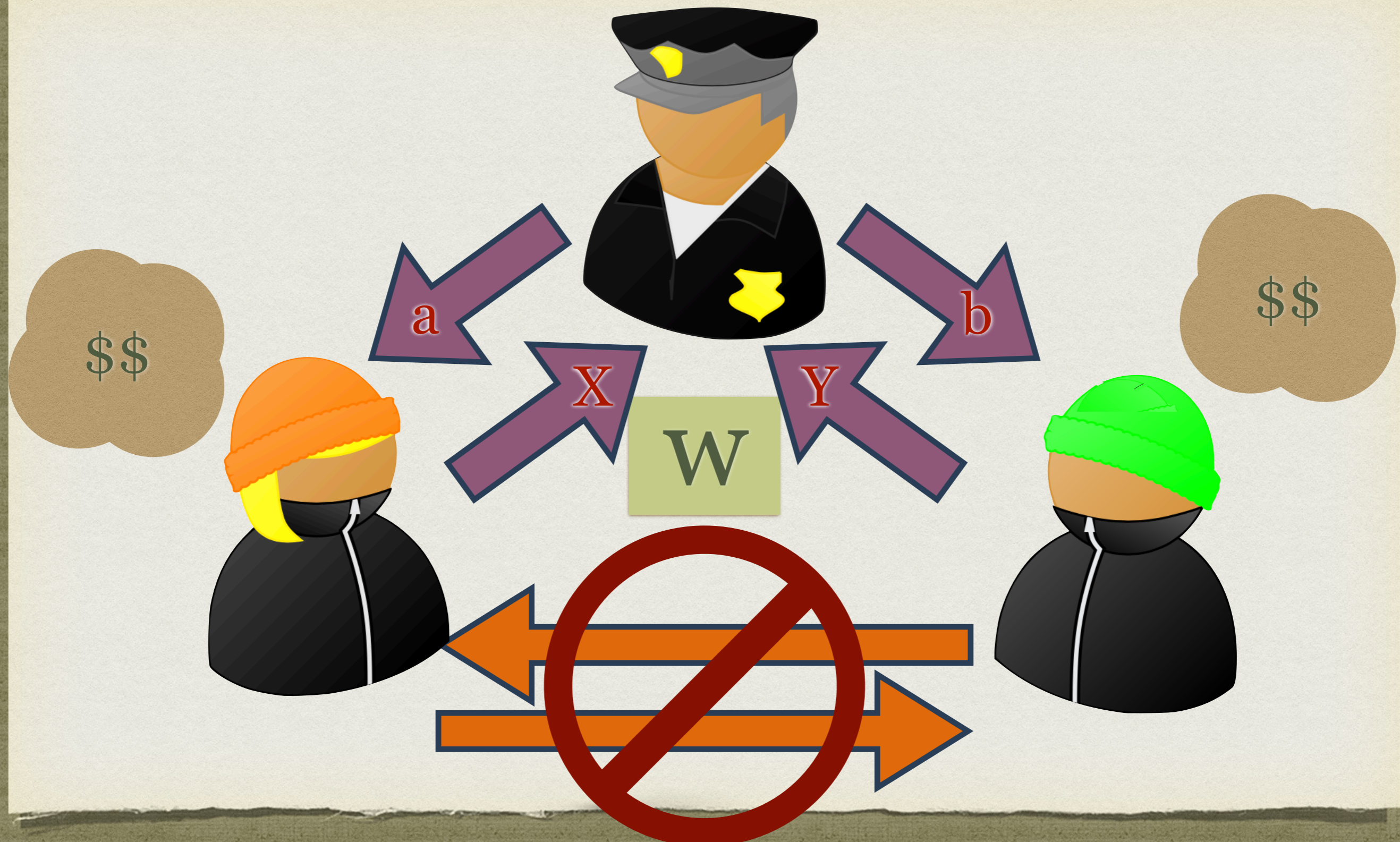
LeMIP







$\exists$  ,  $\exists$  , ,  $\forall w \in L,$




$\text{Prob}[(\text{orange hat} : \text{police} : \text{green hat}) \text{ accepte}] \geq 1 - \epsilon$



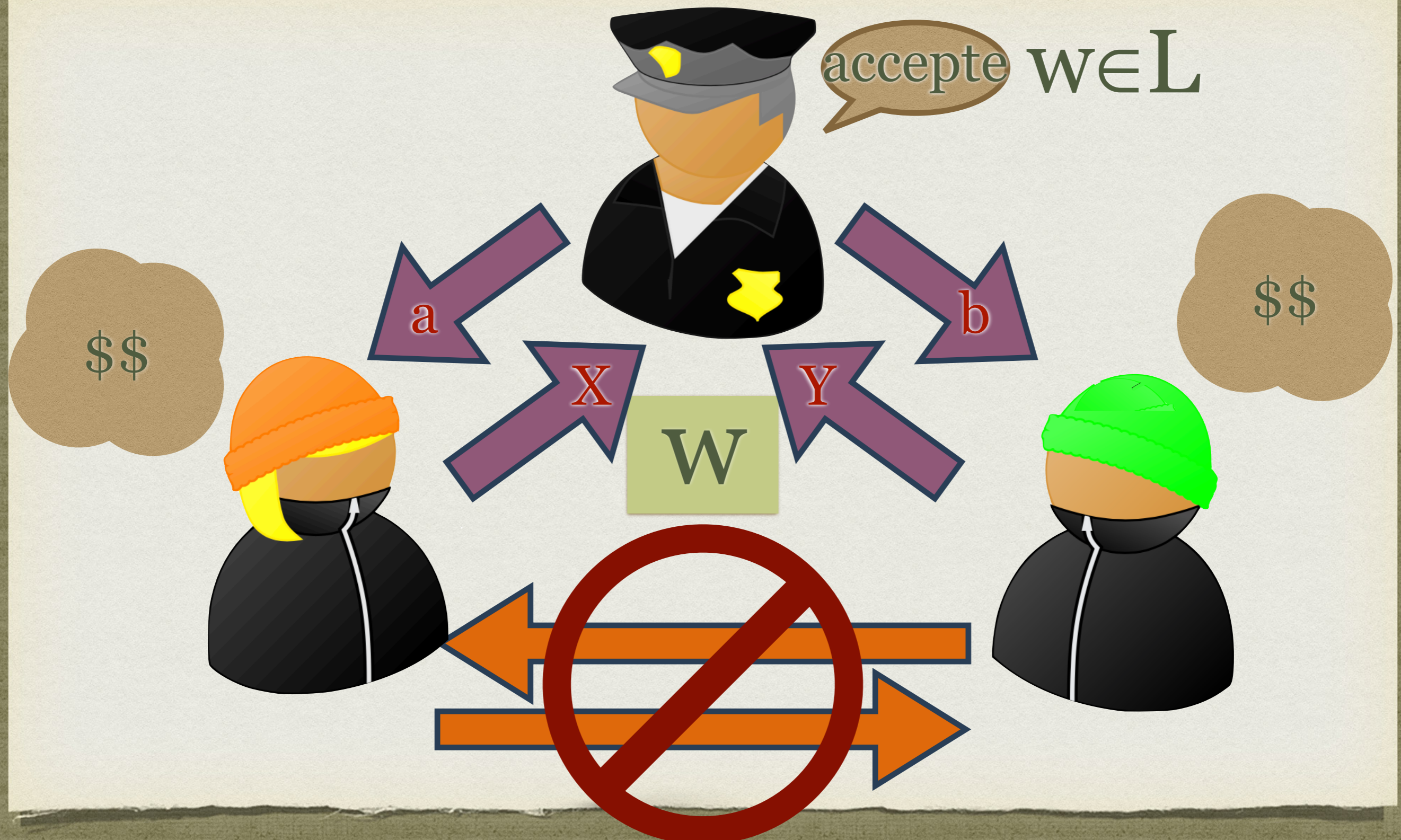
$\exists$  ,  $\exists$  , ,  $\forall w \in L$ ,

$\text{Prob}[(\text{orange hat} : \text{police} : \text{green hat}) \text{ accepte}] \geq 1 - \epsilon$



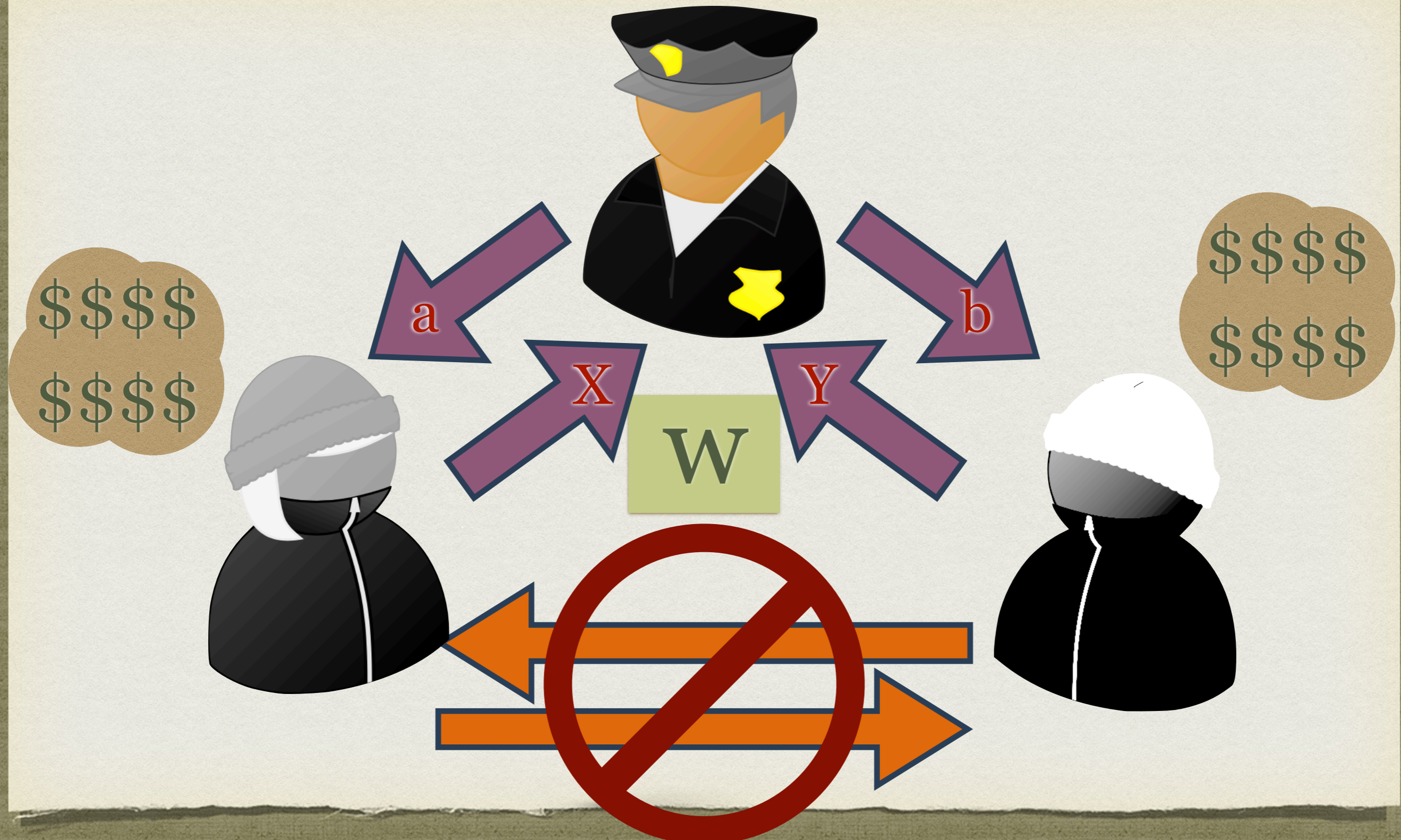
$\exists$  ,  $\exists$  , ,  $\forall w \in L$ ,

$\text{Prob}[(\text{worker with orange hat} : \text{police officer} : \text{worker with green hat}) \text{ accepte } ] \geq 1 - \epsilon$



$\exists$  ,       ,  $\forall w \notin L,$

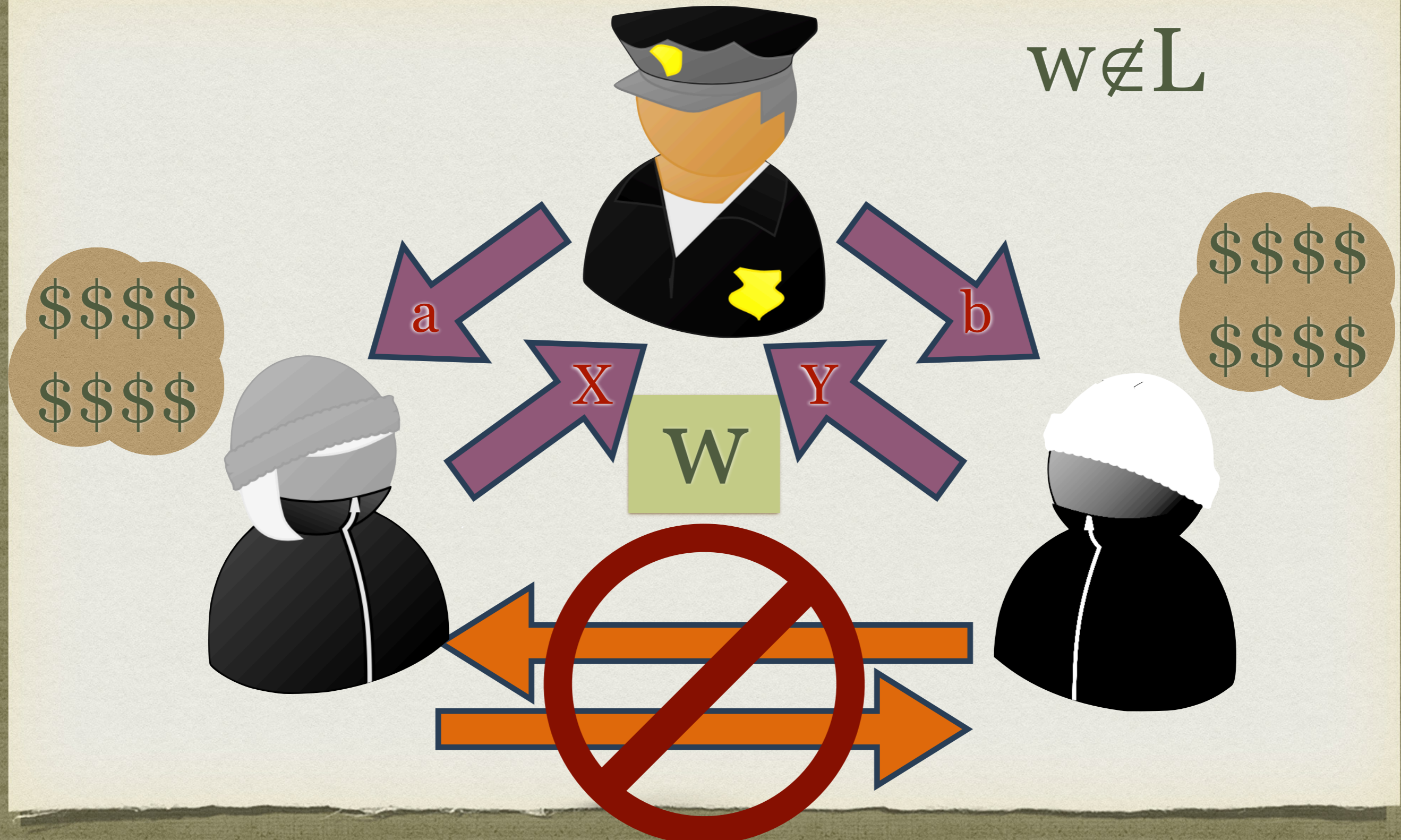
$\text{Prob}[(\text{grey hood} : \text{police} : \text{white hood}) \text{ accepte}] \leq \epsilon$



$\exists$  , et  $\forall$  , ,  $\forall w \notin L$ ,

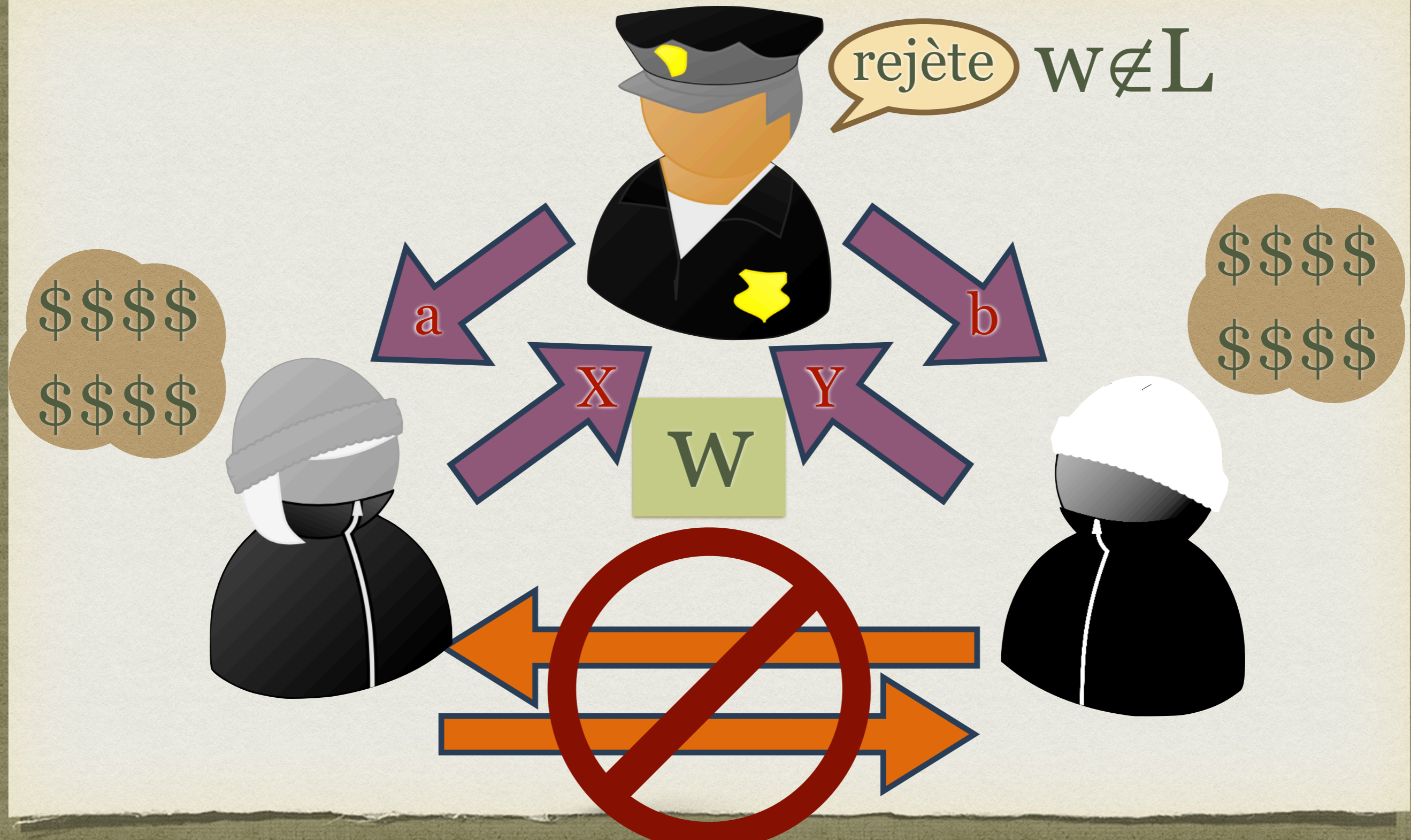
$\text{Prob}[(\text{grey hood} : \text{police} : \text{white hood}) \text{ accepte}] \leq \epsilon$

$w \notin L$



$\exists$  , et  $\forall$  , ,  $\forall w \notin L$ ,

$\text{Prob}[(\text{grey hood} : \text{police} : \text{white hood}) \text{ accepte}] \leq \epsilon$



BOOKWIS8



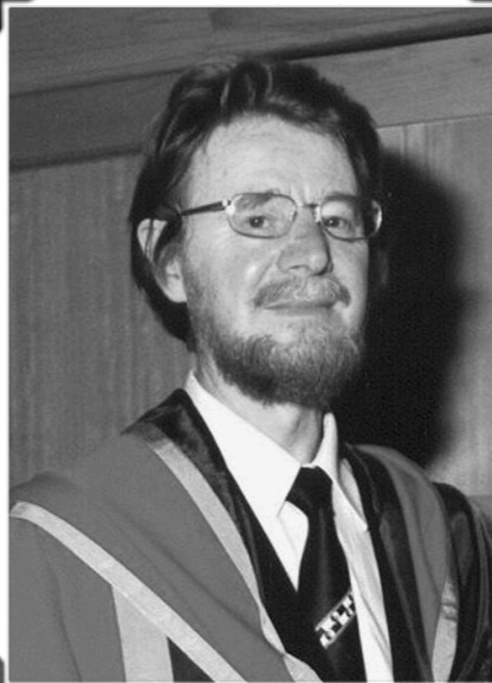
### III.5 ON THE EINSTEIN PODOLSKY ROSEN PARADOX\*

JOHN S. BELL†

#### I. Introduction

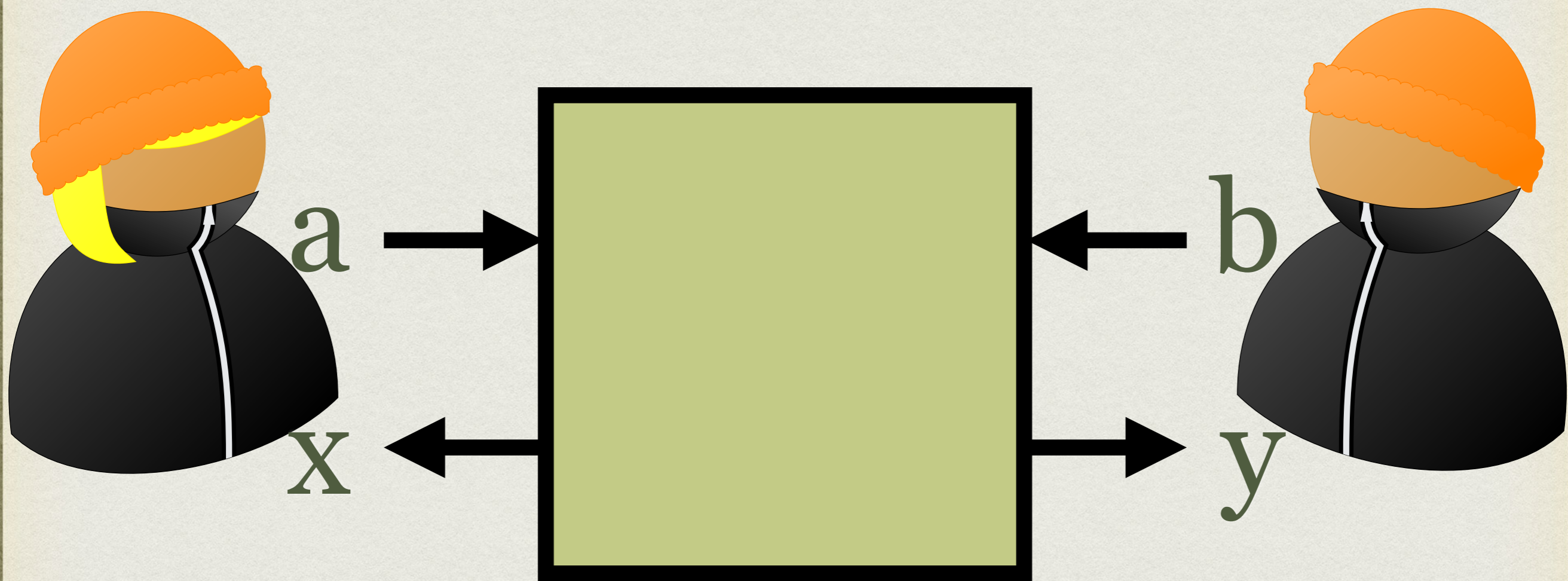
THE paradox of Einstein, Podolsky and Rosen [1] was advanced as an argument that quantum mechanics could not be a complete theory but should be supplemented by additional variables. These additional variables were to restore to the theory causality and locality [2]. In this note that idea will be formulated mathematically and shown to be incompatible with the statistical predictions of quantum mechanics. It is the requirement of locality, or more precisely that the result of a measurement on one system be unaffected by operations on a distant system with which it has interacted in the past, that creates the essential difficulty. There have been attempts [3] to show that even without such a separability or locality requirement no "hidden variable" interpretation of quantum mechanics has been examined elsewhere [4] and found wanting. A local hidden variable interpretation of quantum theory [5] has been explicitly constructed which has a local structure. This is characteristic, and reproduces exactly the quantum mechanical

These attempts have been an interpretation of elementary quantum mechanics has indeed a grossly non-local character, of any such theory which

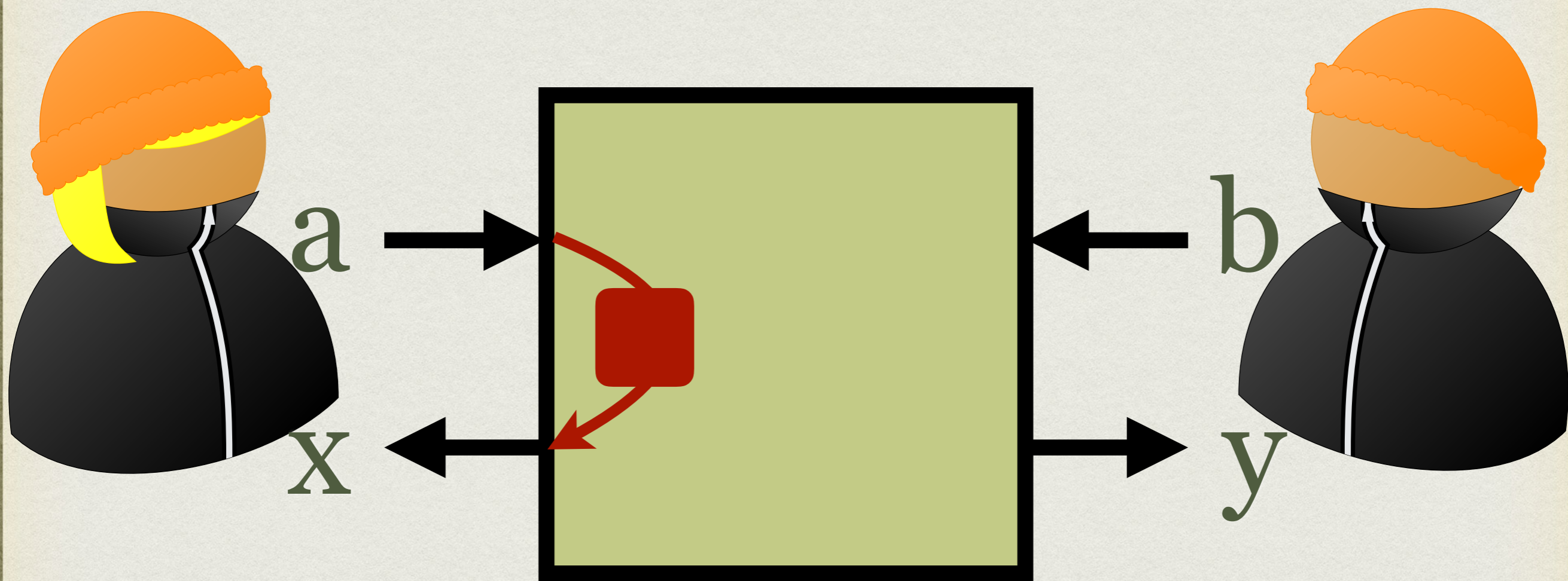




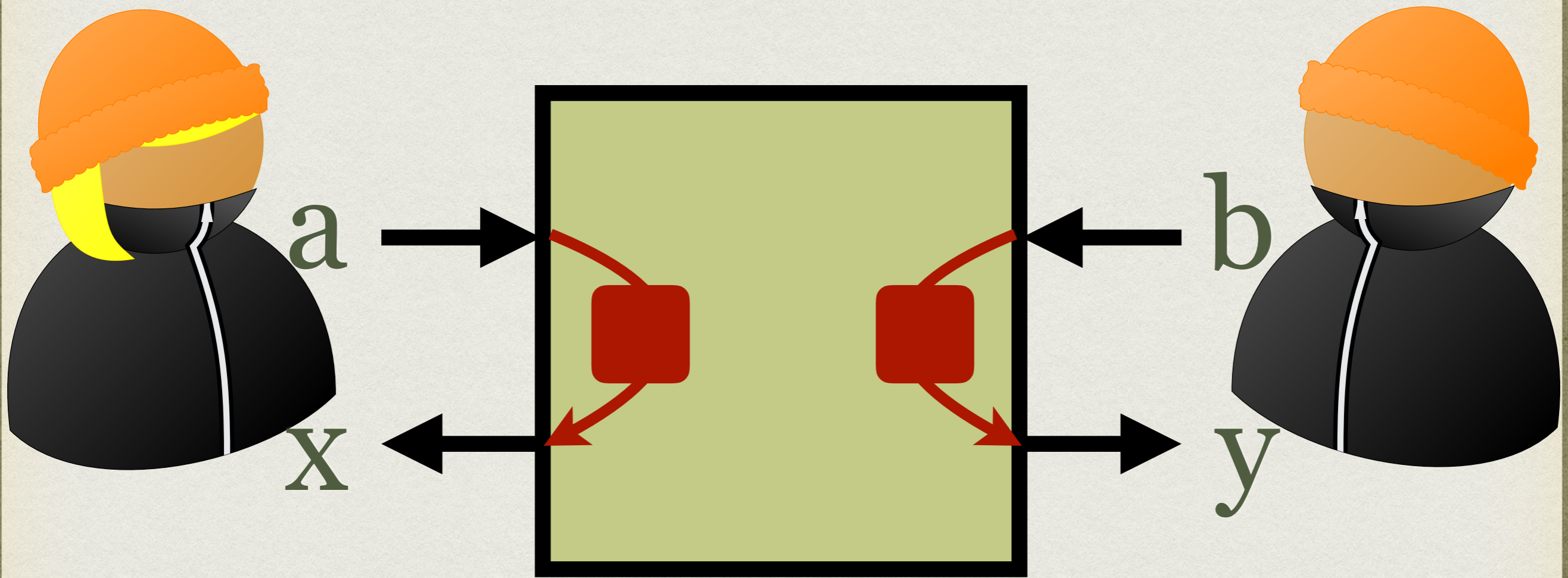
# LOCALITÉ



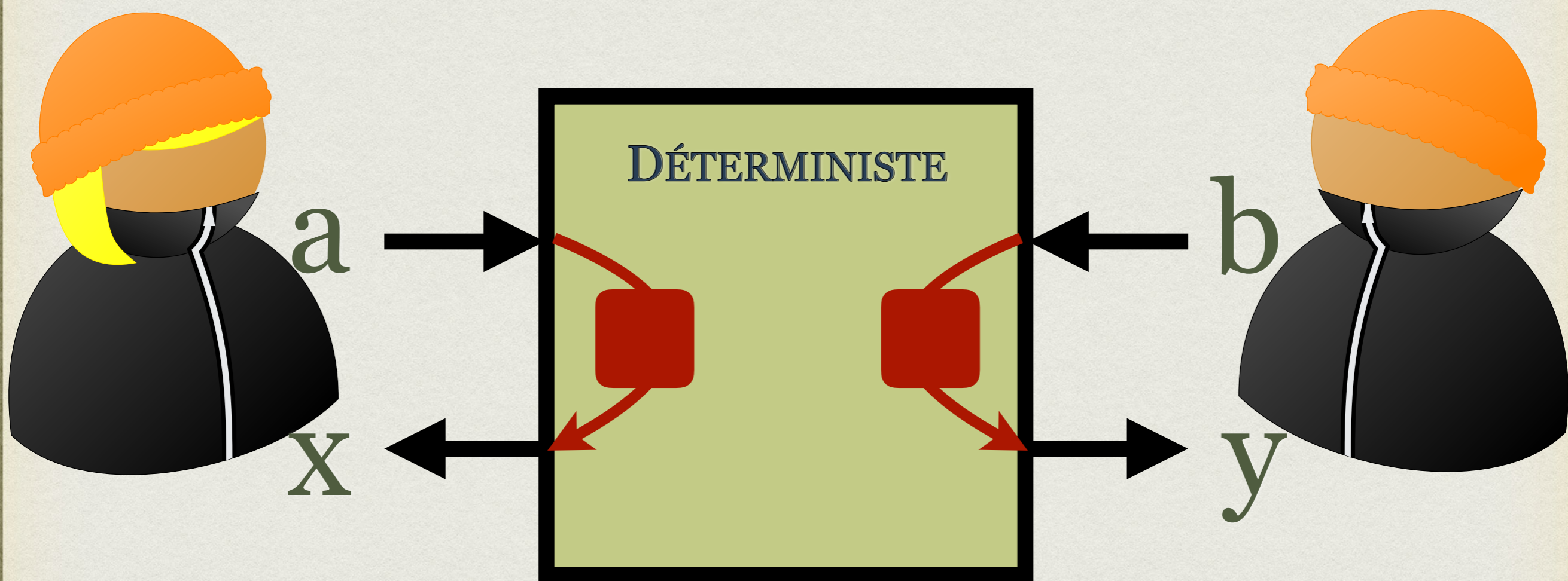
# LOCALITÉ



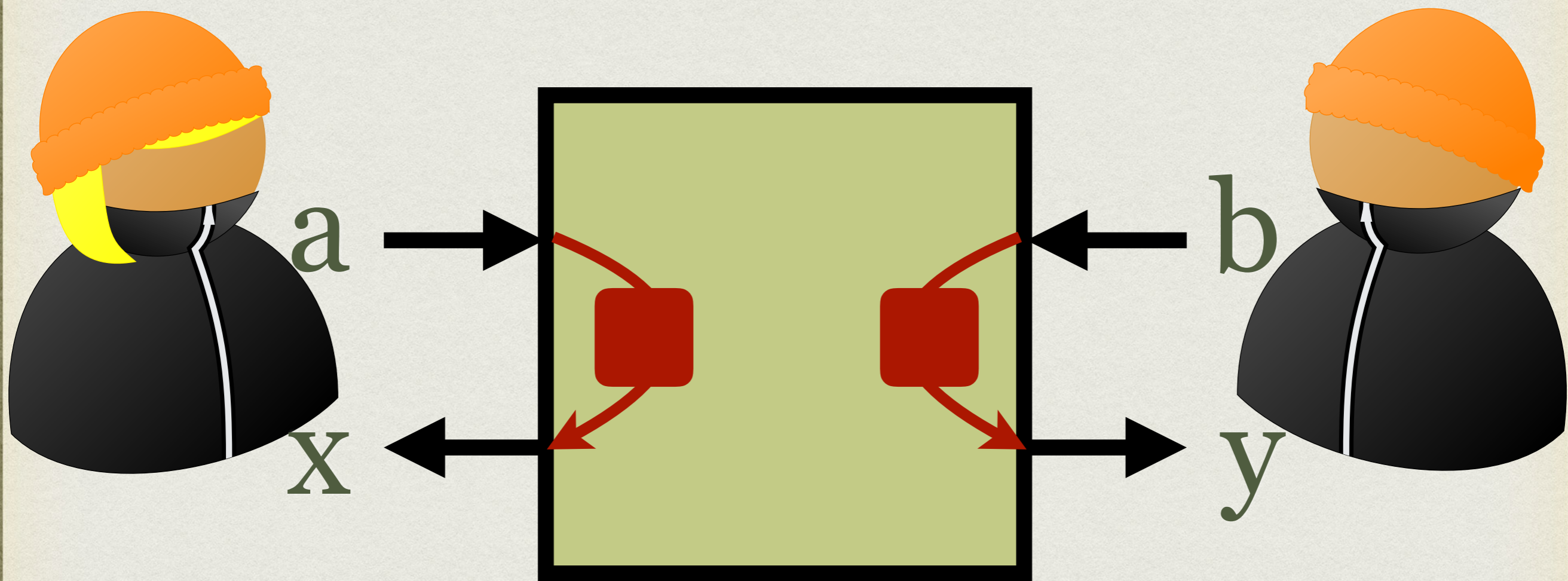
# LOCALITÉ



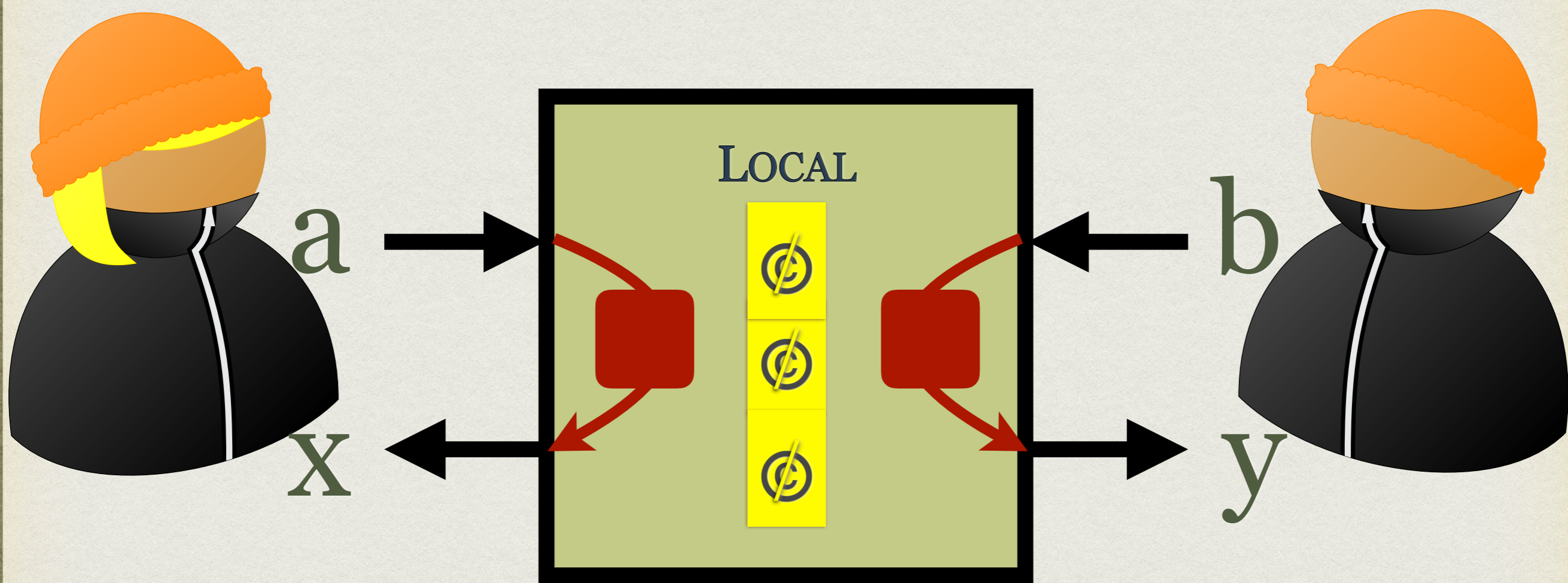
# LOCALITÉ



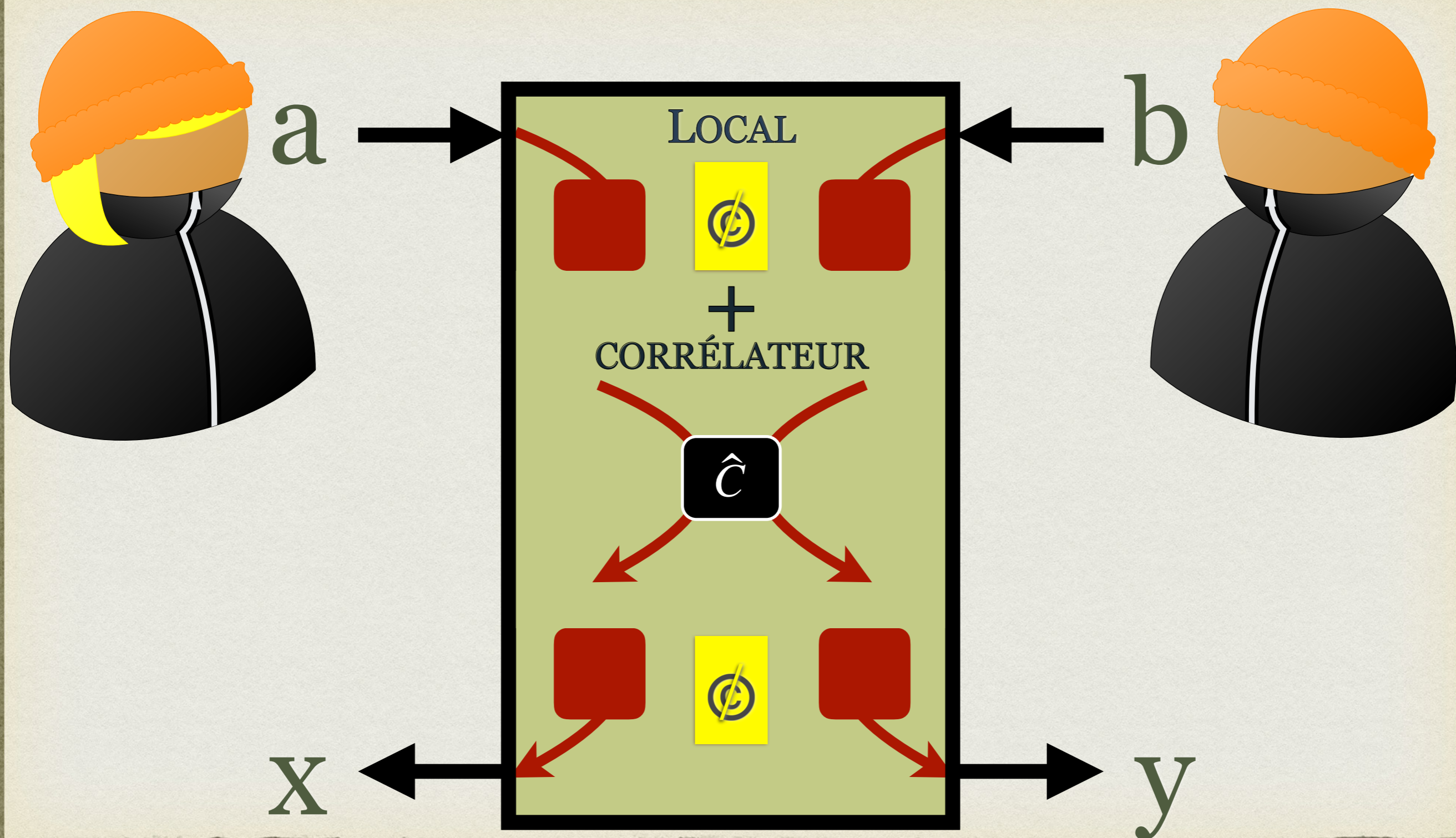
# LOCALITÉ



# LOCALITÉ



# HIERARCHIE DE NON-LOCALITÉ

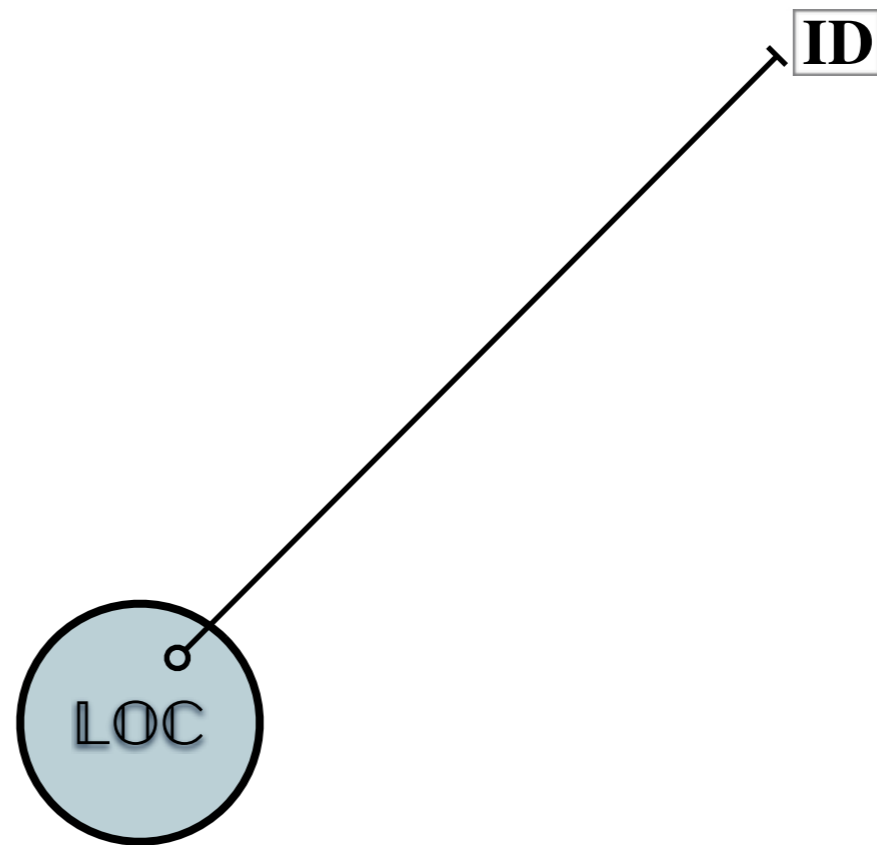


# HIERARCHIE DE NON-LOCALITÉ





# HIERARCHIE DE NON-LOCALITÉ



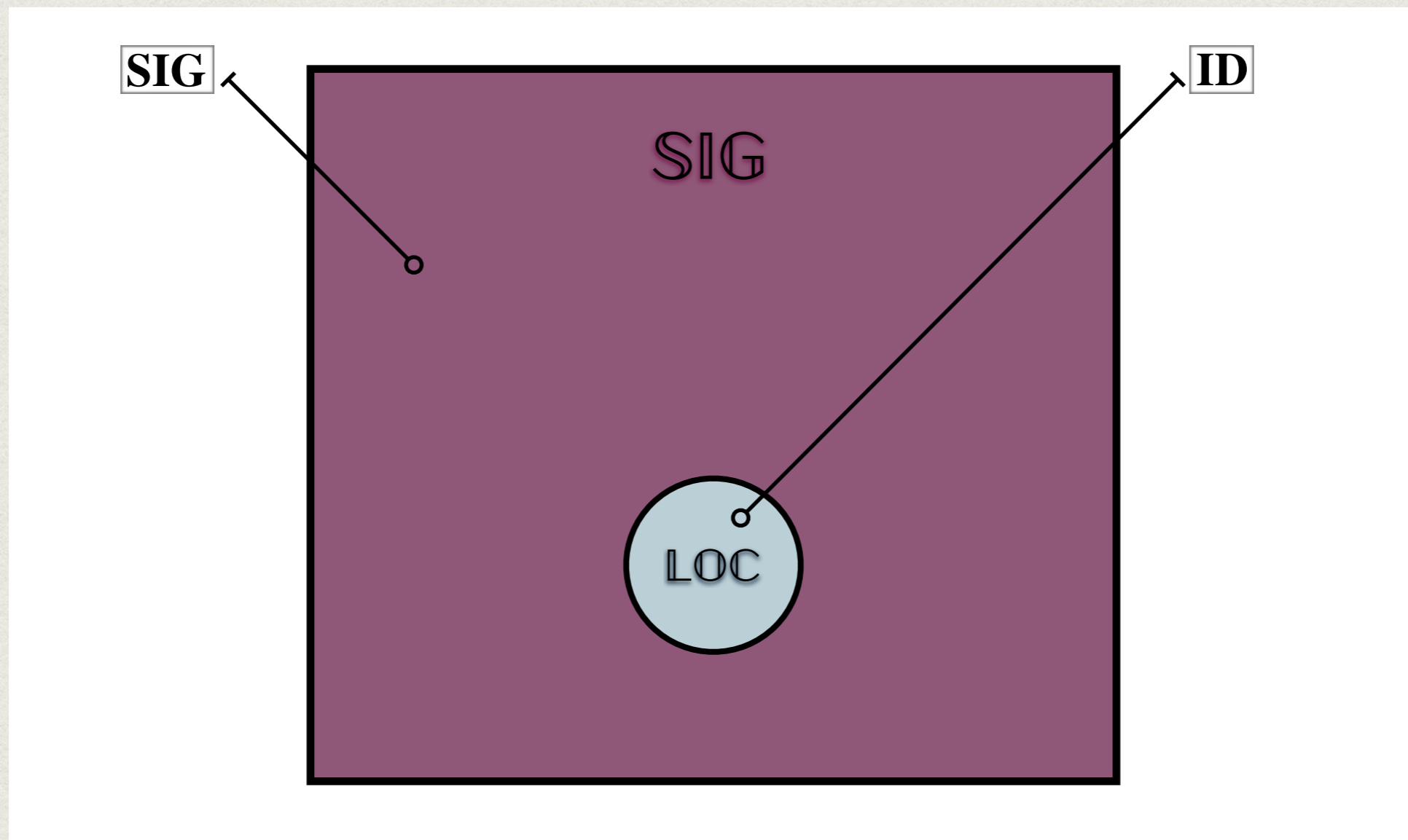
# HIERARCHIE DE NON-LOCALITÉ



# HIERARCHIE DE NON-LOCALITÉ



# HIERARCHIE DE NON-LOCALITÉ



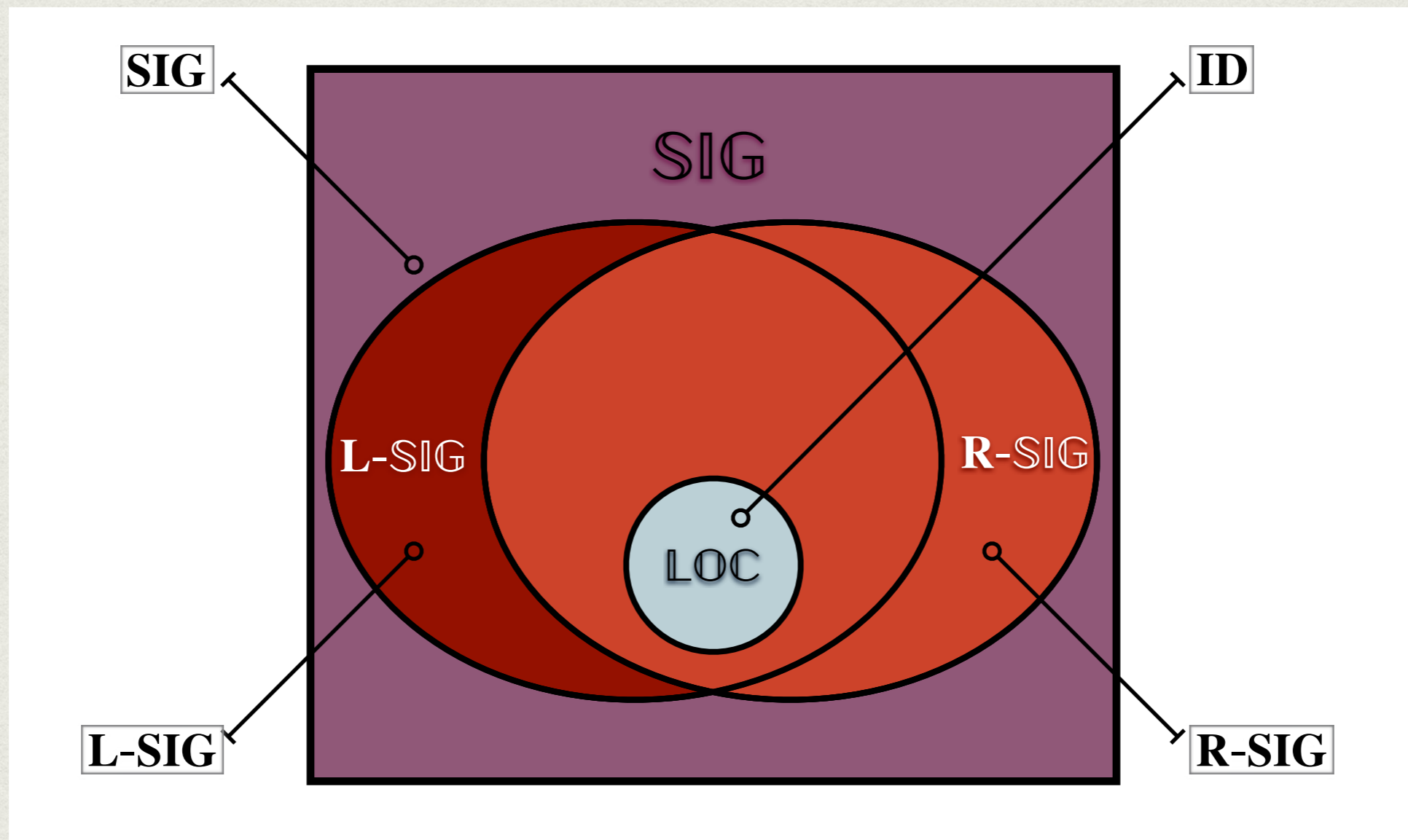
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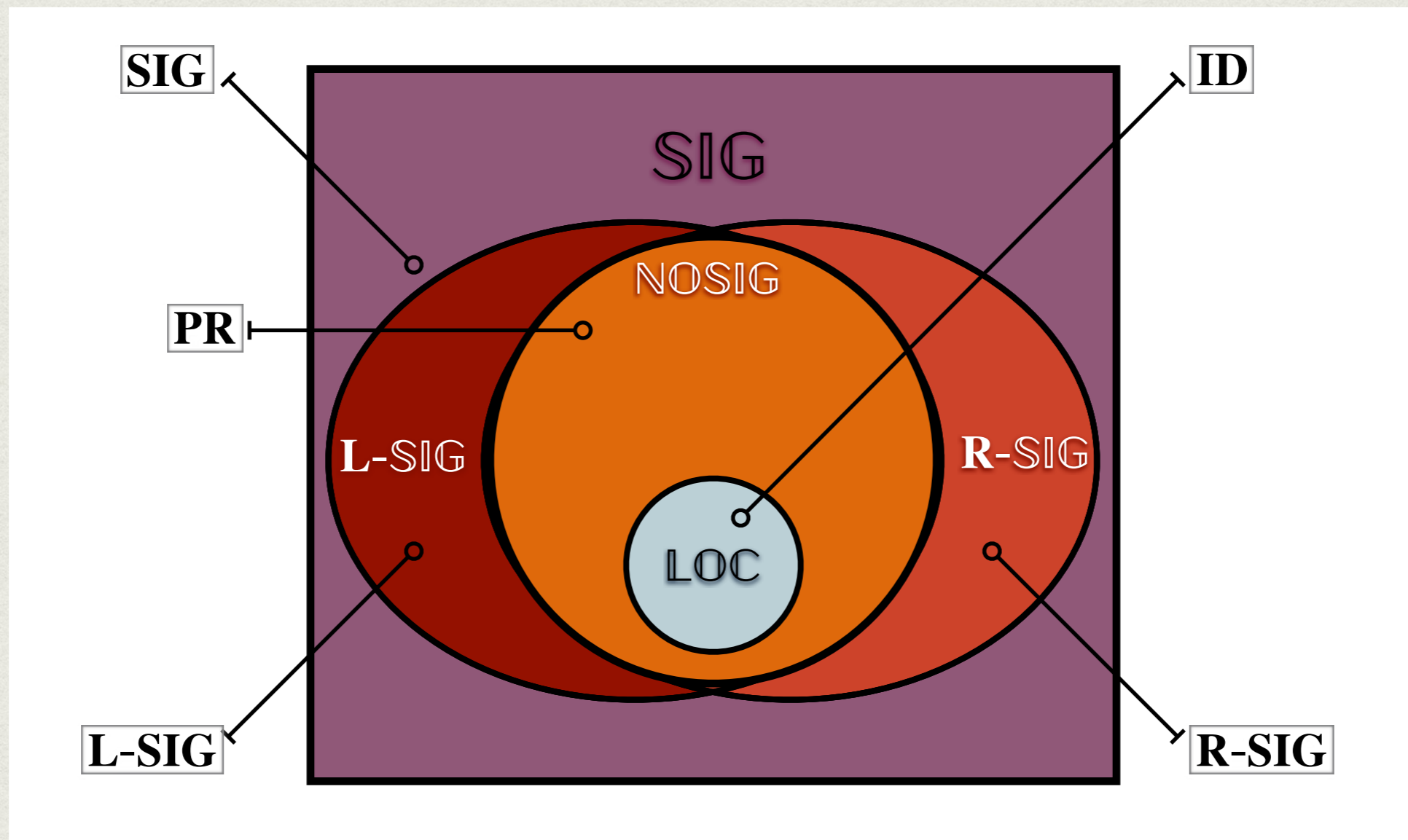
# HIERARCHIE DE NON-LOCALITÉ



# HIERARCHIE DE NON-LOCALITÉ



# HIERARCHIE DE NON-LOCALITÉ





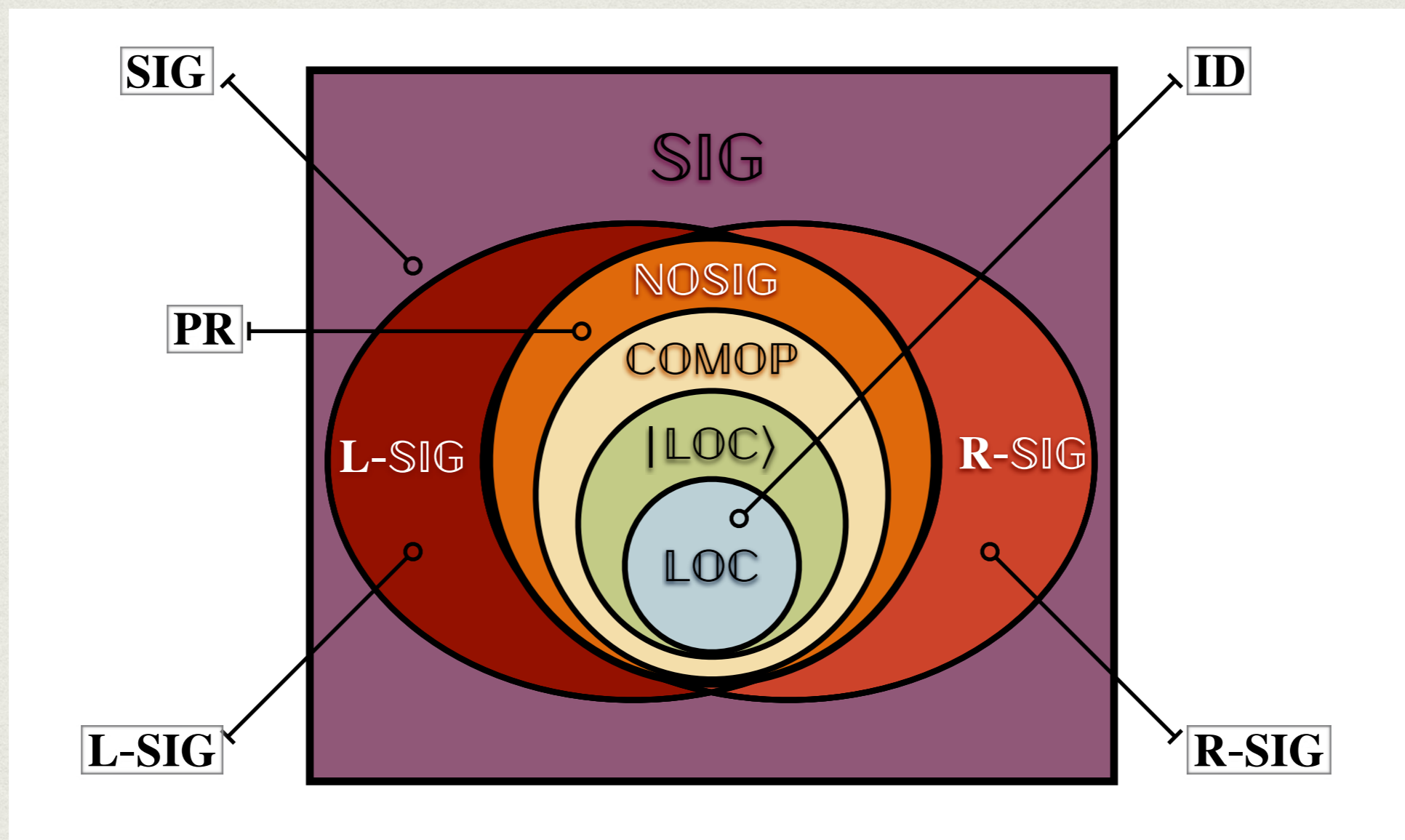
# HIERARCHIE DE NON-LOCALITÉ



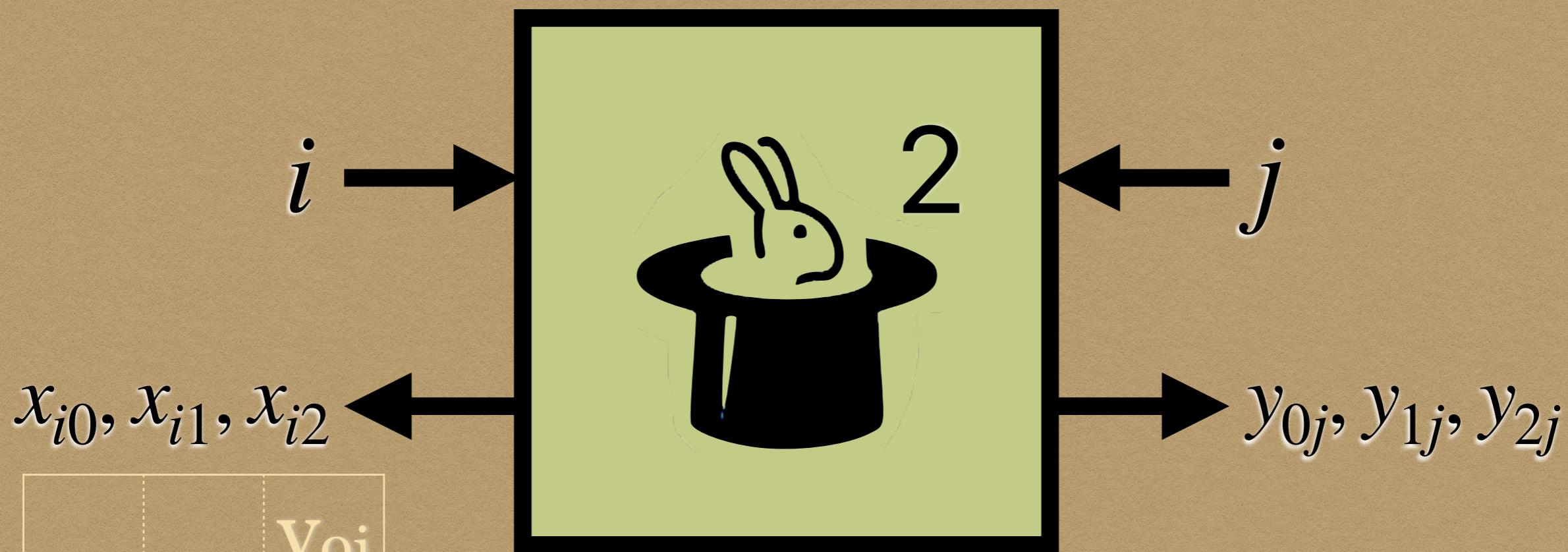
$$x \oplus y = a \cdot b$$

$x$  est uniforme

# HIERARCHIE DE NON-LOCALITÉ



# HIERARCHIE DE NON-LOCALITÉ



		$y_{0j}$
$x_{i0}$	$x_{i1}$	$x_{i2} = y_{2j}$
		$y_{2j}$

→ paire

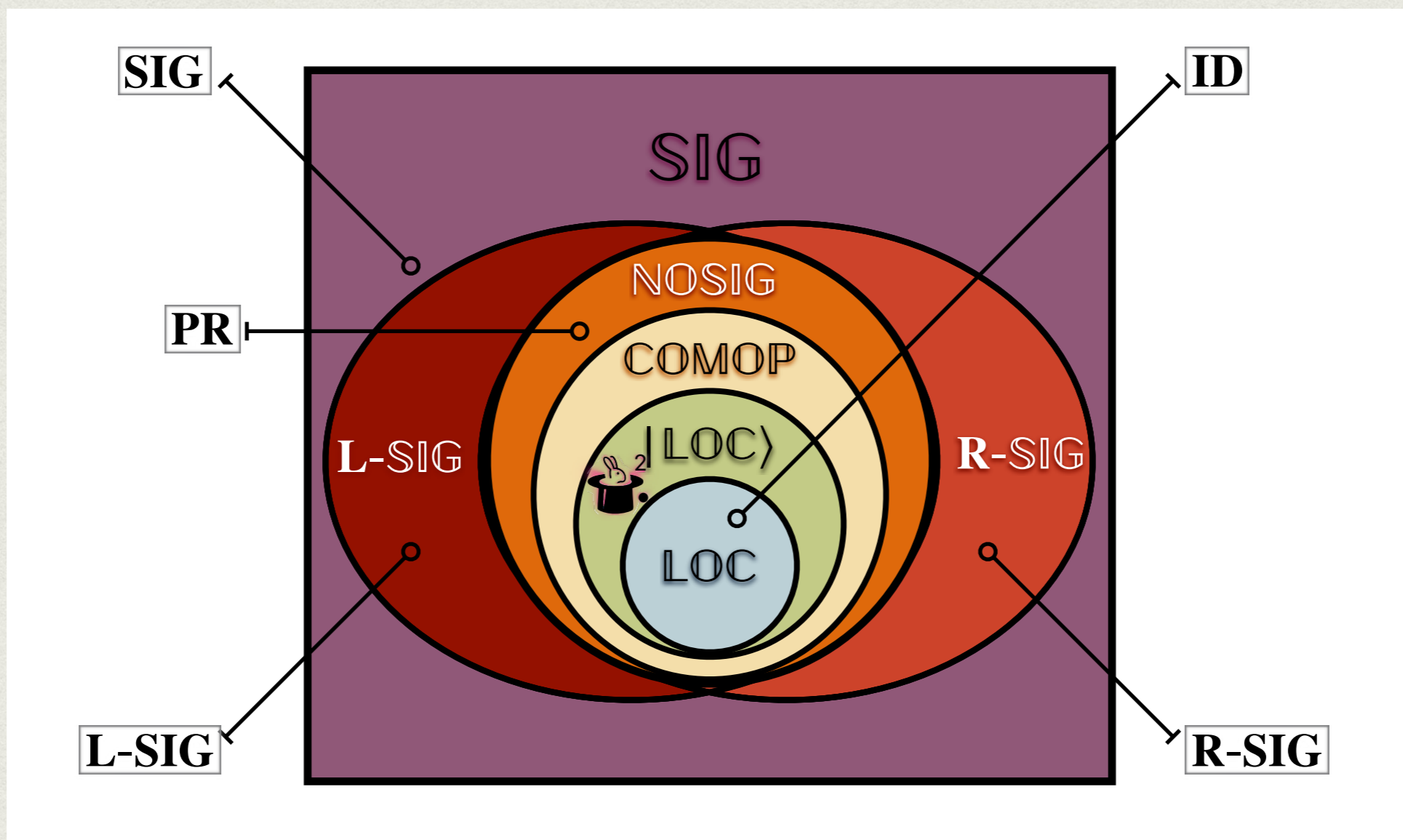
→ impaire

$$x_{ij} = y_{ij}$$

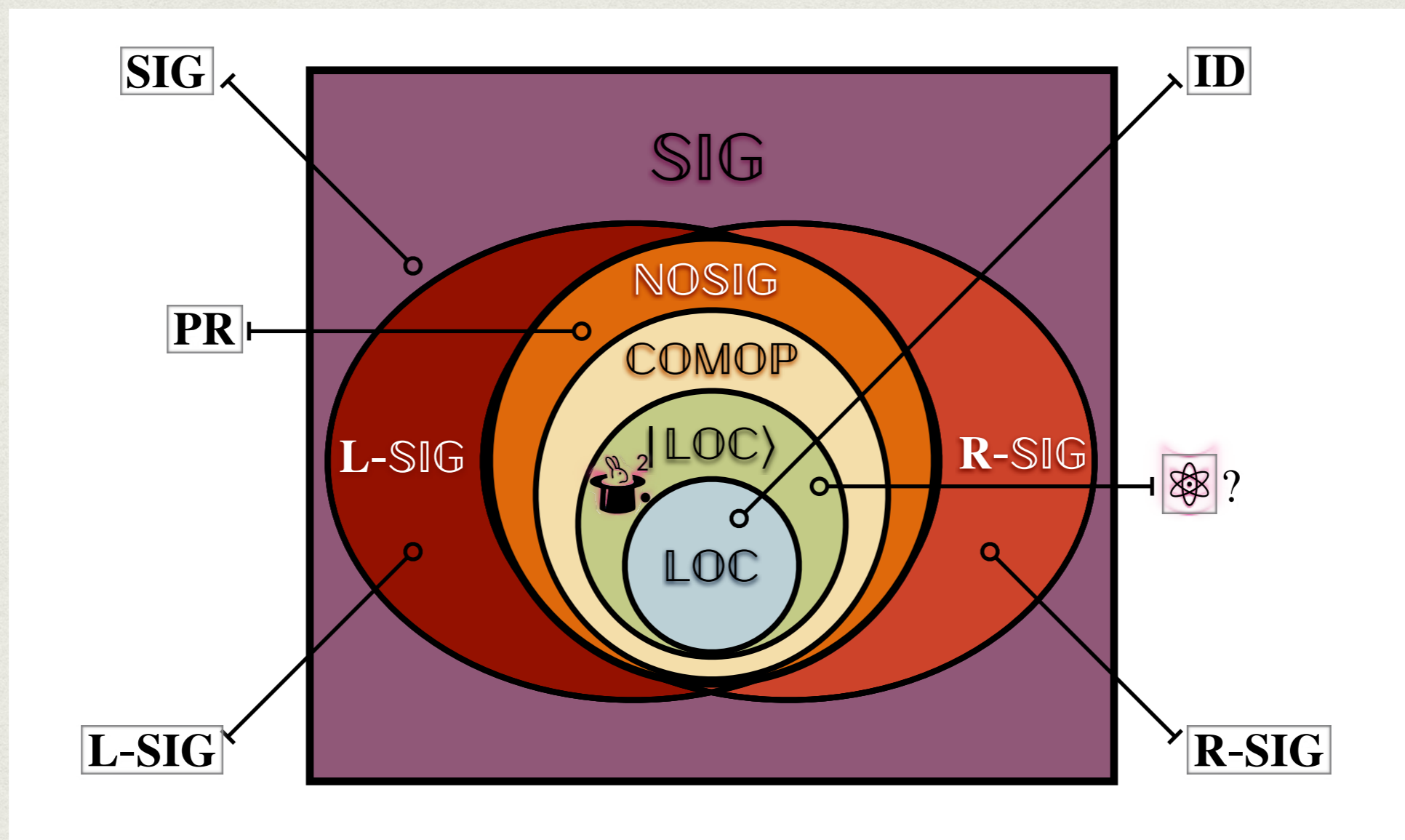
$$x_{i0} \oplus x_{i1} \oplus x_{i2} = 0$$

$$y_{0j} \oplus y_{1j} \oplus y_{2j} = 1$$

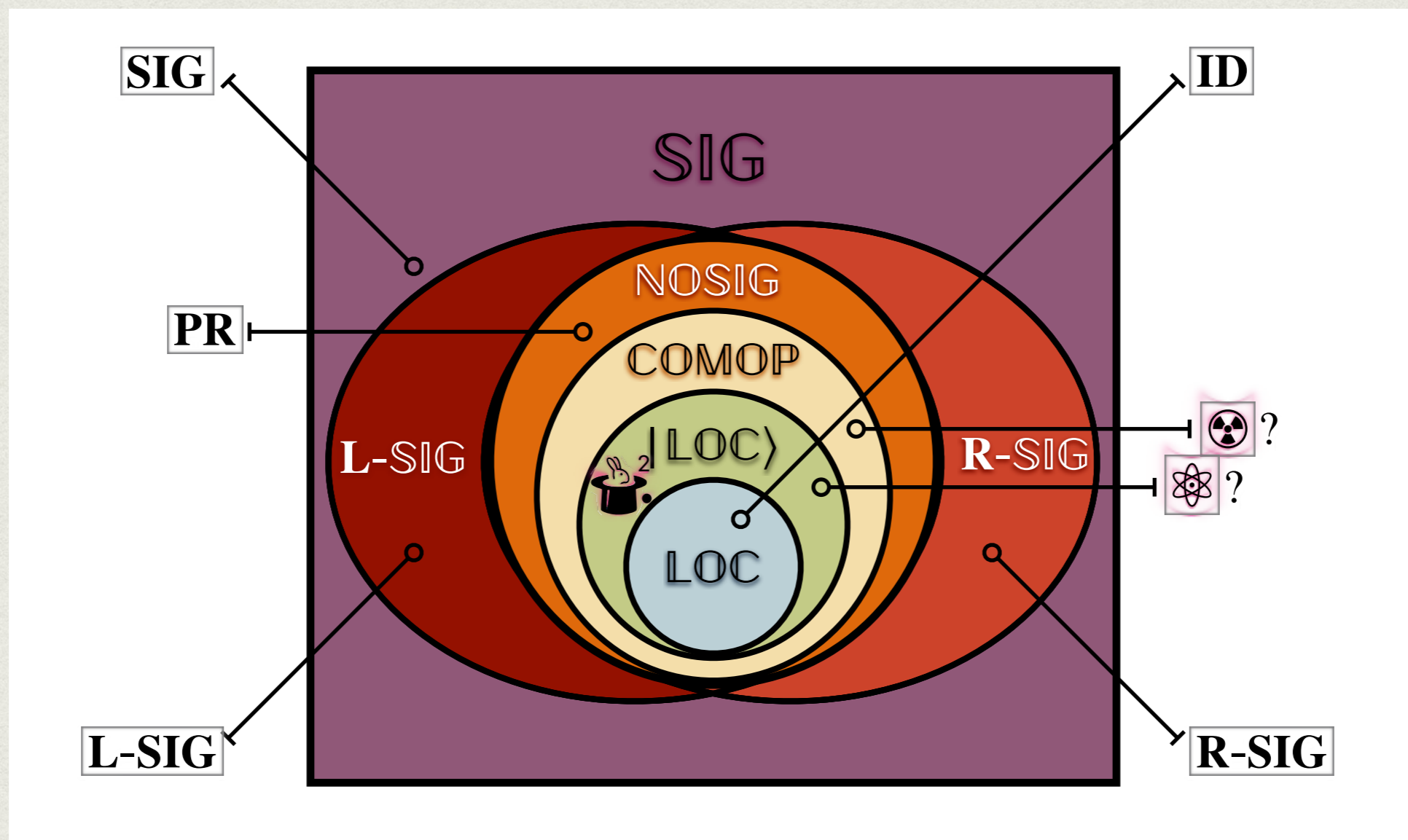
# HIERARCHIE DE NON-LOCALITÉ



# HIERARCHIE DE NON-LOCALITÉ



# HIERARCHIE DE NON-LOCALITÉ



# CLASSES DE COMPLEXITÉ

$$\text{MIP}^{\text{SIG}} = \text{IP} \\ = \text{PSPACE}$$

# CLASSES DE COMPLEXITÉ



$MIP^{SIG} = IP$   
 $= PSPACE$

$MIP^{LOC} = MIP$   
 $= NEXP$



# CLASSES DE COMPLEXITÉ

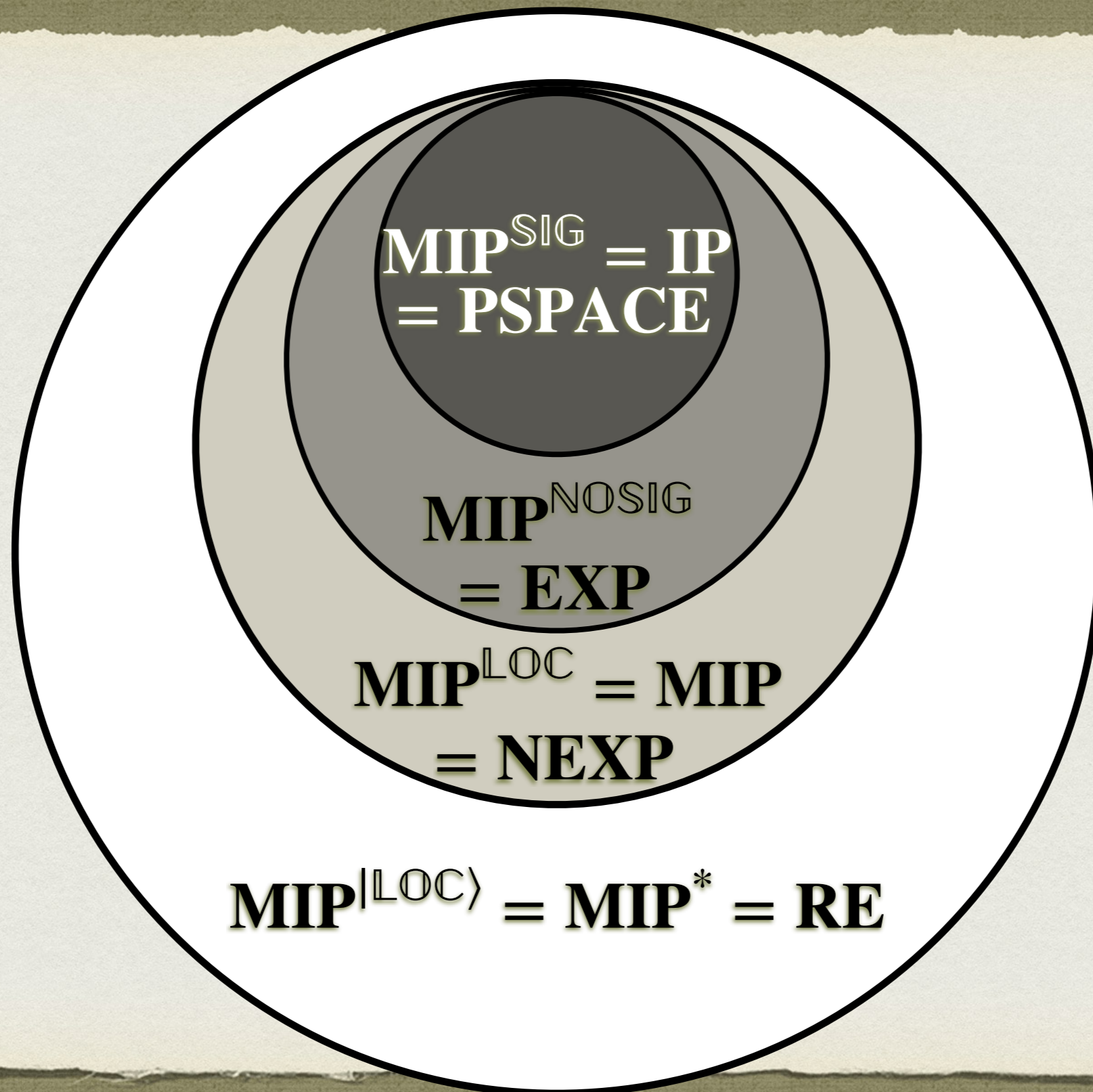


$MIP^{SIG} = IP$   
 $= PSPACE$

$MIP^{LOC} = MIP$   
 $= NEXP$

$MIP^{|\text{LOC}\rangle} = MIP^* = RE$

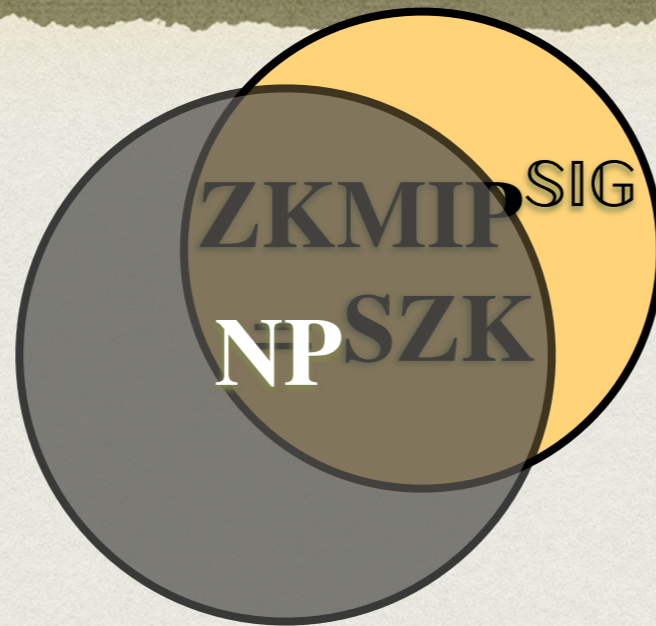
# CLASSES DE COMPLEXITÉ



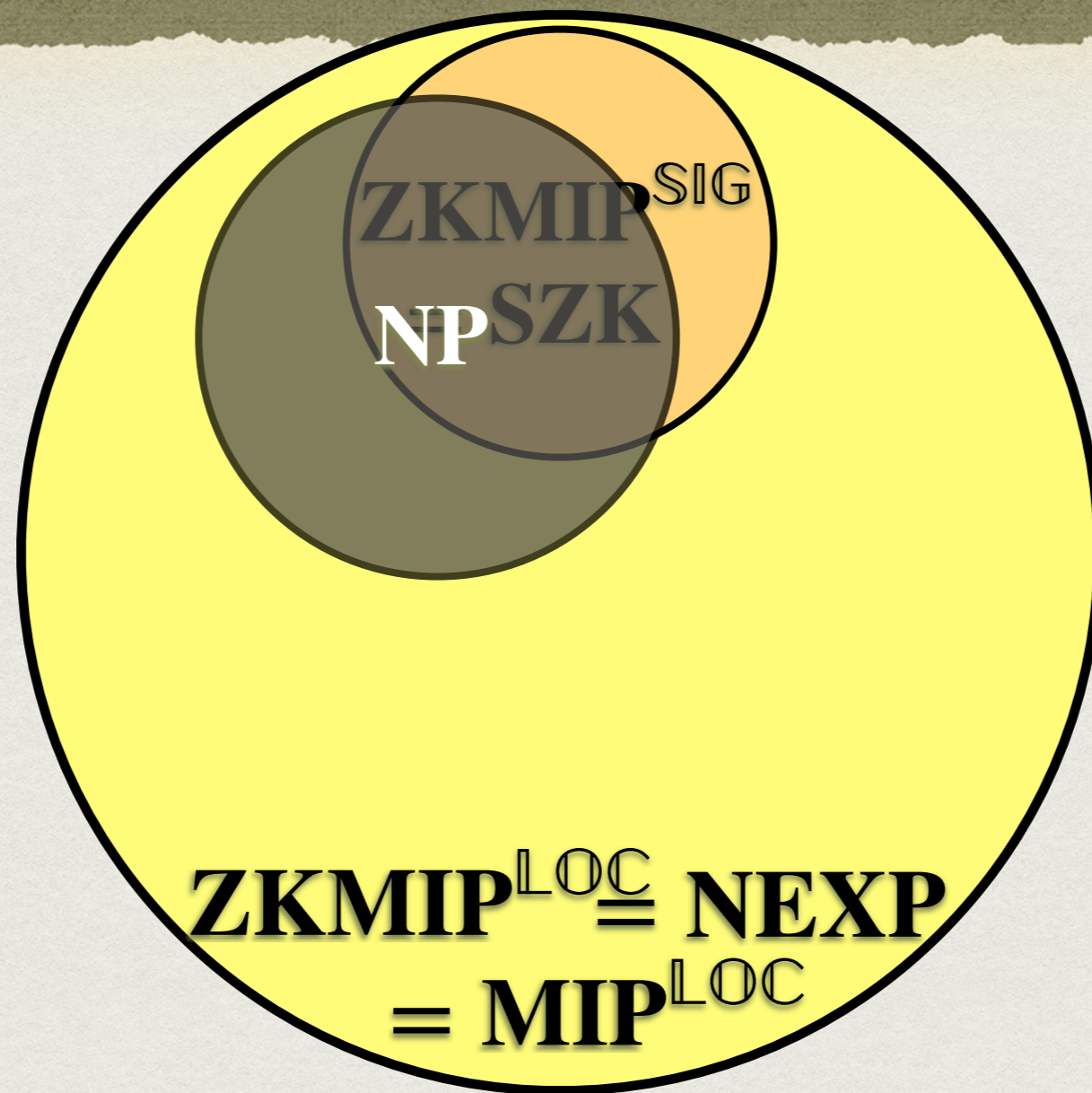
# CLASSES DE COMPLEXITÉ ZK

**ZKMIP<sup>SIG</sup>**  
**= SZK**

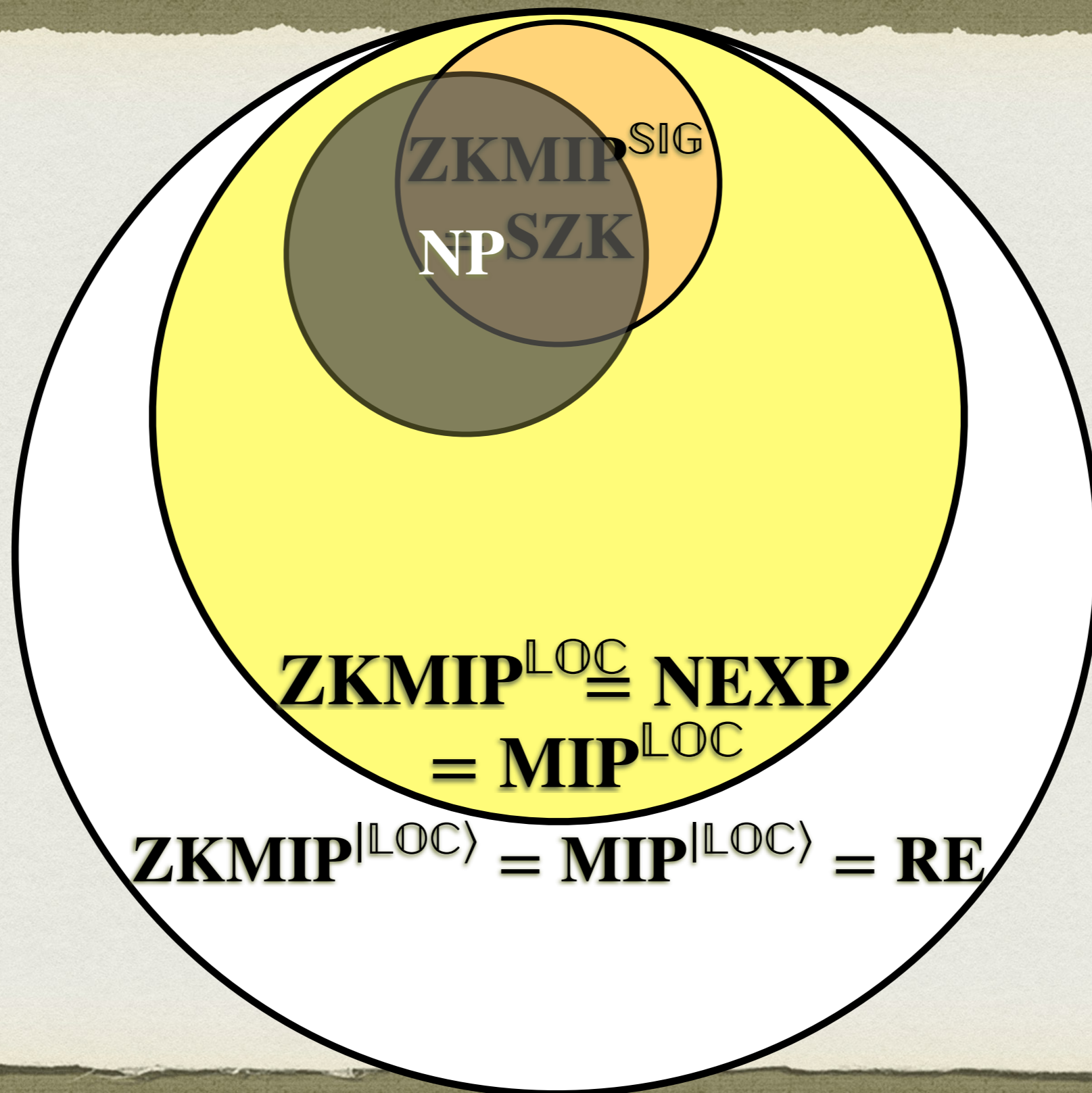
# CLASSES DE COMPLEXITÉ ZK



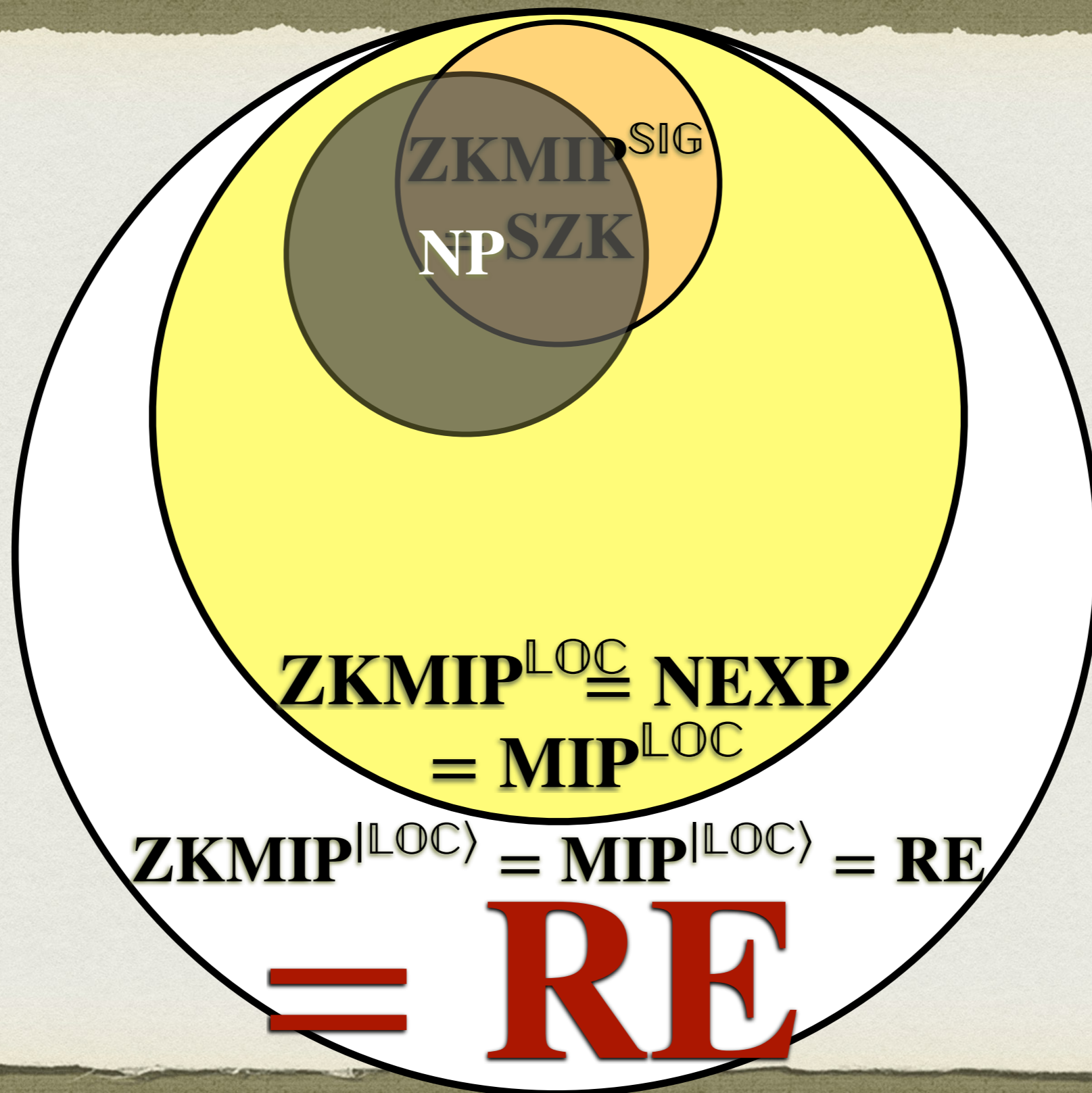
# CLASSES DE COMPLEXITÉ ZK



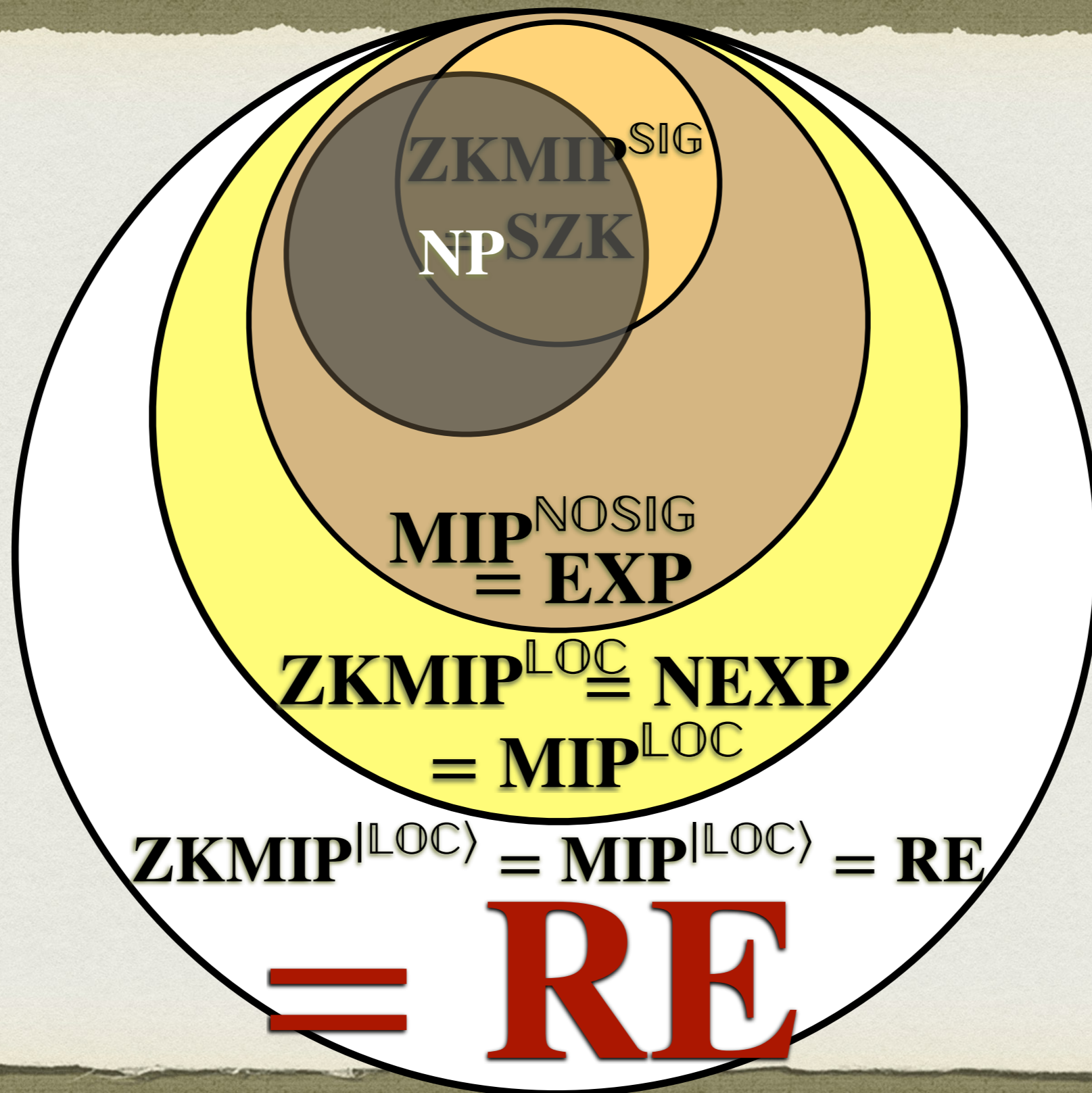
# CLASSES DE COMPLEXITÉ ZK



# CLASSES DE COMPLEXITÉ ZK

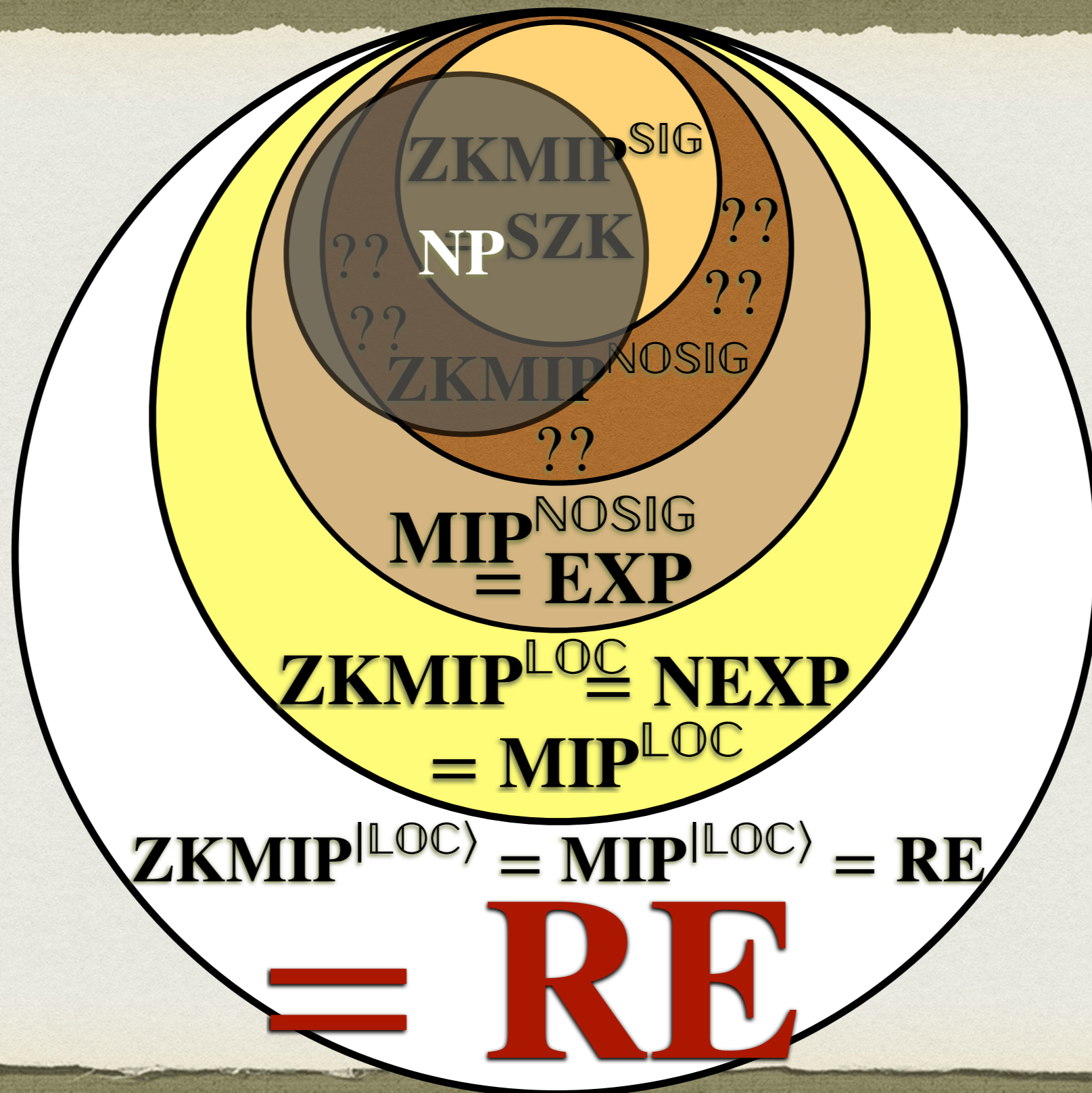


# CLASSES DE COMPLEXITÉ ZK

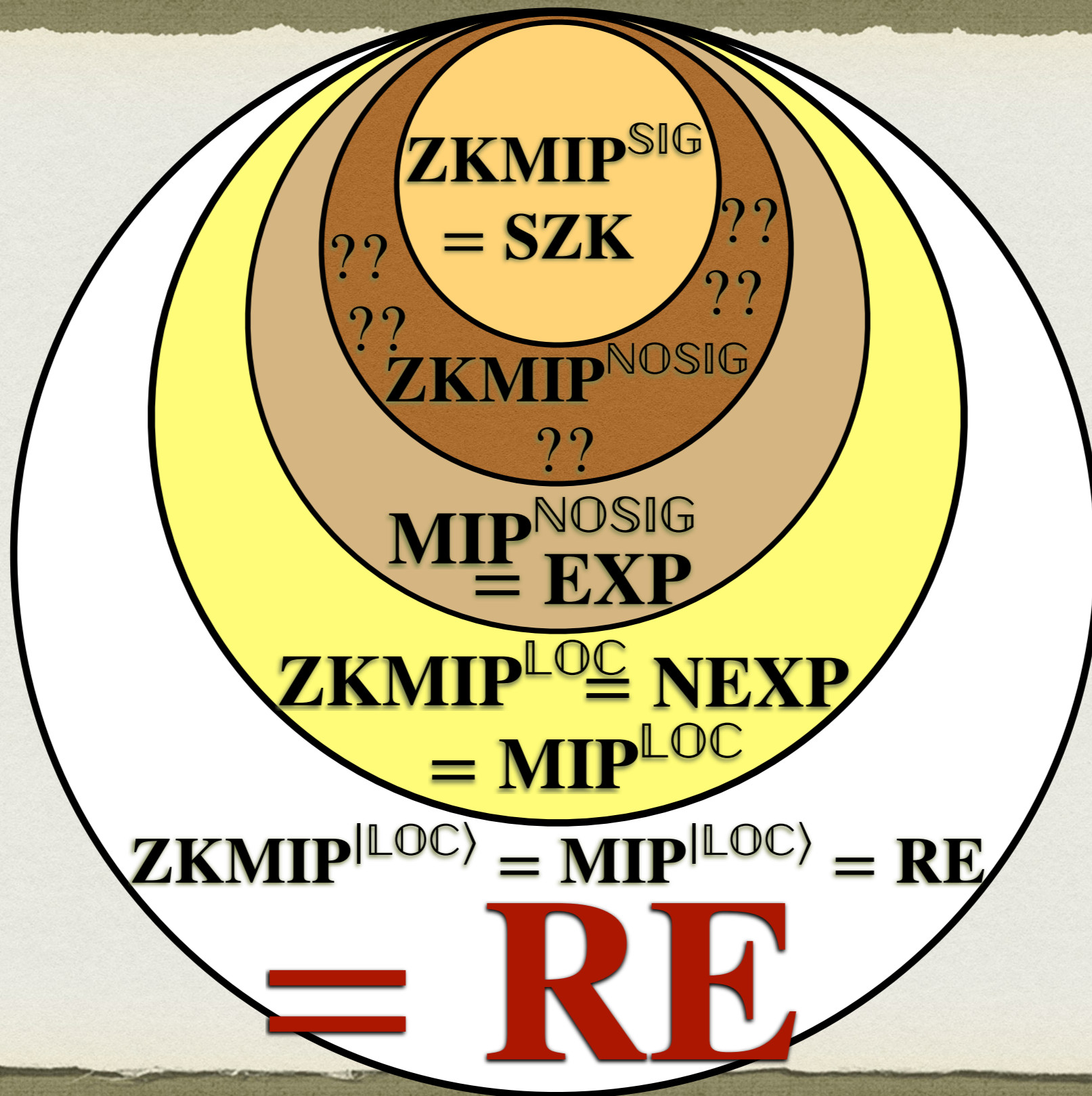


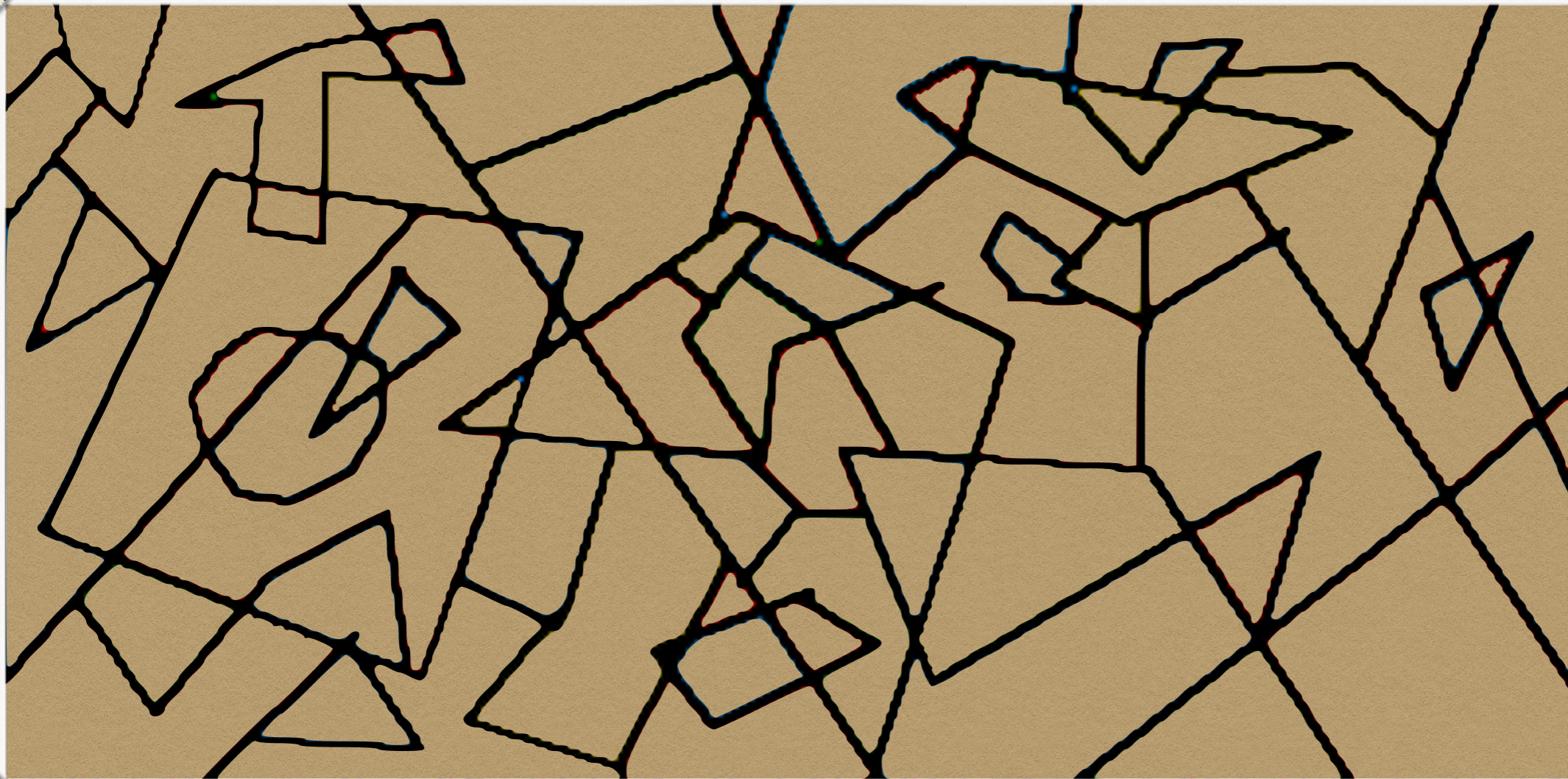


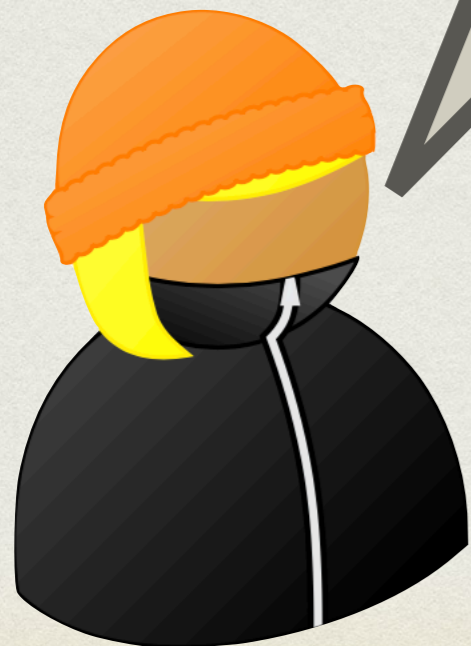
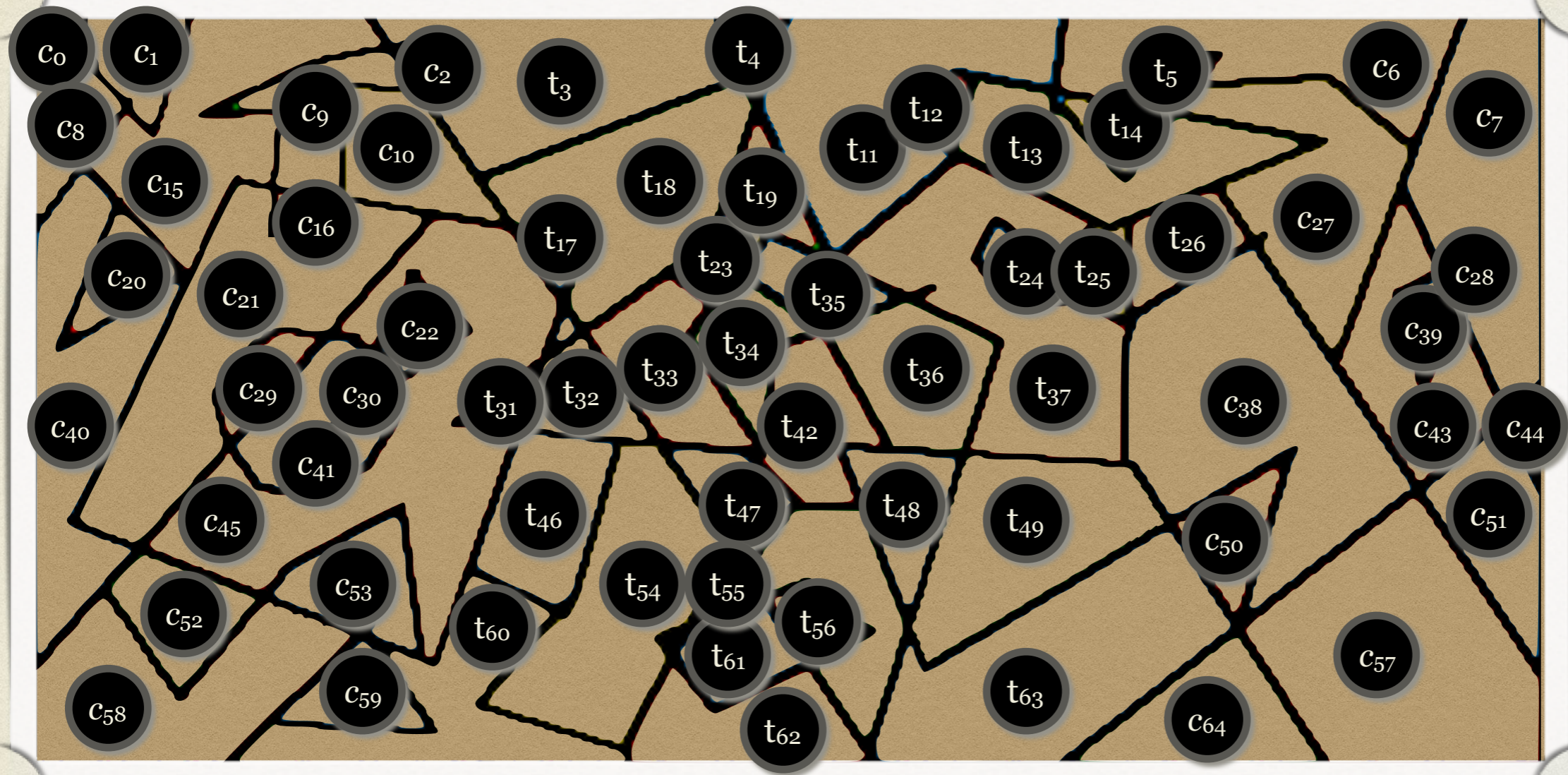
# CLASSES DE COMPLEXITÉ ZK



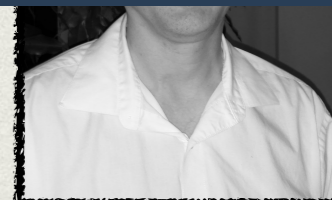
# CLASSES DE COMPLEXITÉ ZK







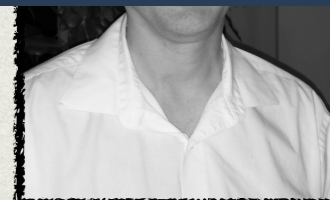
# COHÉRENCE INTRIQUÉE ?



COHÉRENCE INTRIQUÉE

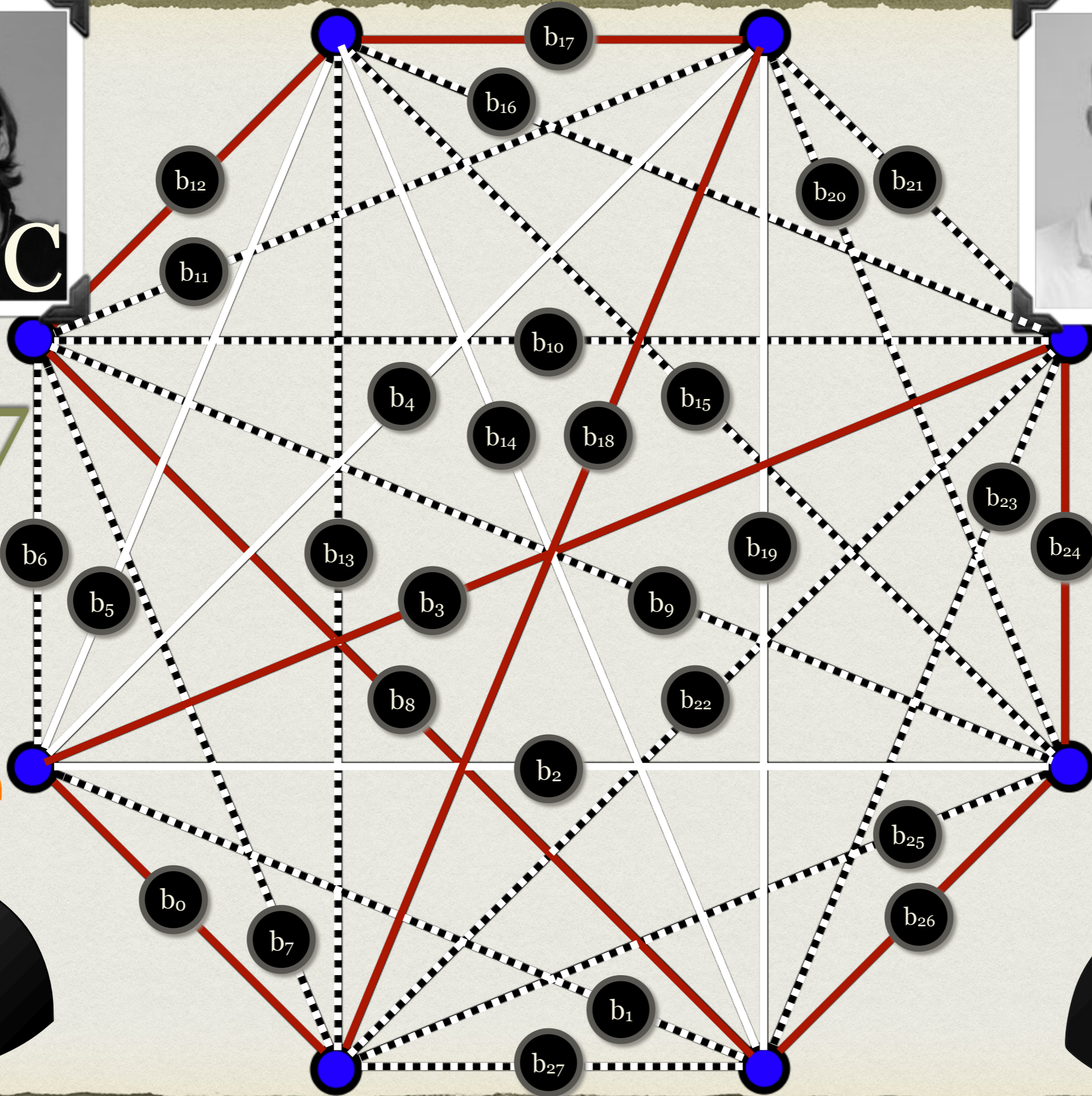
?

SAIS PAS !

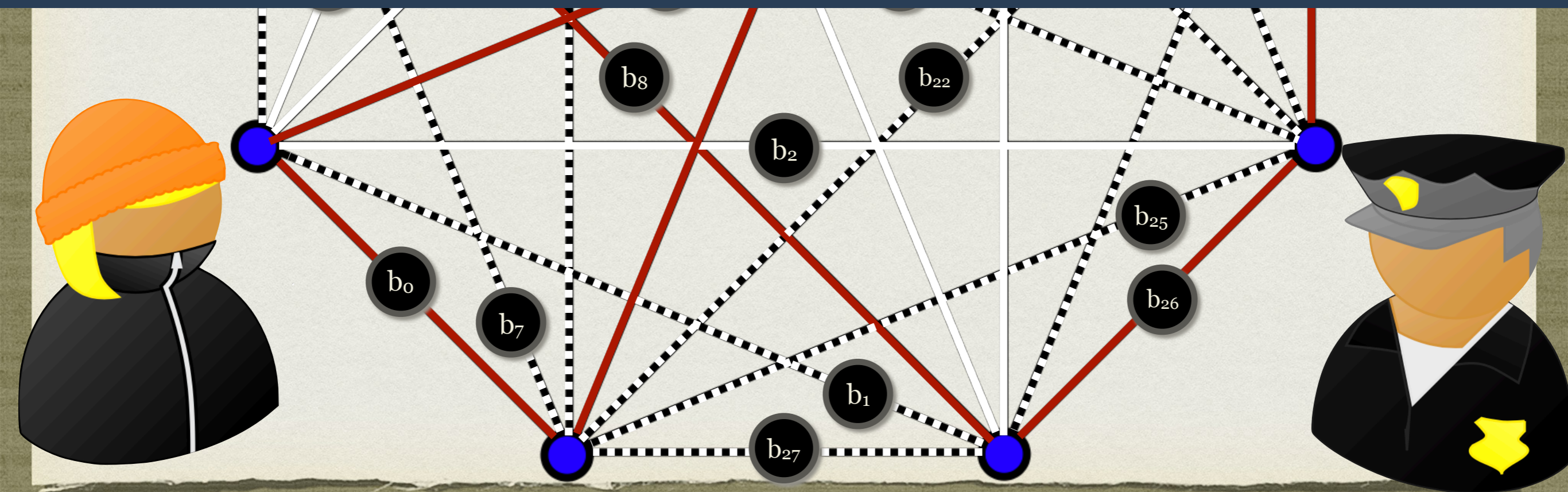




2017



# COHÉRENCE INTRIFIQUÉE ?

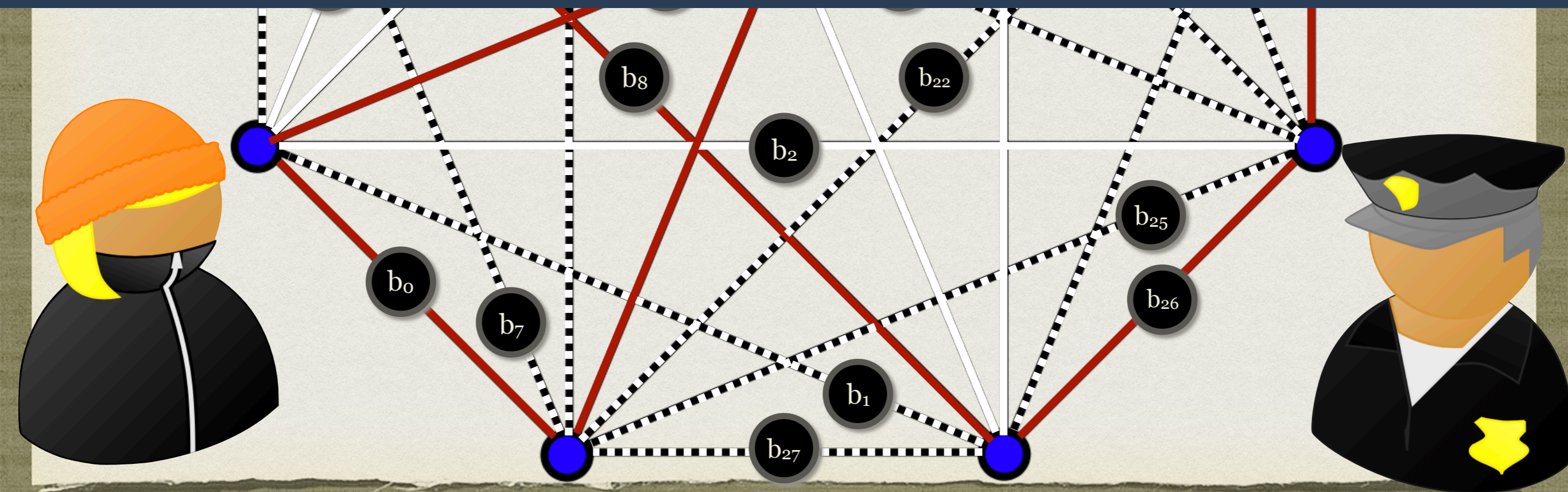




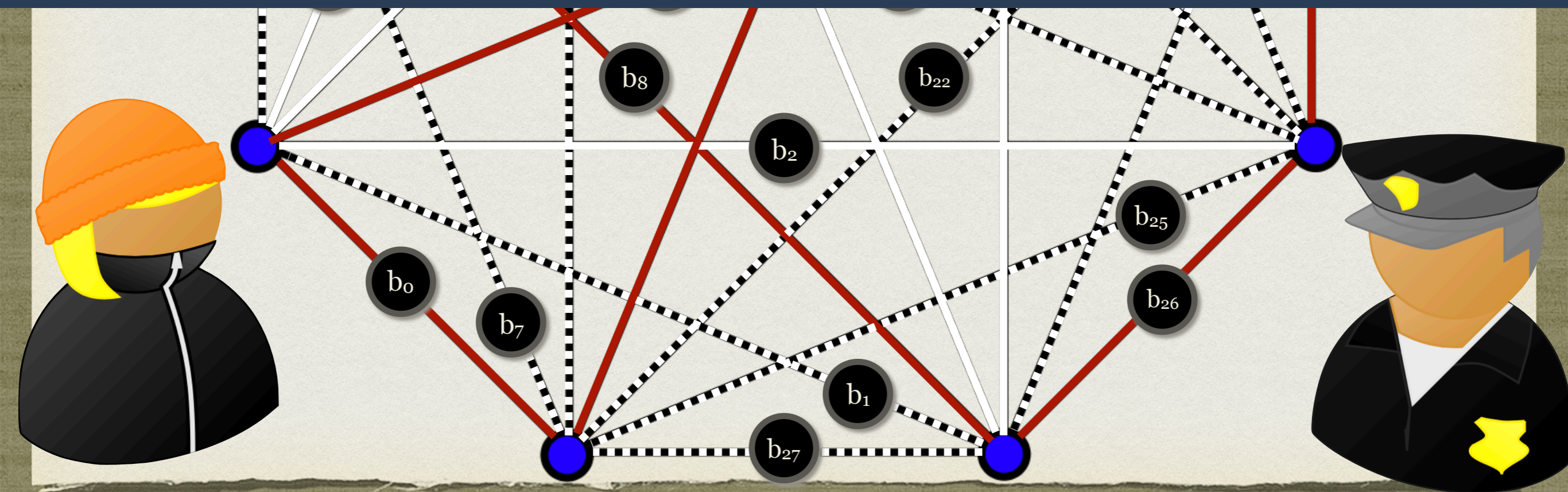
COHÉRENCE INTRIFIQUÉE

?

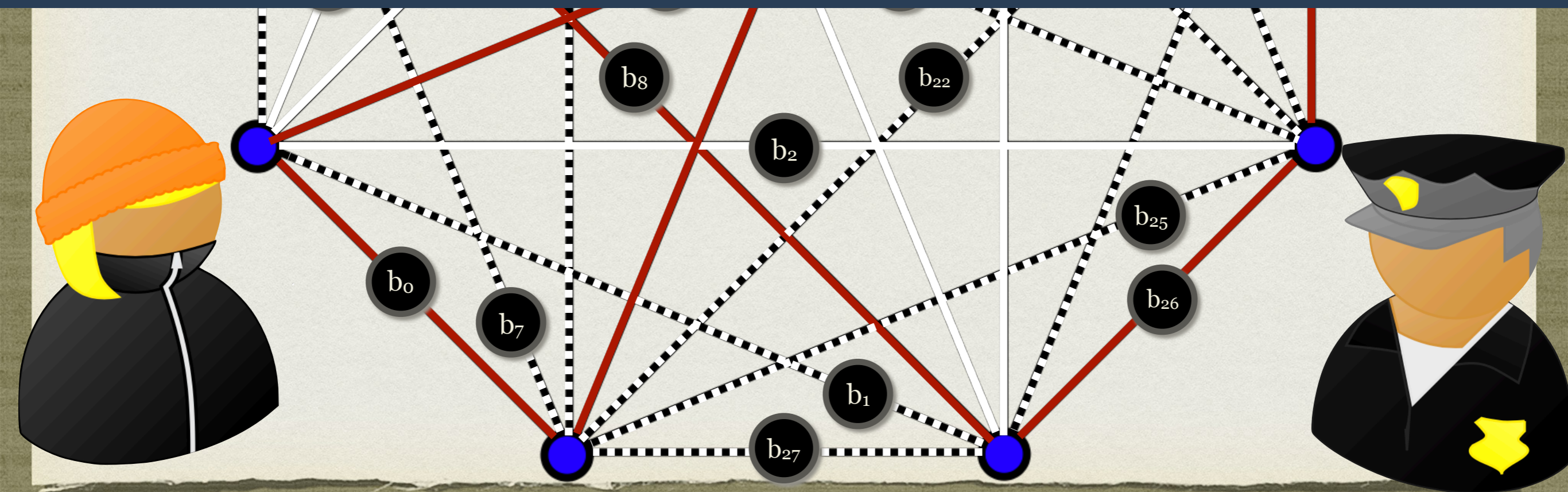
OUI!



# PRACTIQUE ?

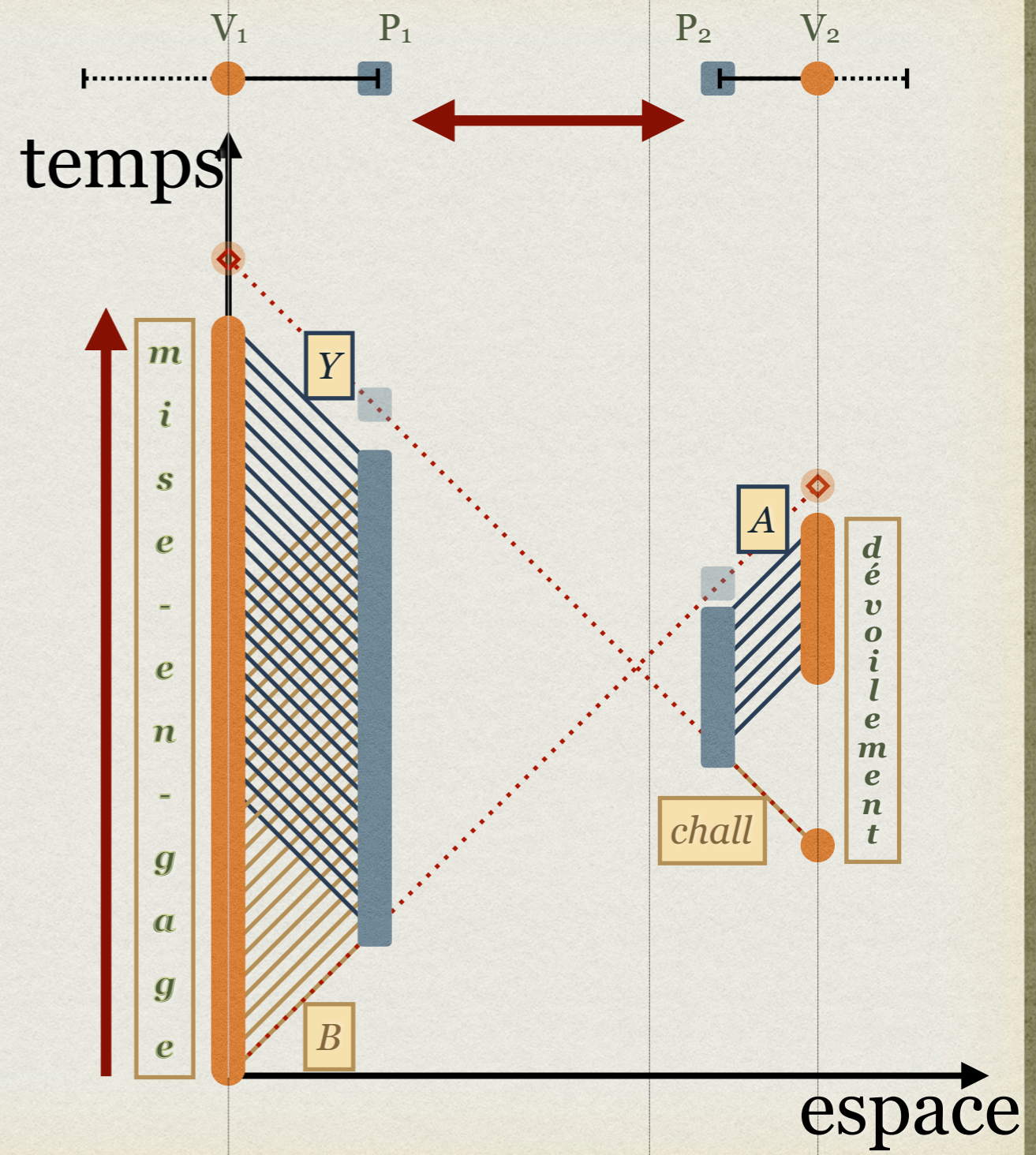
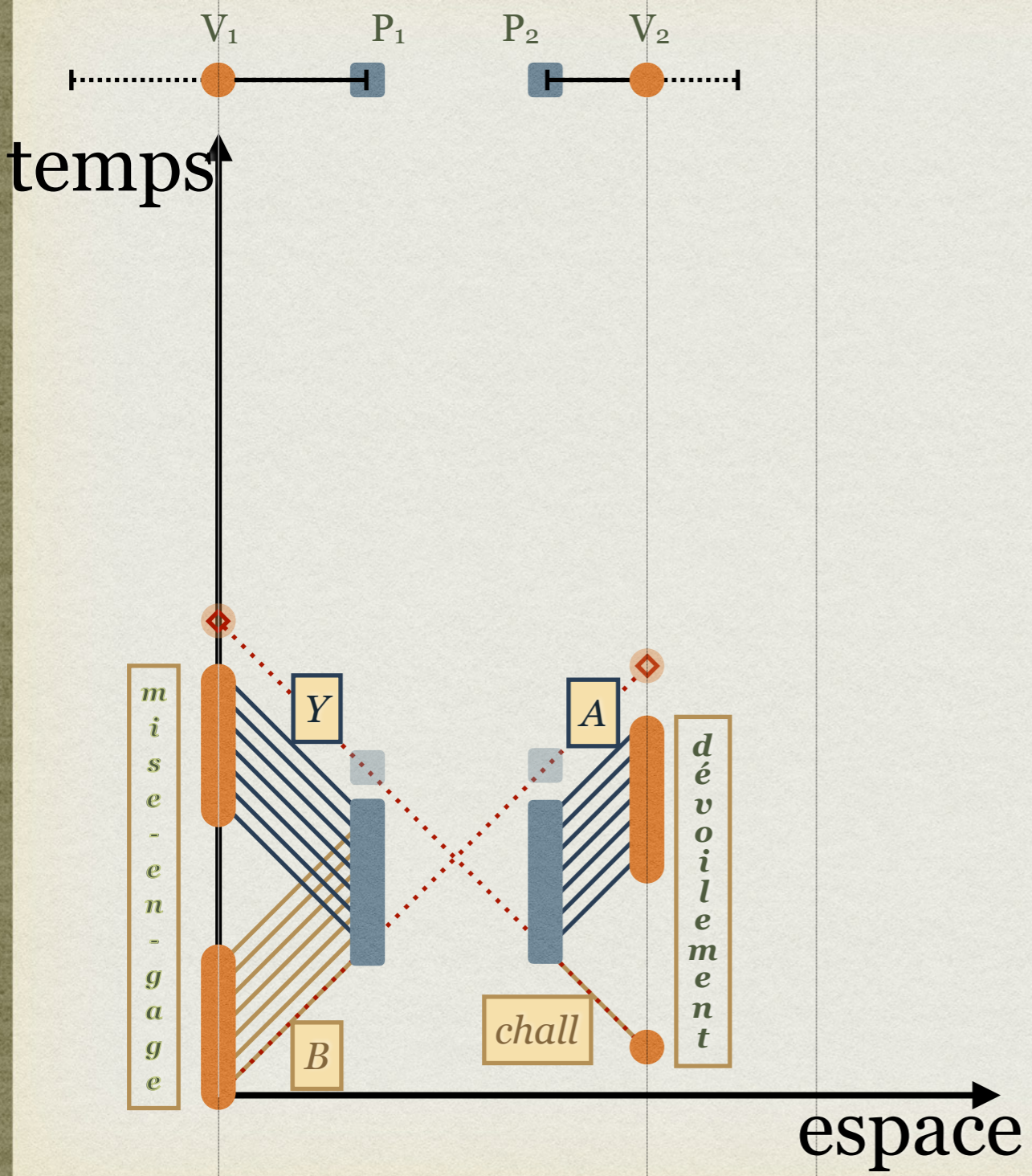


PRACTIQUE ?  
OH QUE NON !





# CHAILLOUX-LEVERRIER





Massenet



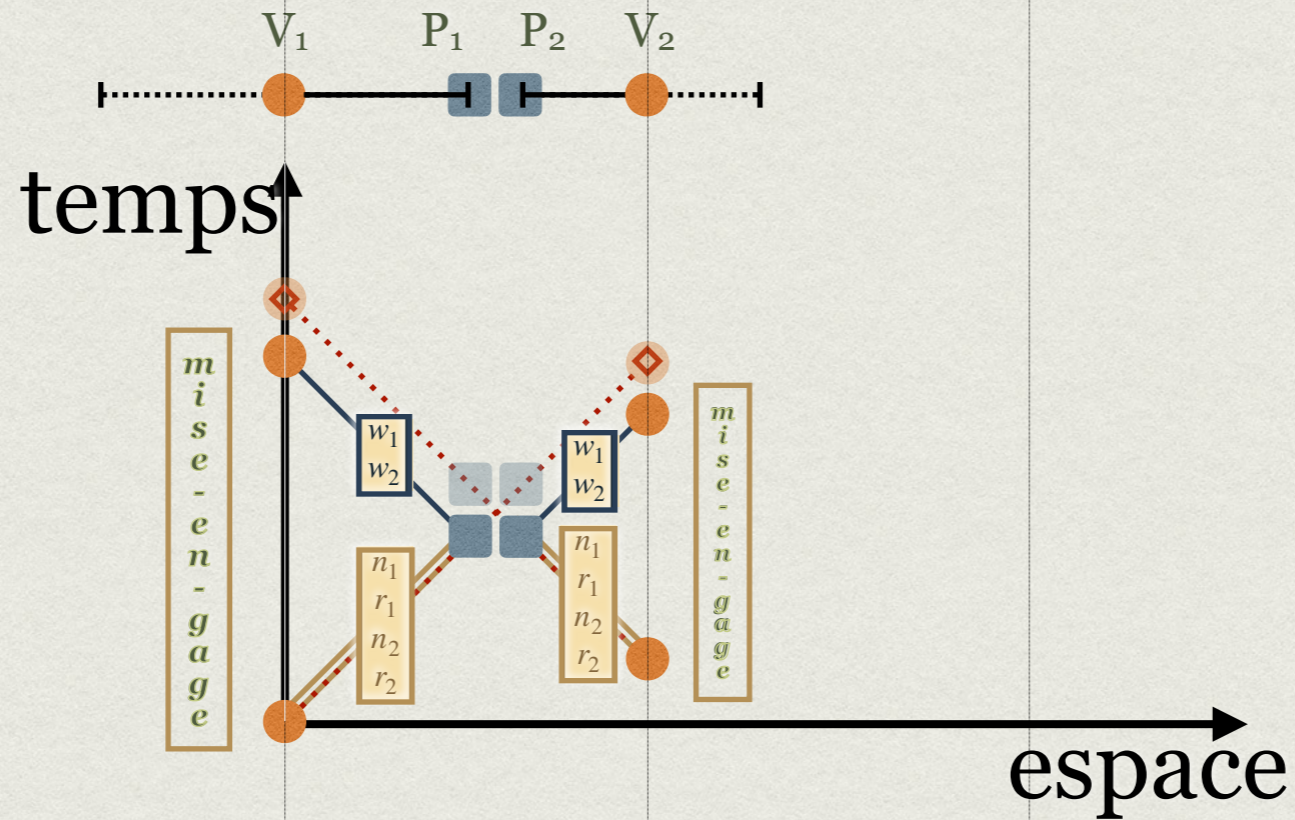
Salvail

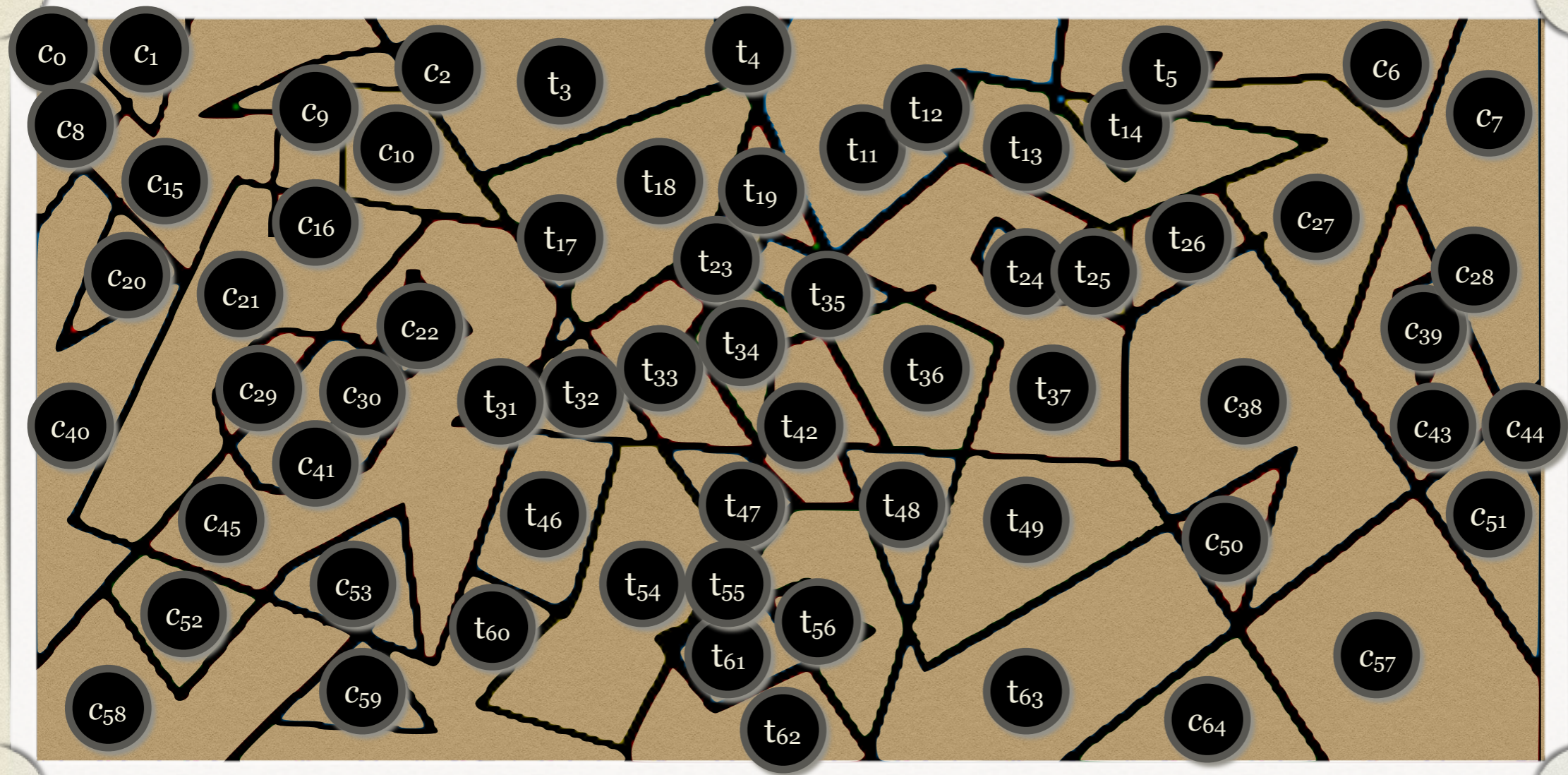


Stinchcombe



Yang



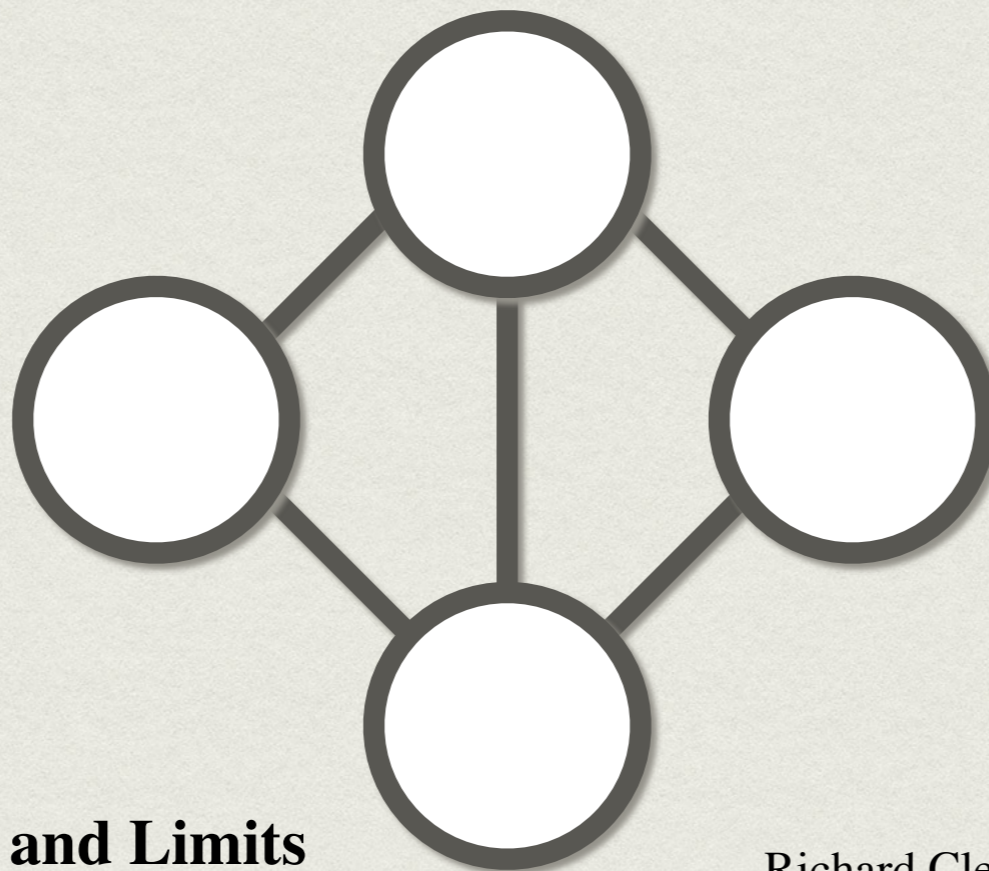
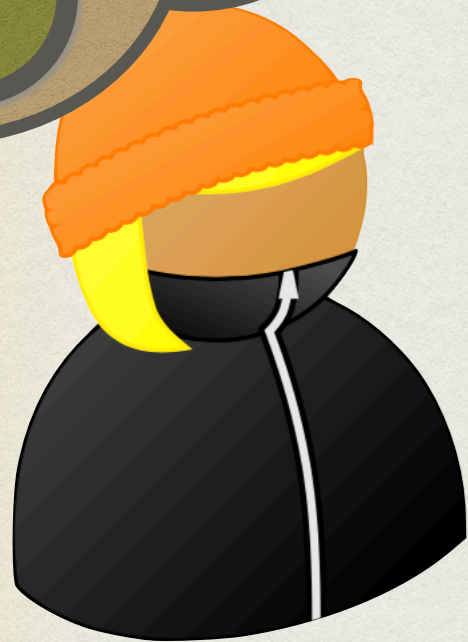
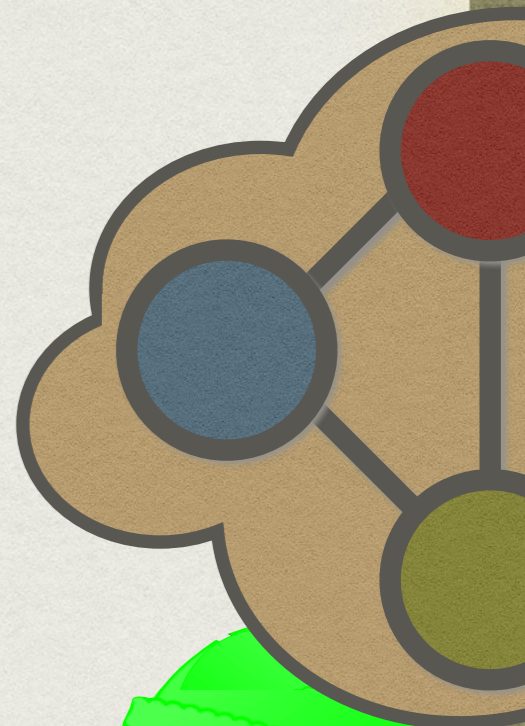
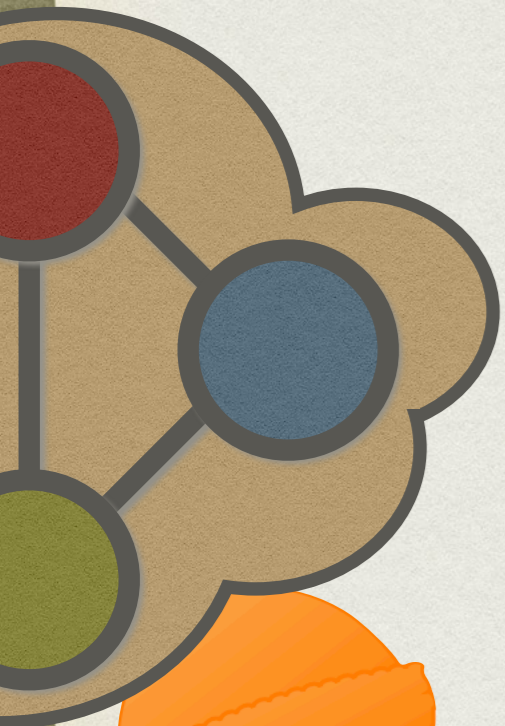


# NOTRE APPROCHE

*(ZK)MIPs*



2004  
**COMPLÉTUDE**



**Consequences and Limits  
of Nonlocal Strategies**

Richard Cleve  
Benjamin Toner

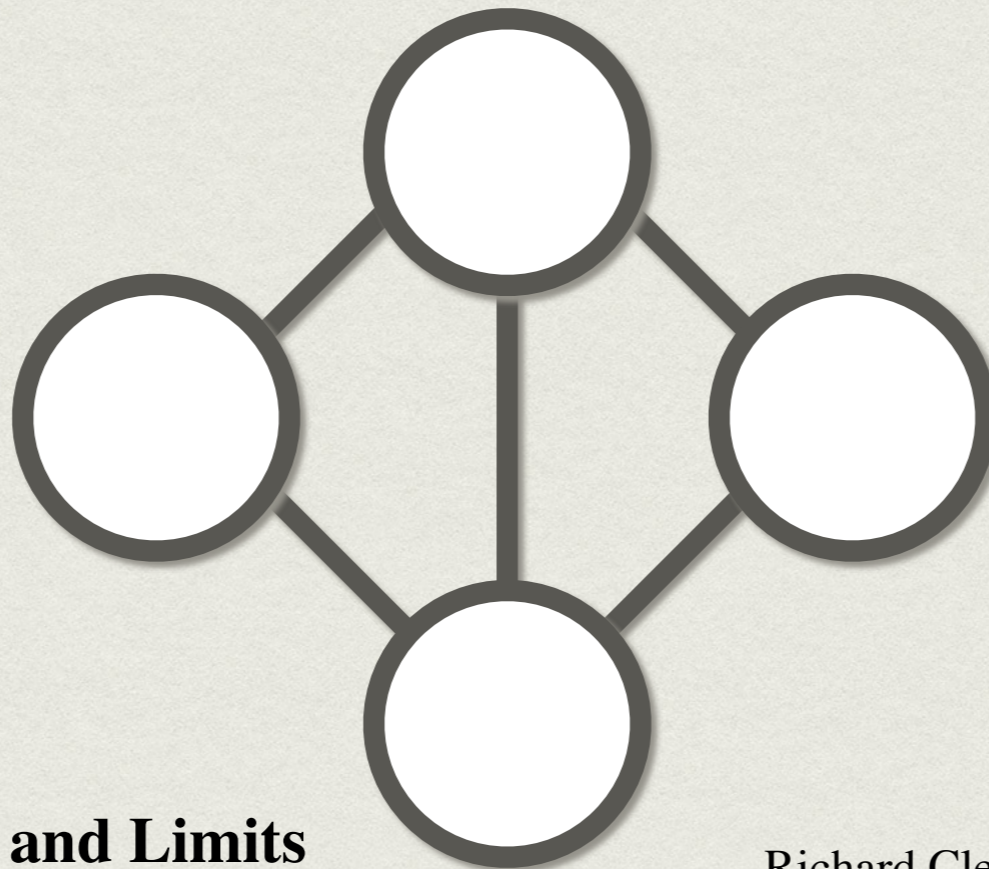
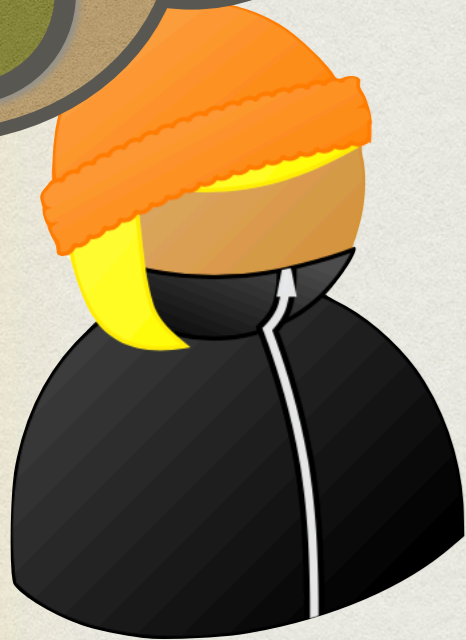
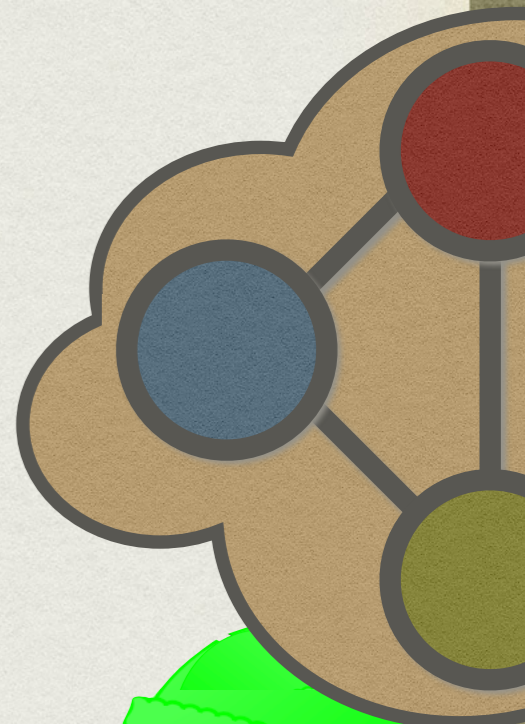
Peter Høyer  
John Watrous





2

# 2004 COMPLÉTUDE



**Consequences and Limits  
of Nonlocal Strategies**

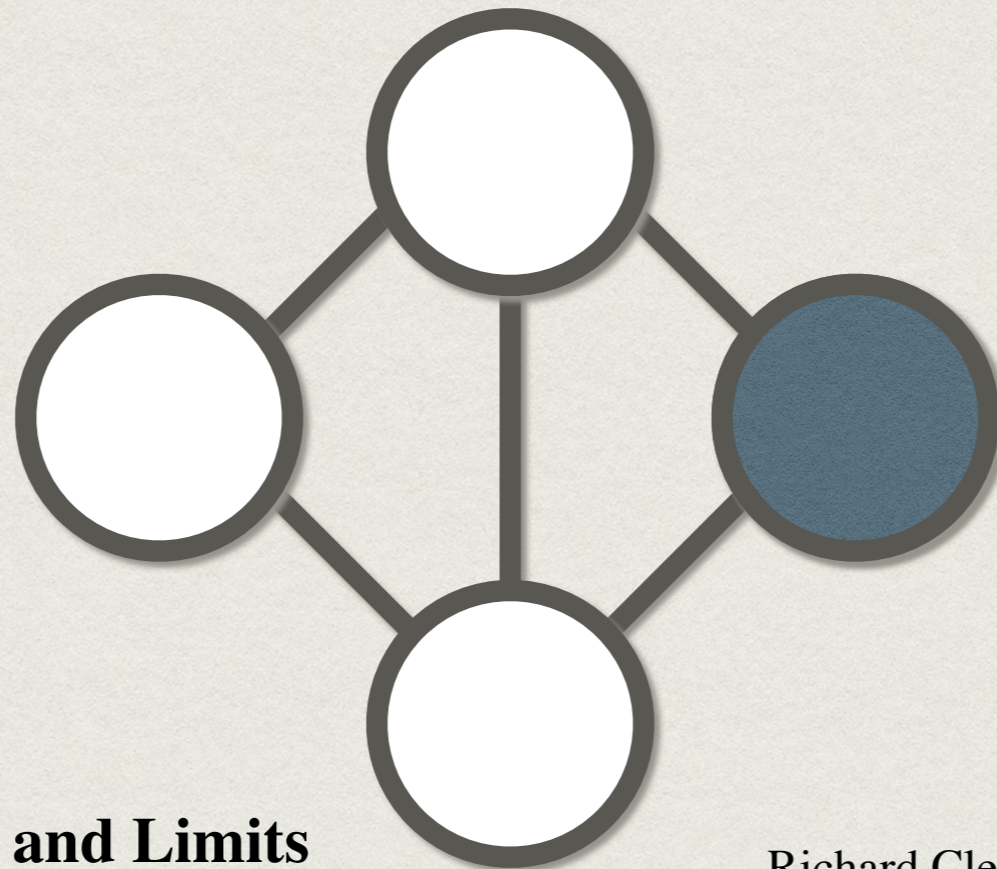
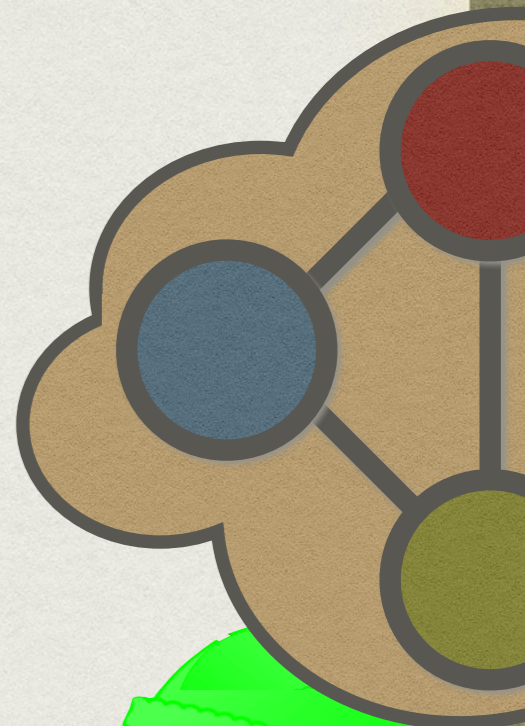
Richard Cleve  
Benjamin Toner

Peter Høyer  
John Watrous



2

# 2004 COMPLÉTUDE



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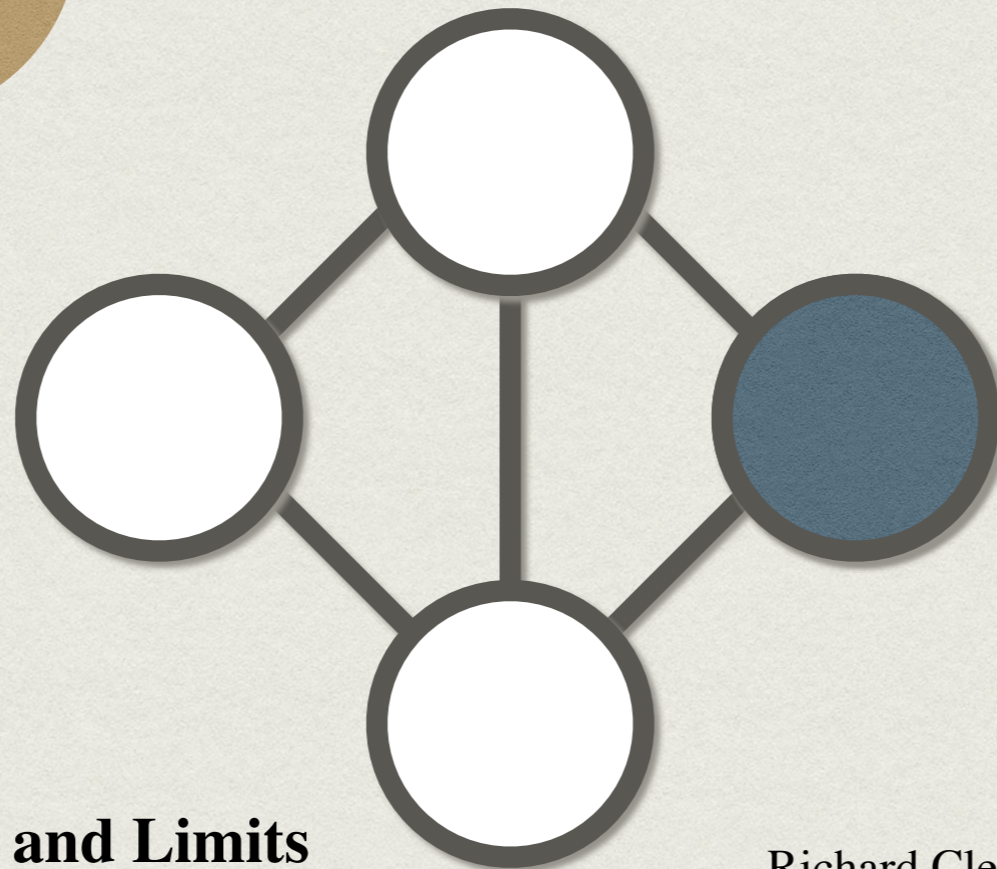
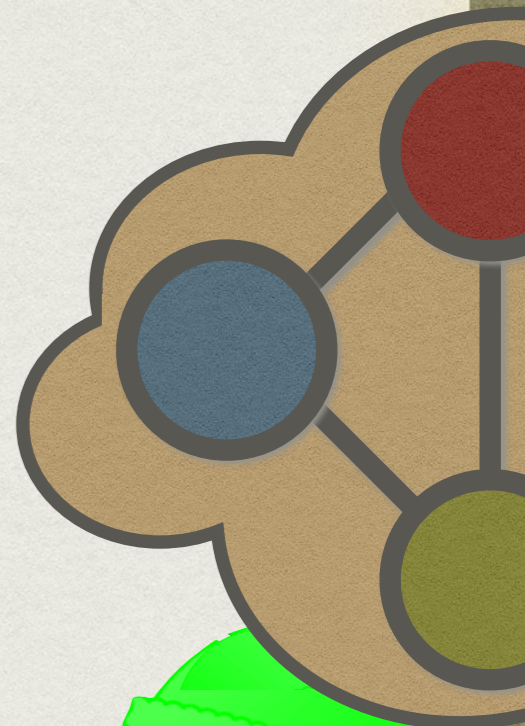
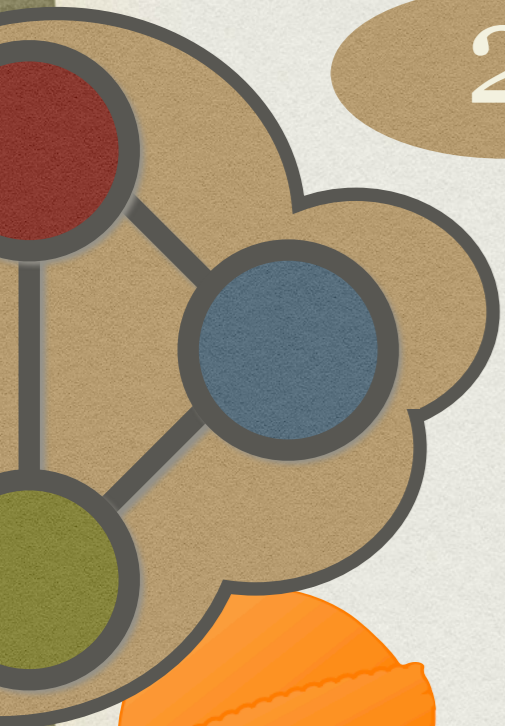
Peter Høyer  
John Watrous



2

2004

# COMPLÉTUDE



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Peter Høyer  
John Watrous

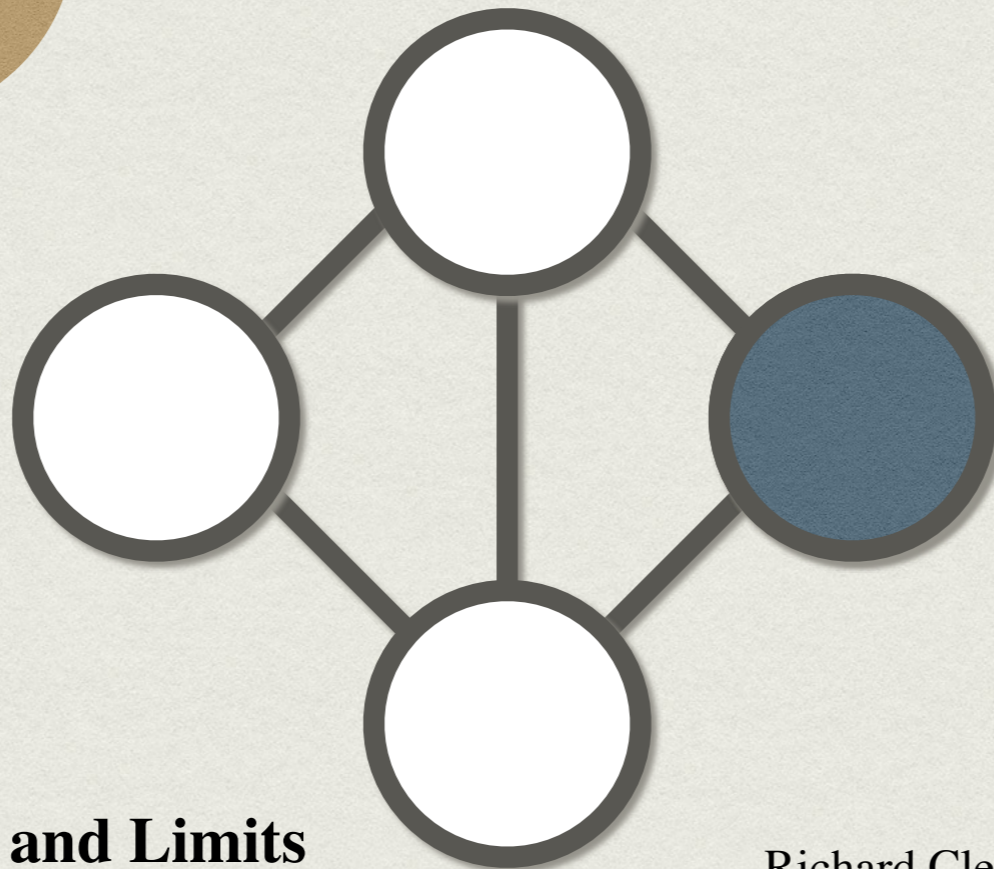
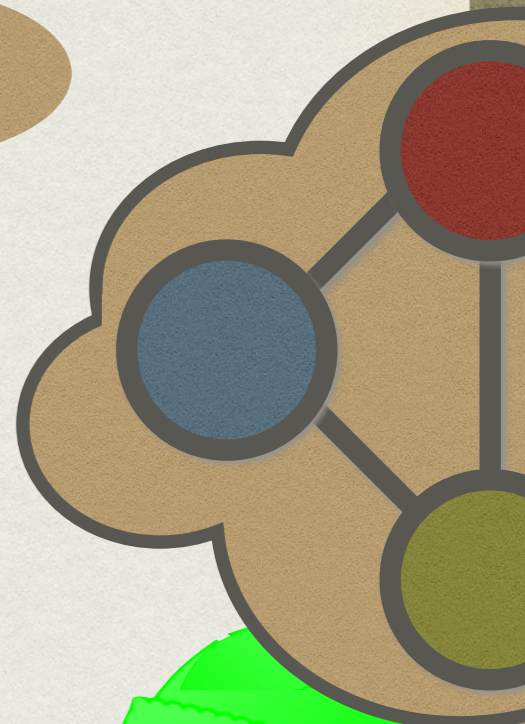


2

3

2004

# COMPLÉTUDE



**Consequences and Limits  
of Nonlocal Strategies**

Richard Cleve  
Benjamin Toner

Peter Høyer  
John Watrous

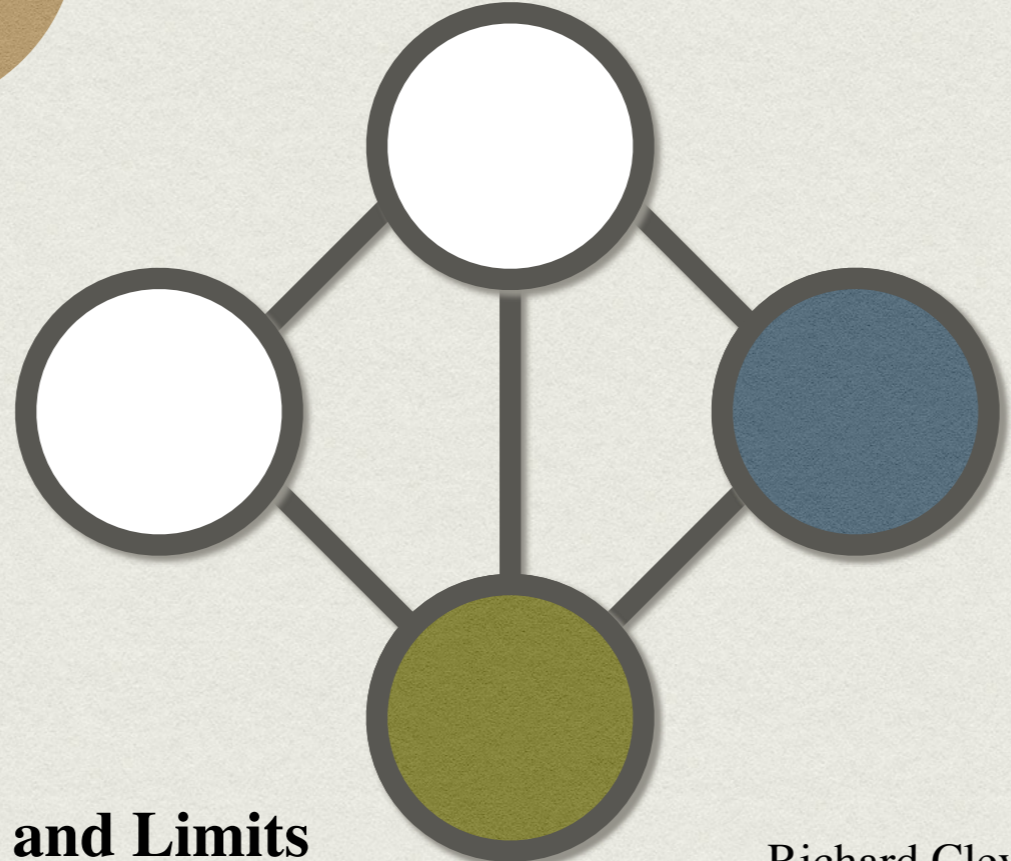


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3

2004

# COMPLÉTUDE



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Peter Høyer  
John Watrous

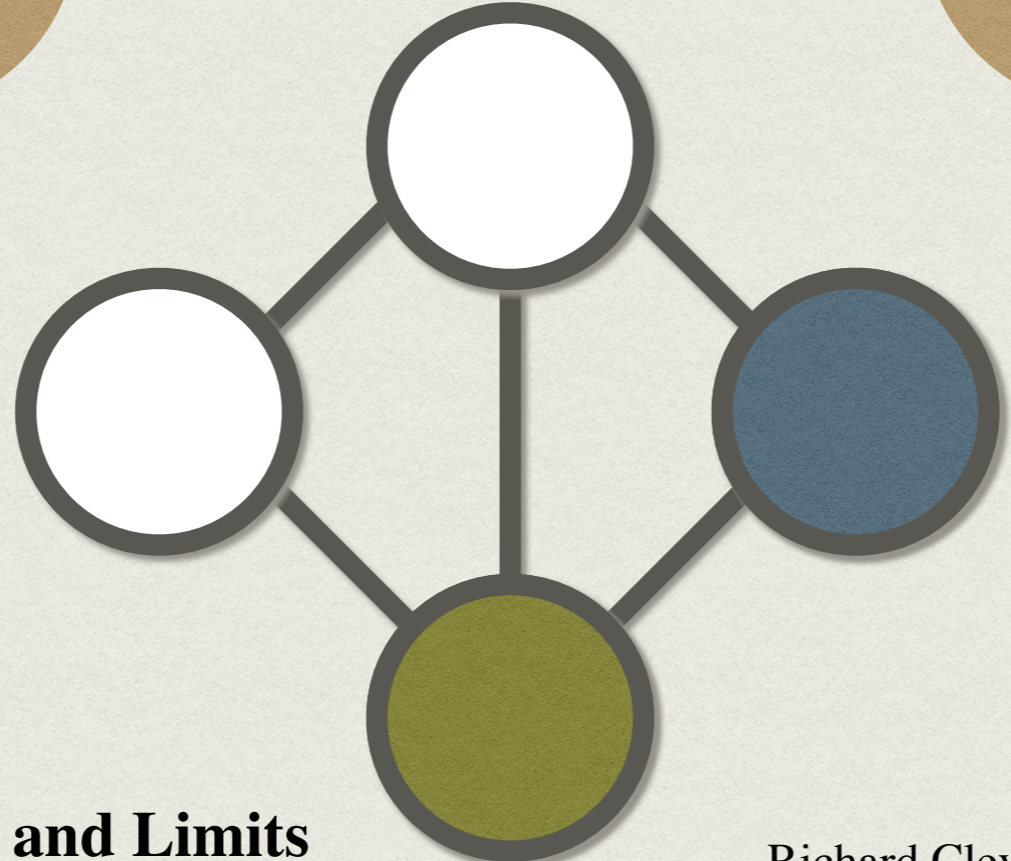
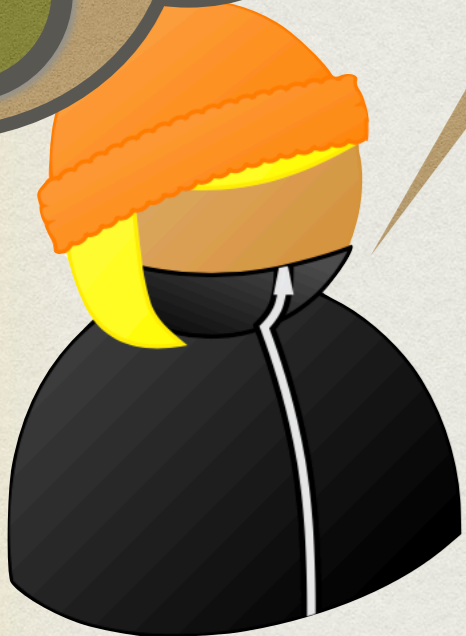
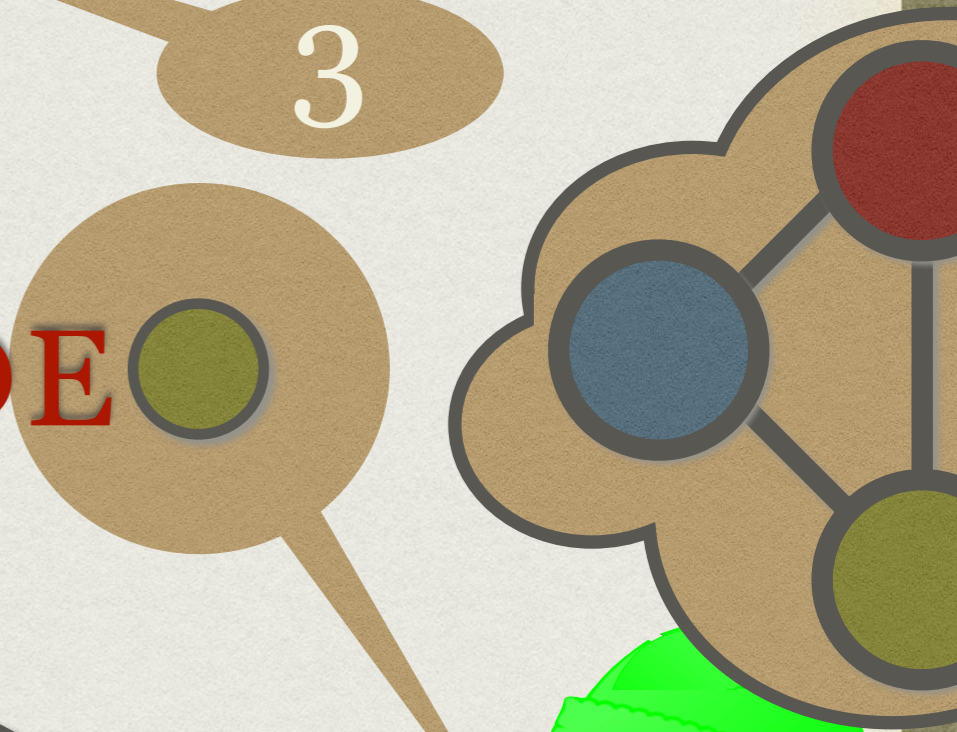
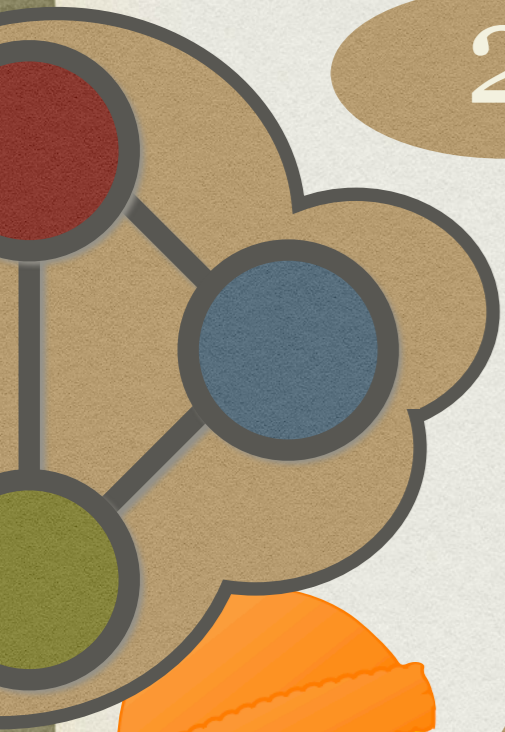


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2004

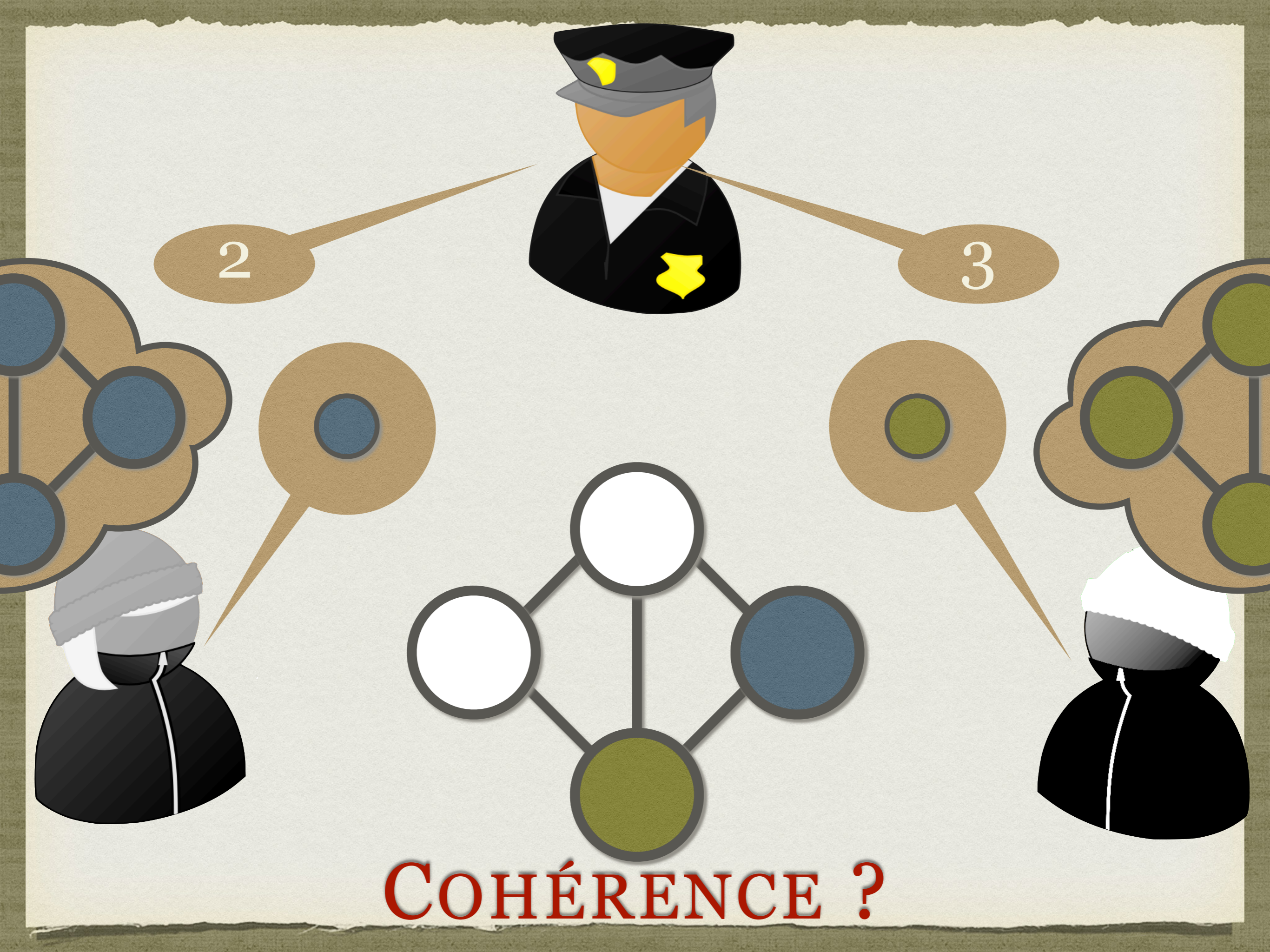
# COMPLÉTUDE



**Consequences and Limits  
of Nonlocal Strategies**

Richard Cleve  
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John Watrous

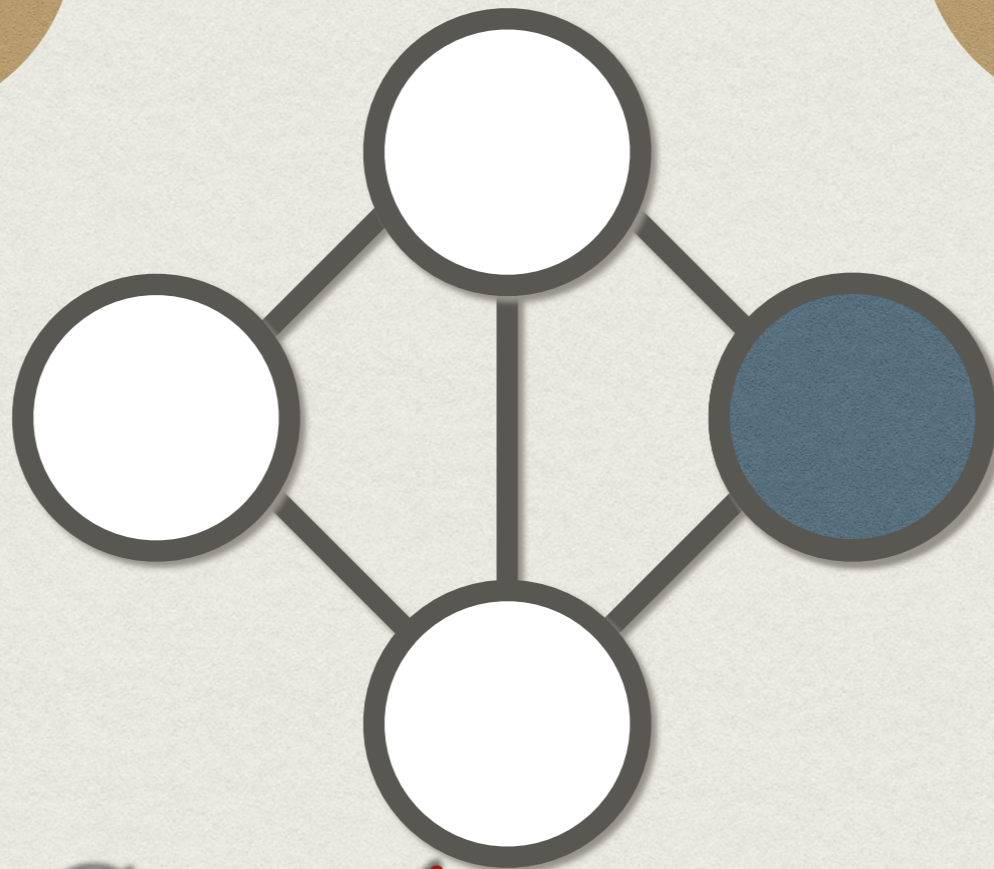




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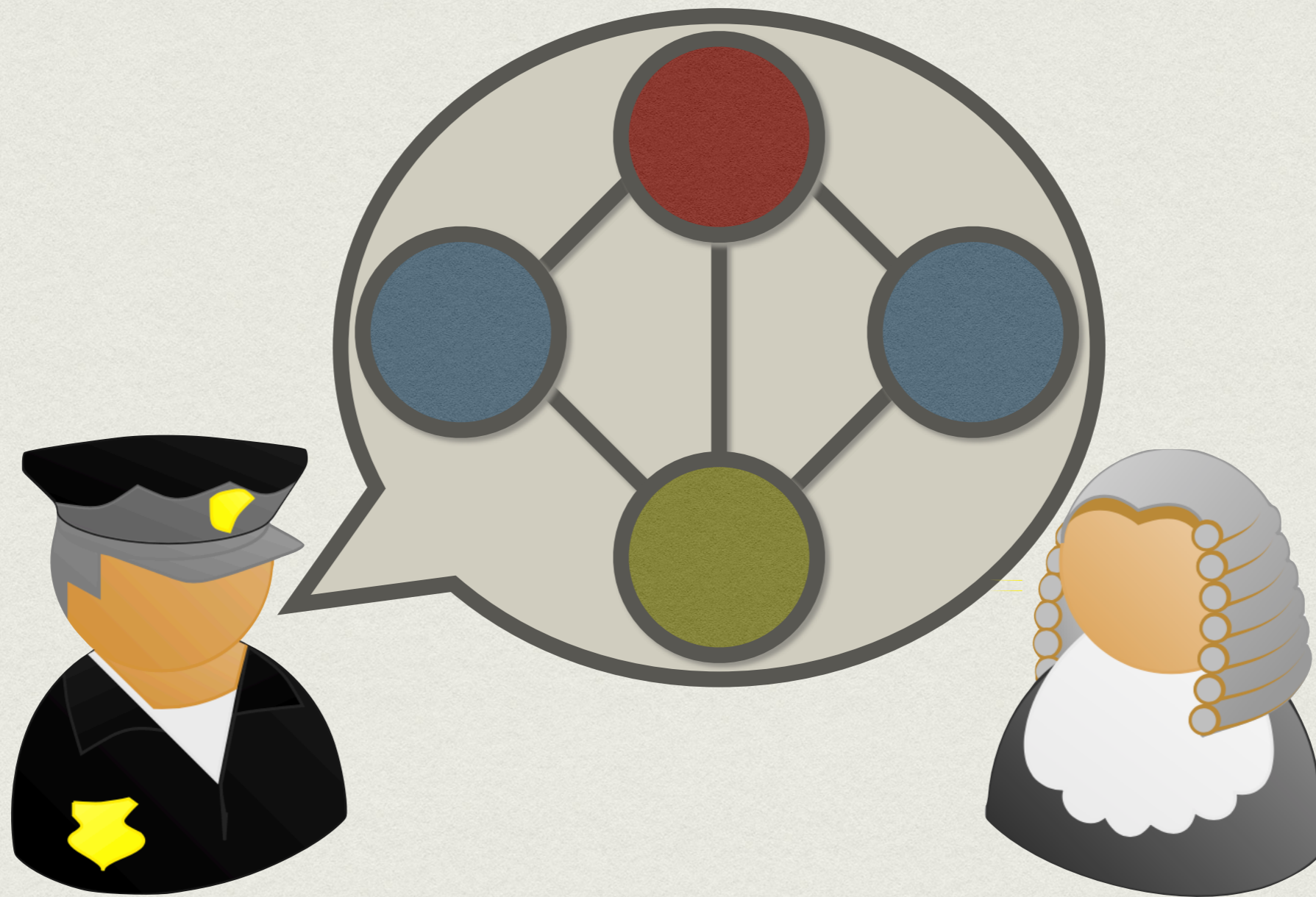
COMPLÉTUDE



COHÉRENCE





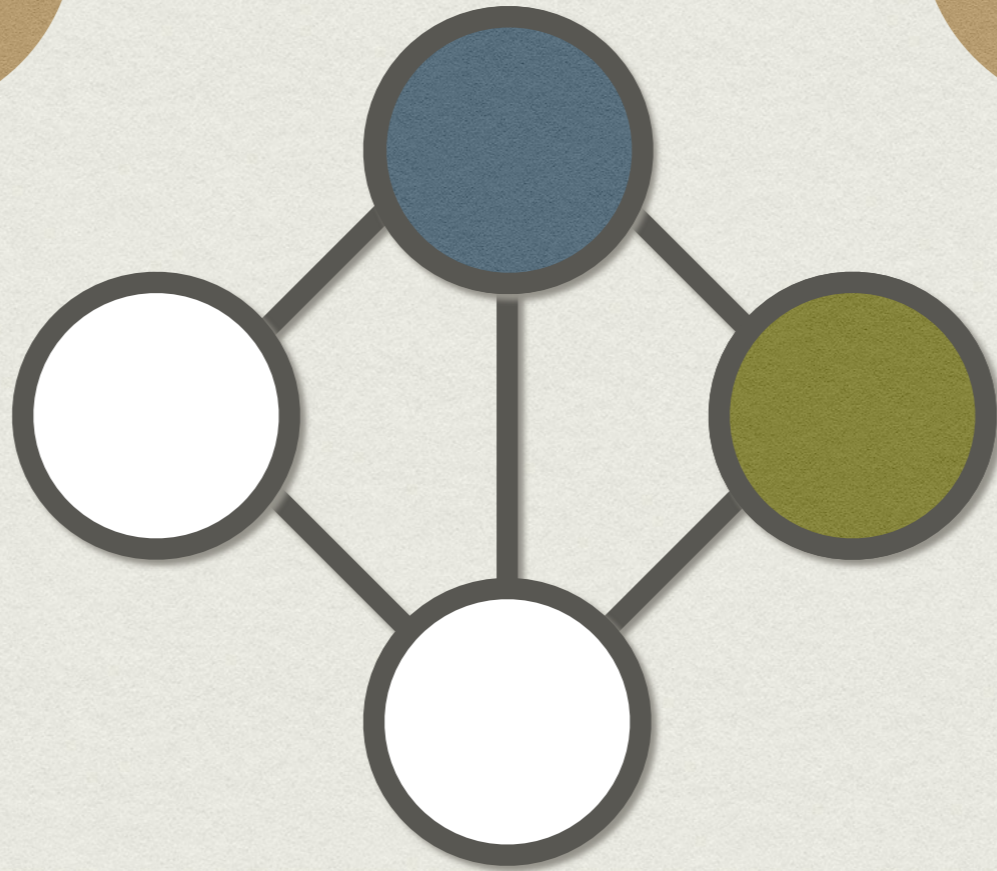
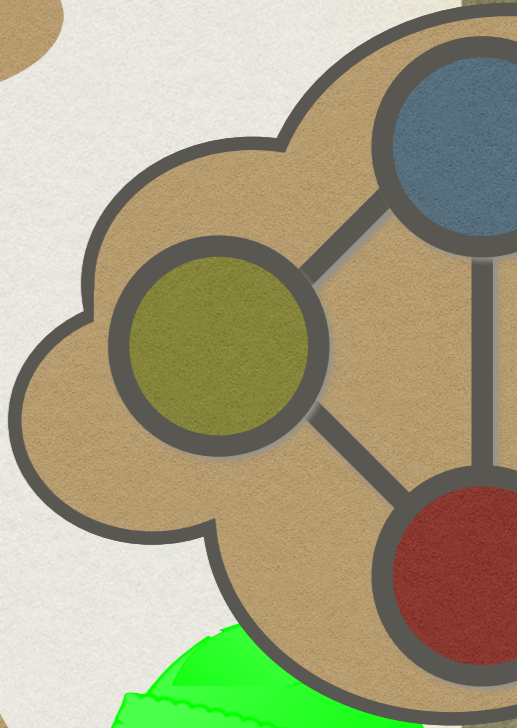
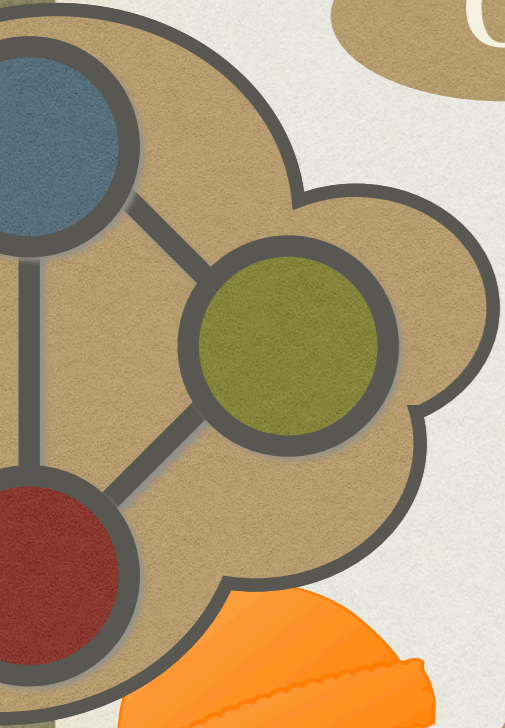


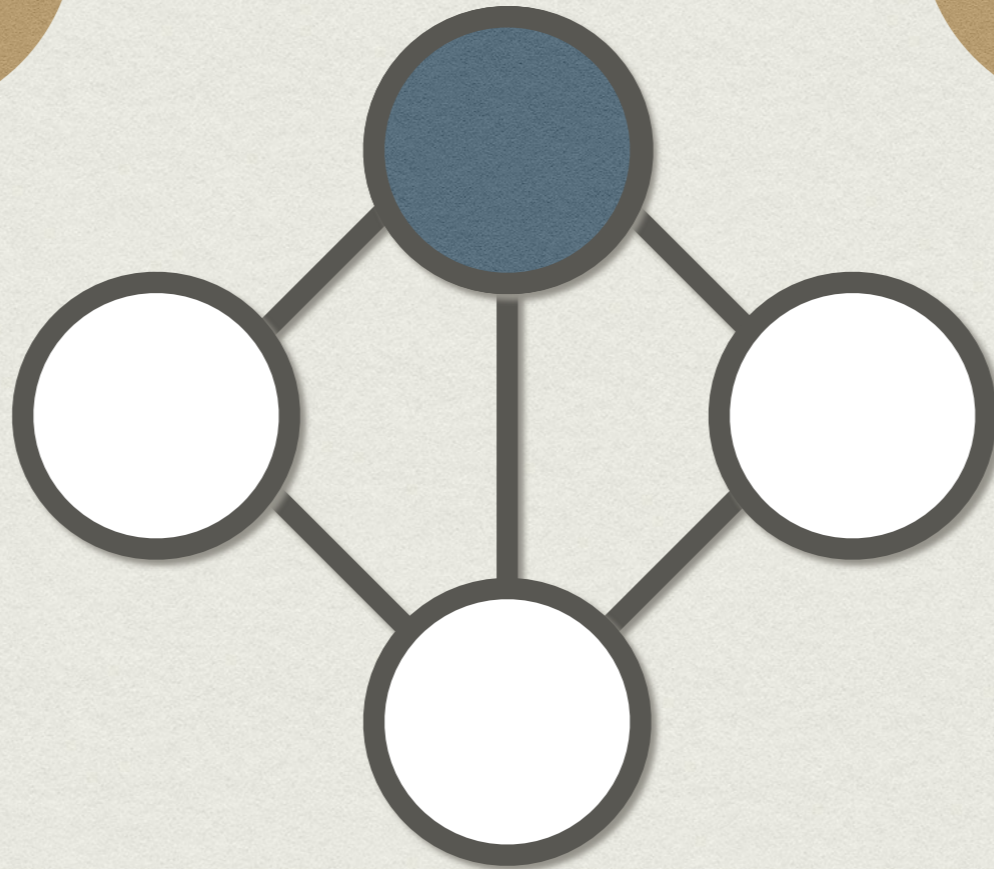
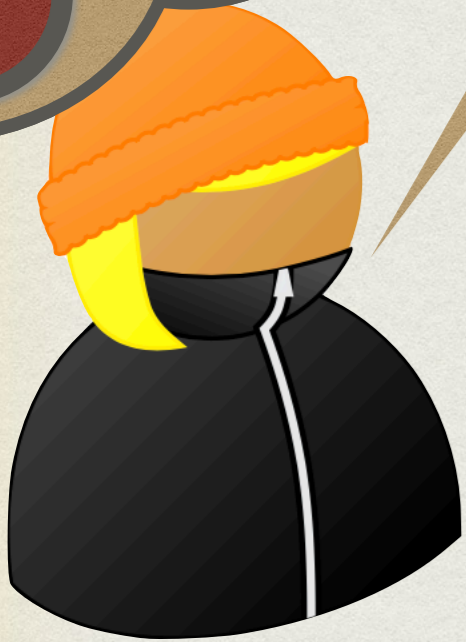
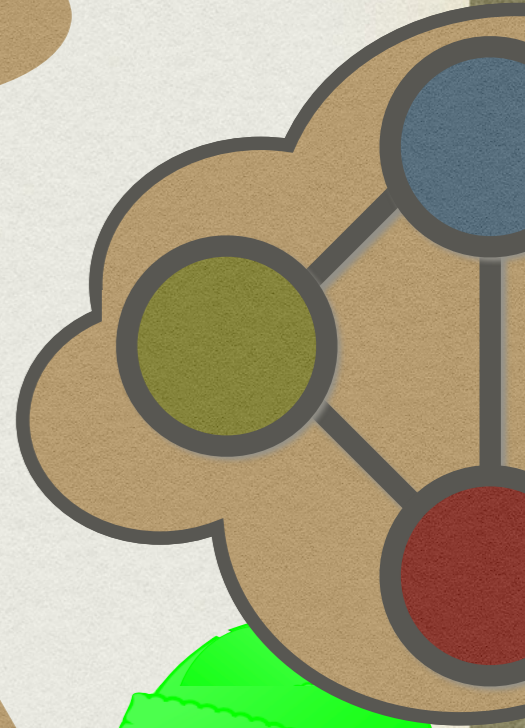
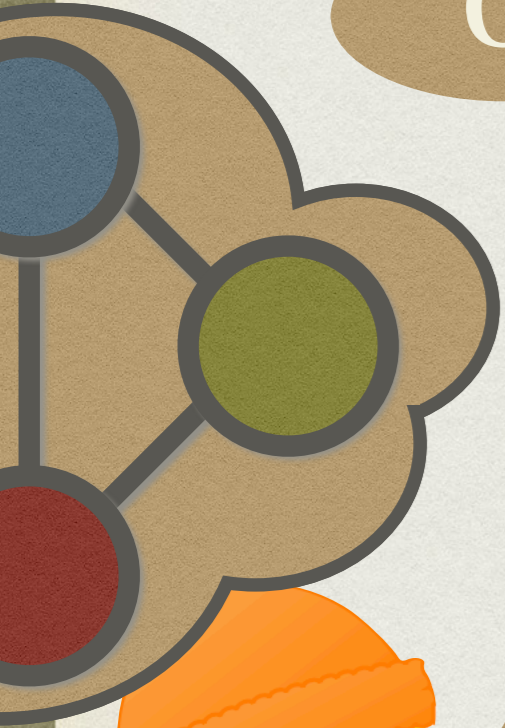
**TRANSFÉRABLE**

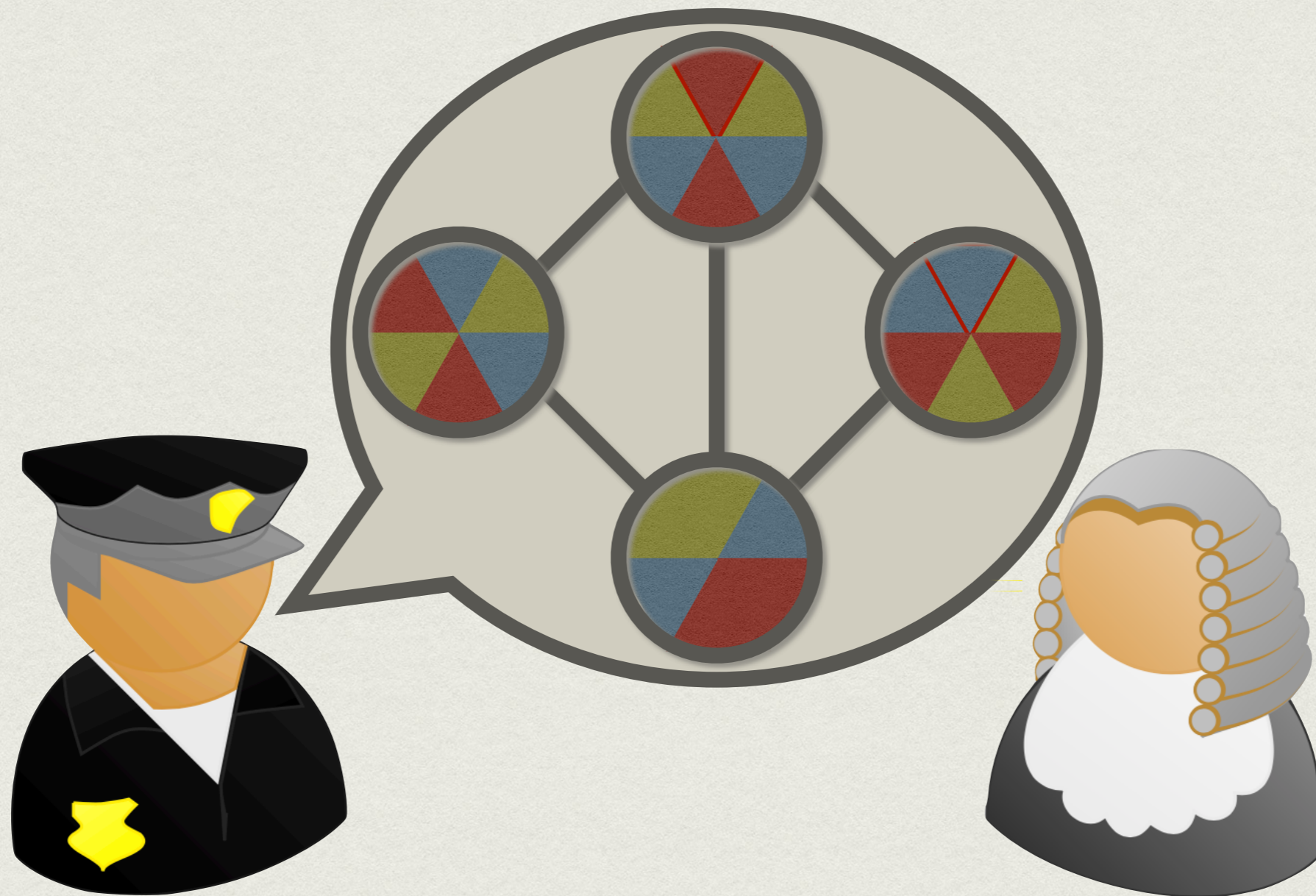


0

2





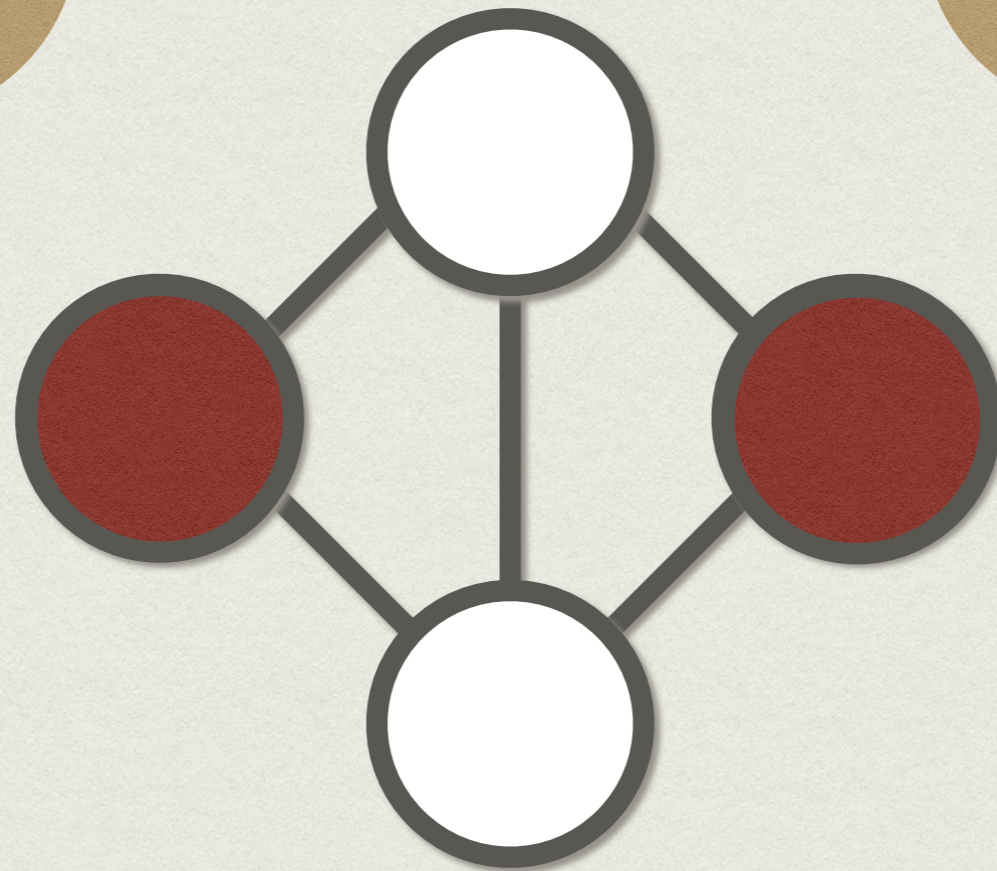
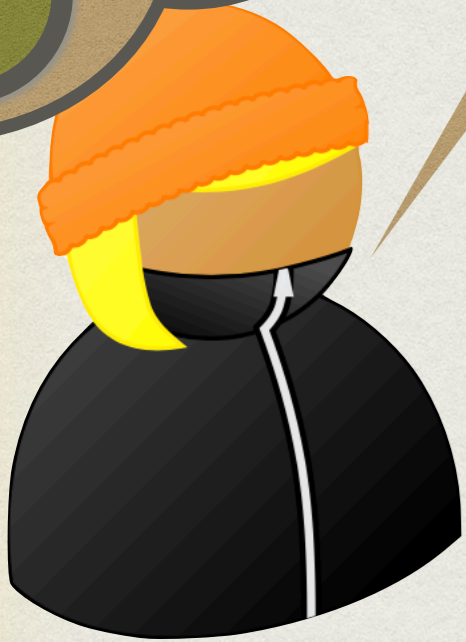
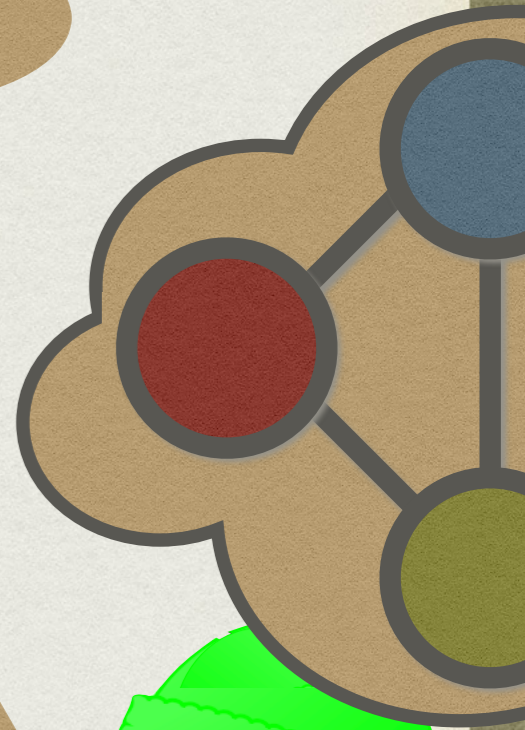
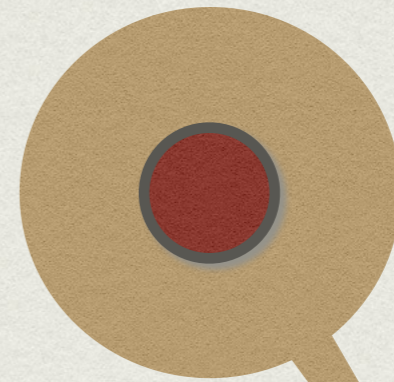
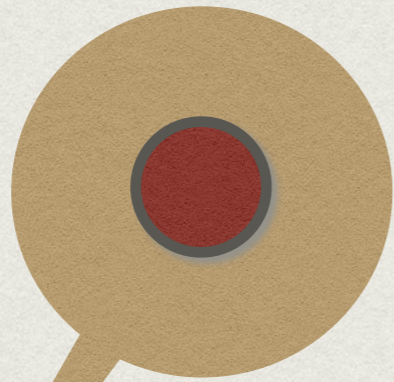
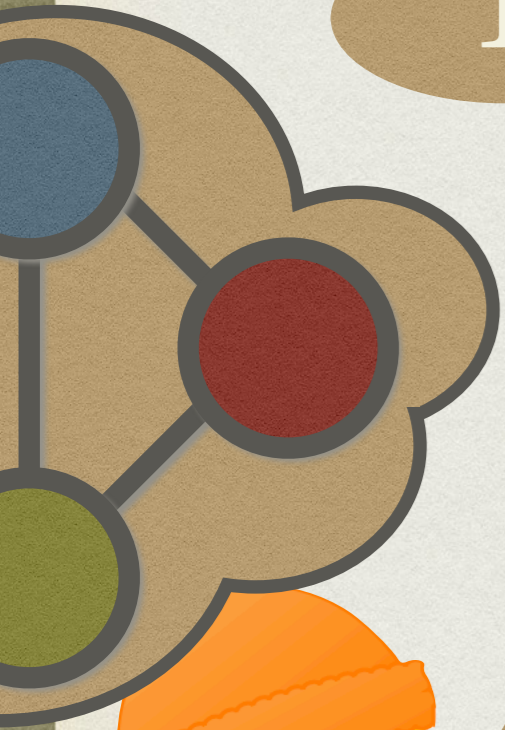


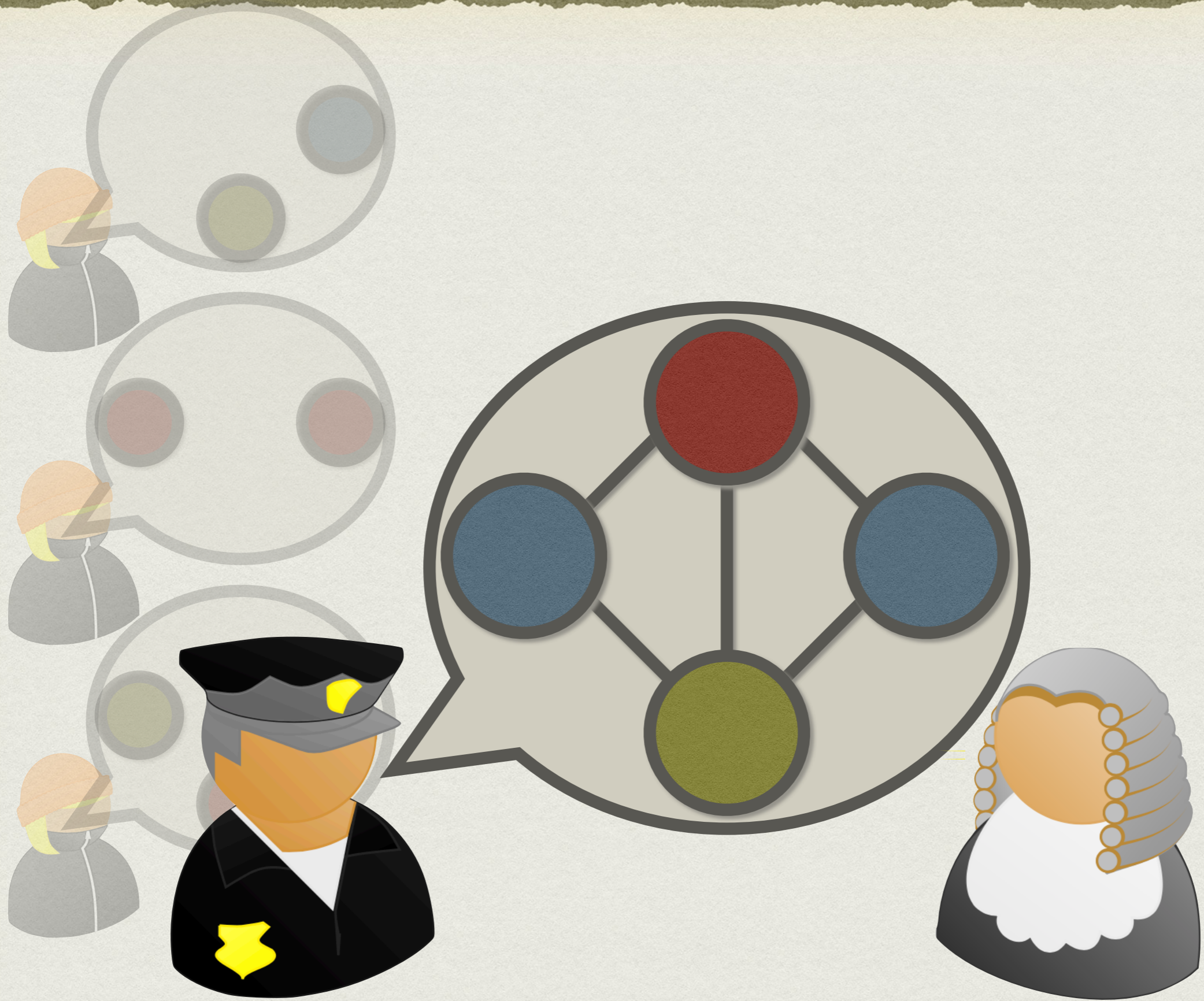
**ZK À VÉRIFICATEUR-HONÊTE**



1

2

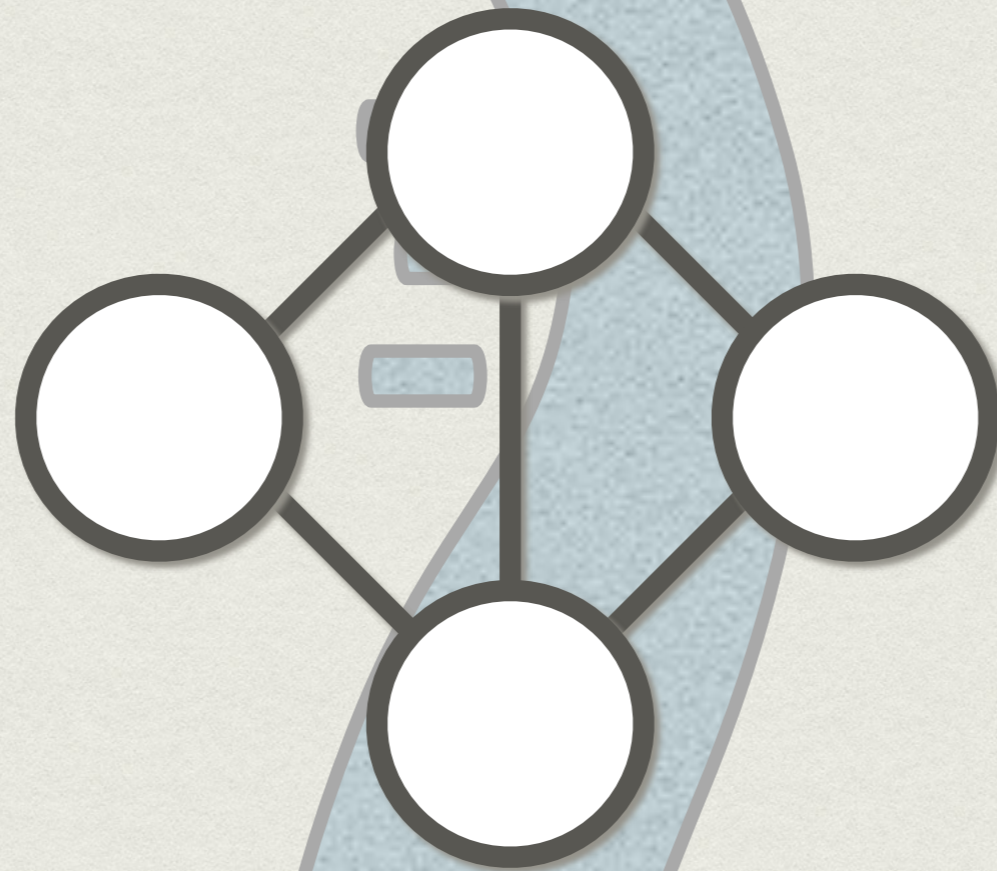
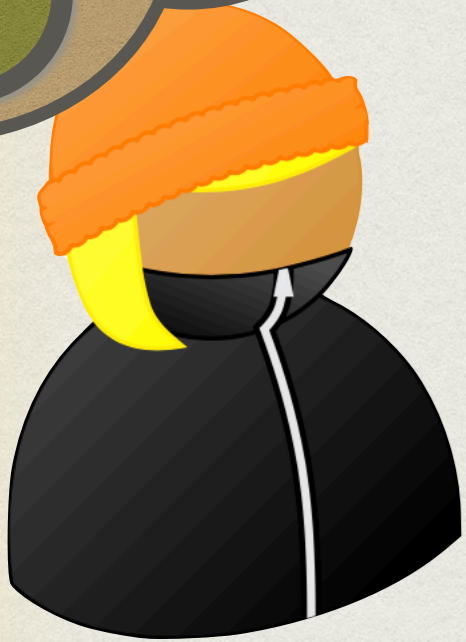
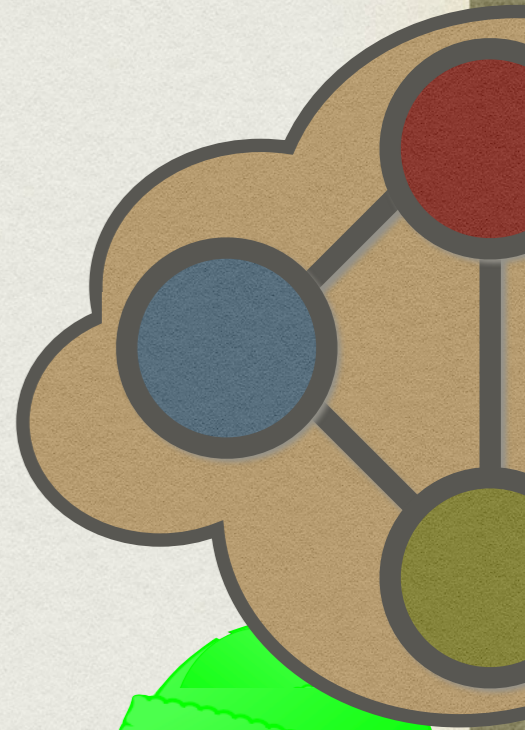
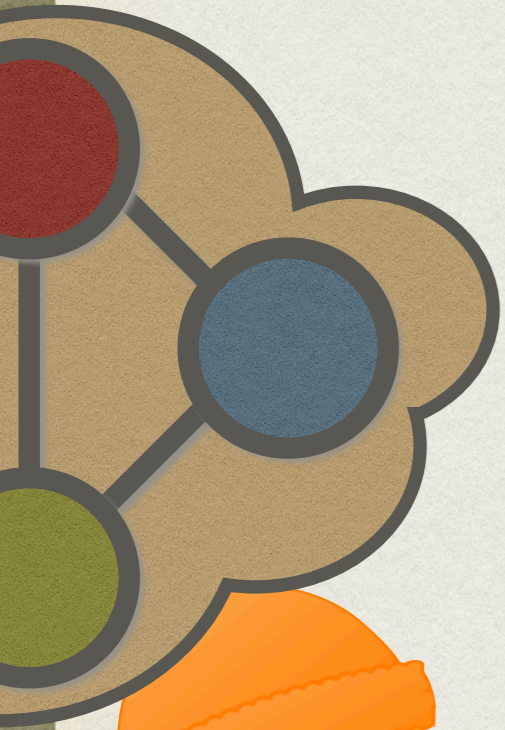




**TRANSFÉRABLE**

# IDÉE NOUVELLE

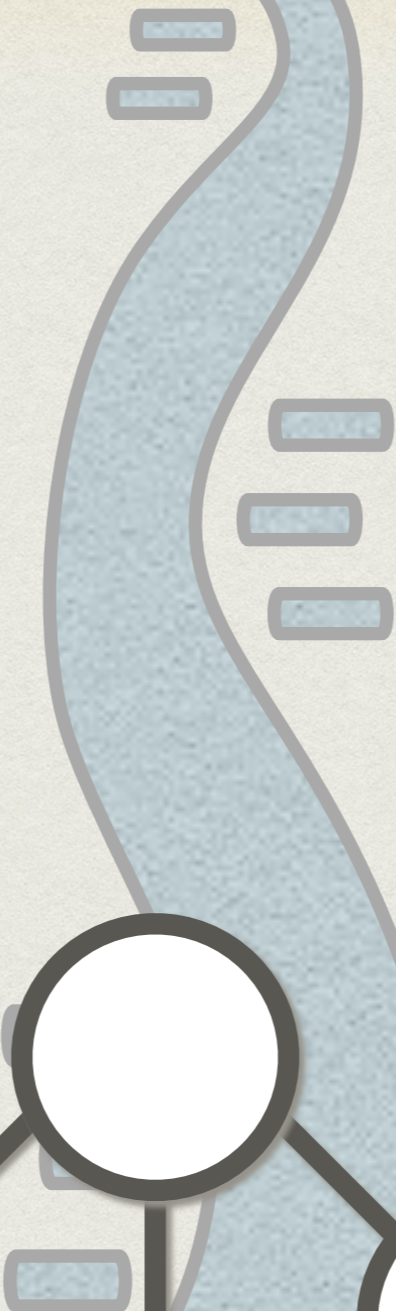
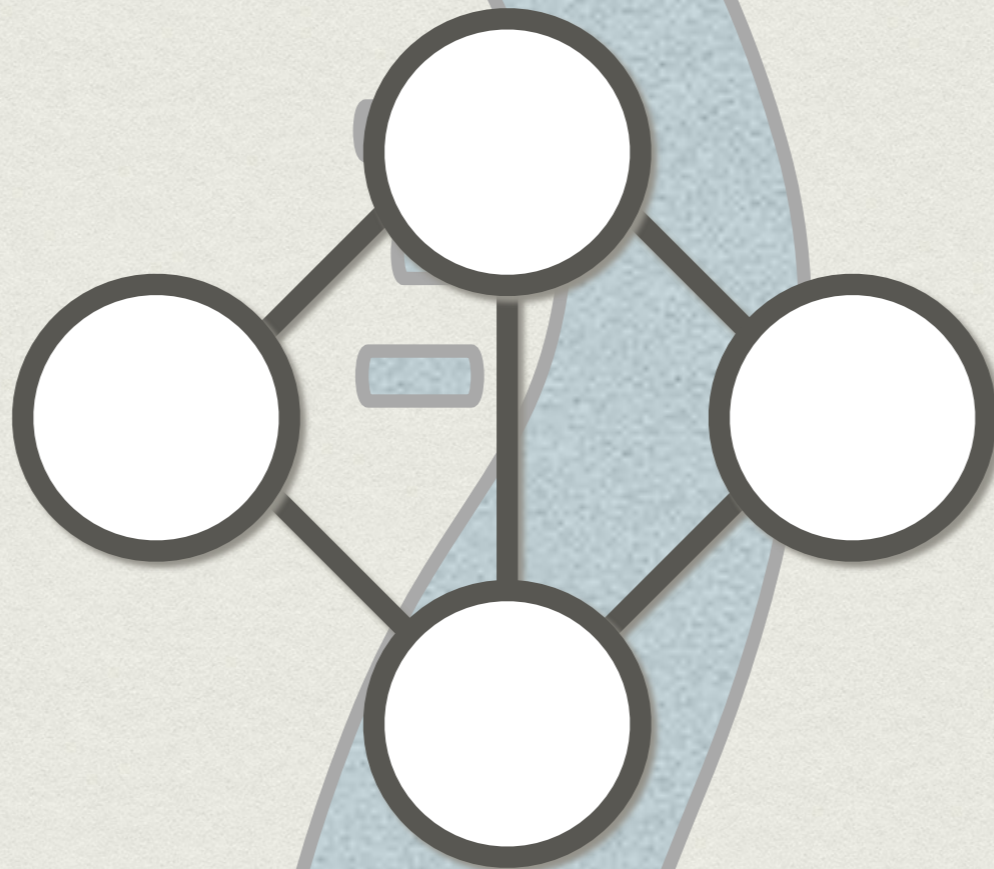
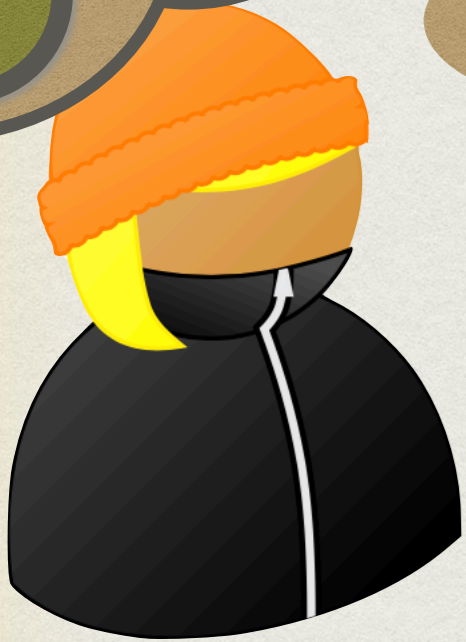
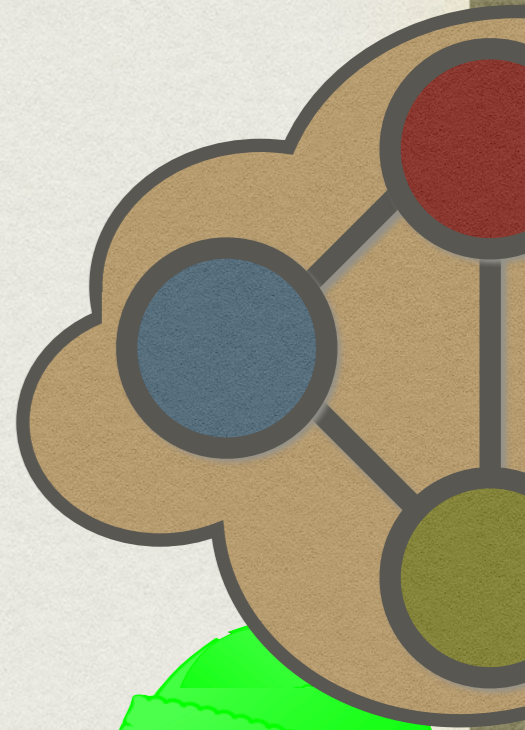
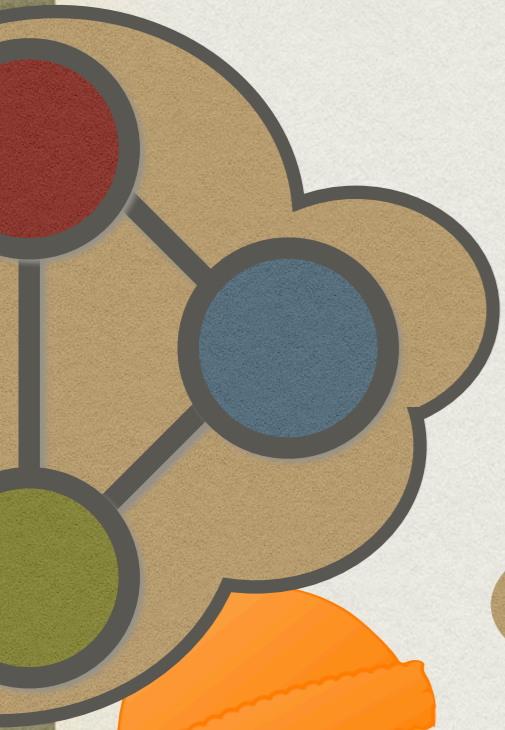
*(ZK)MIPs*

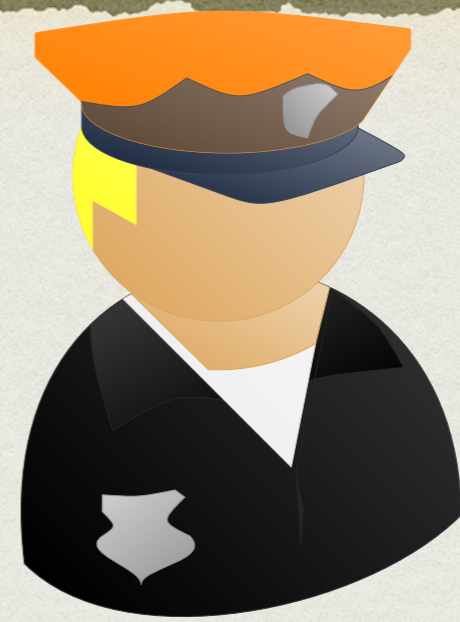




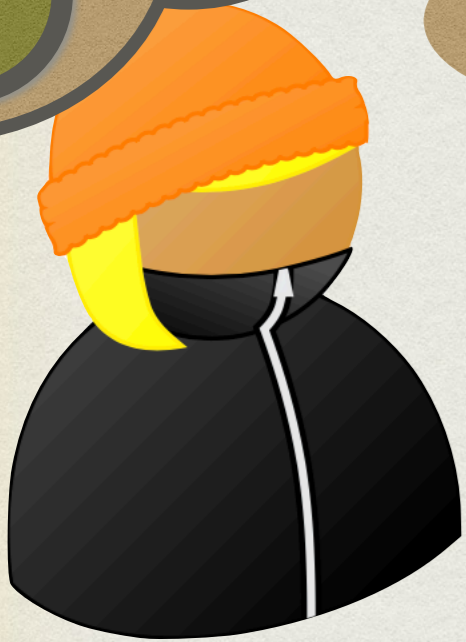
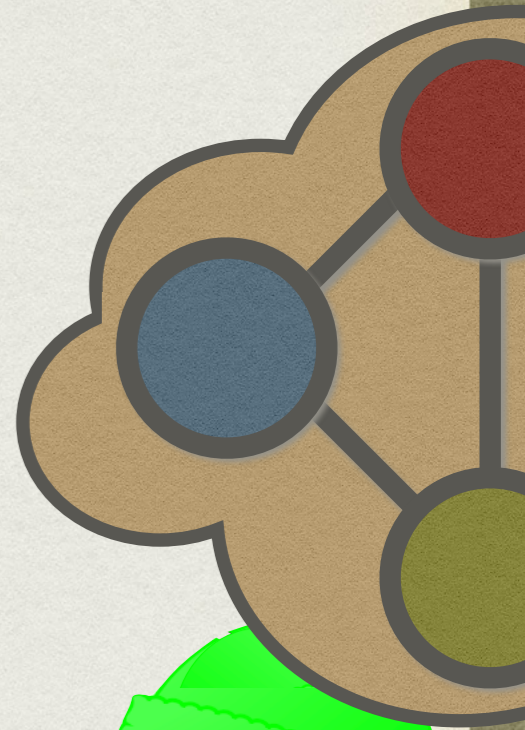
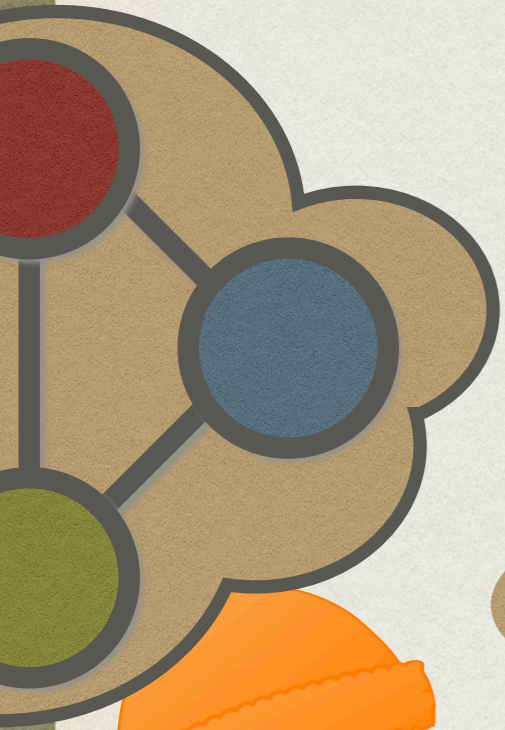
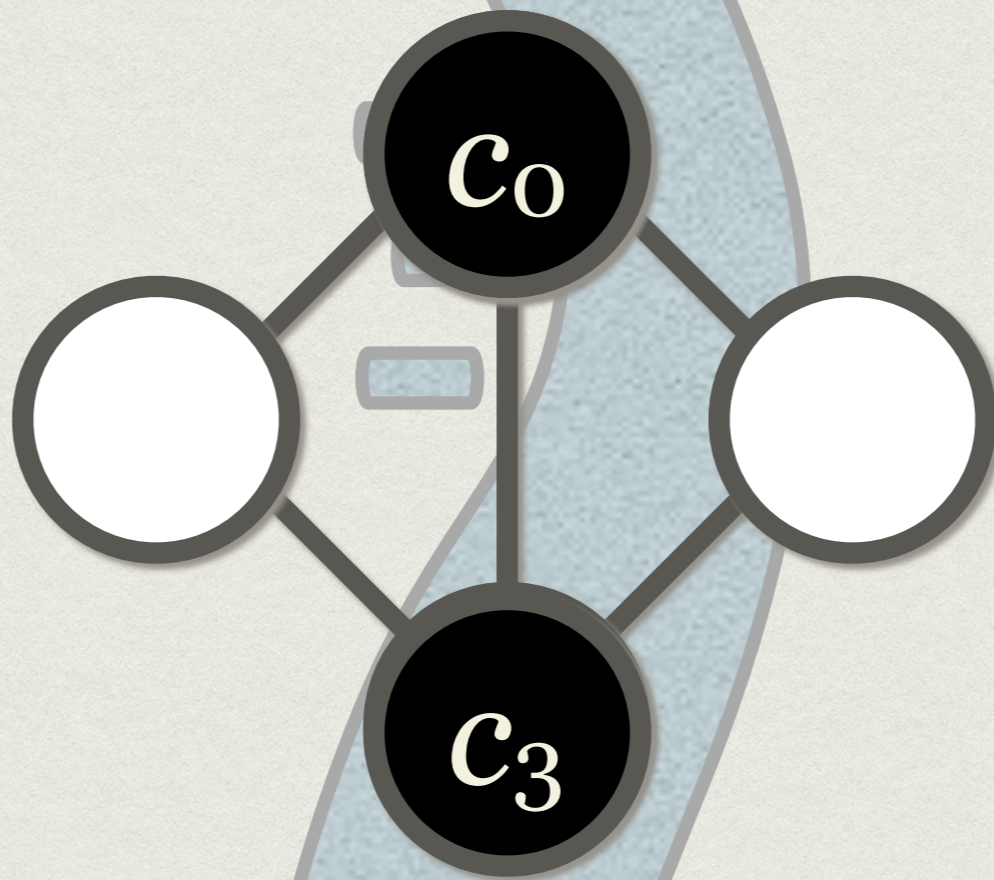


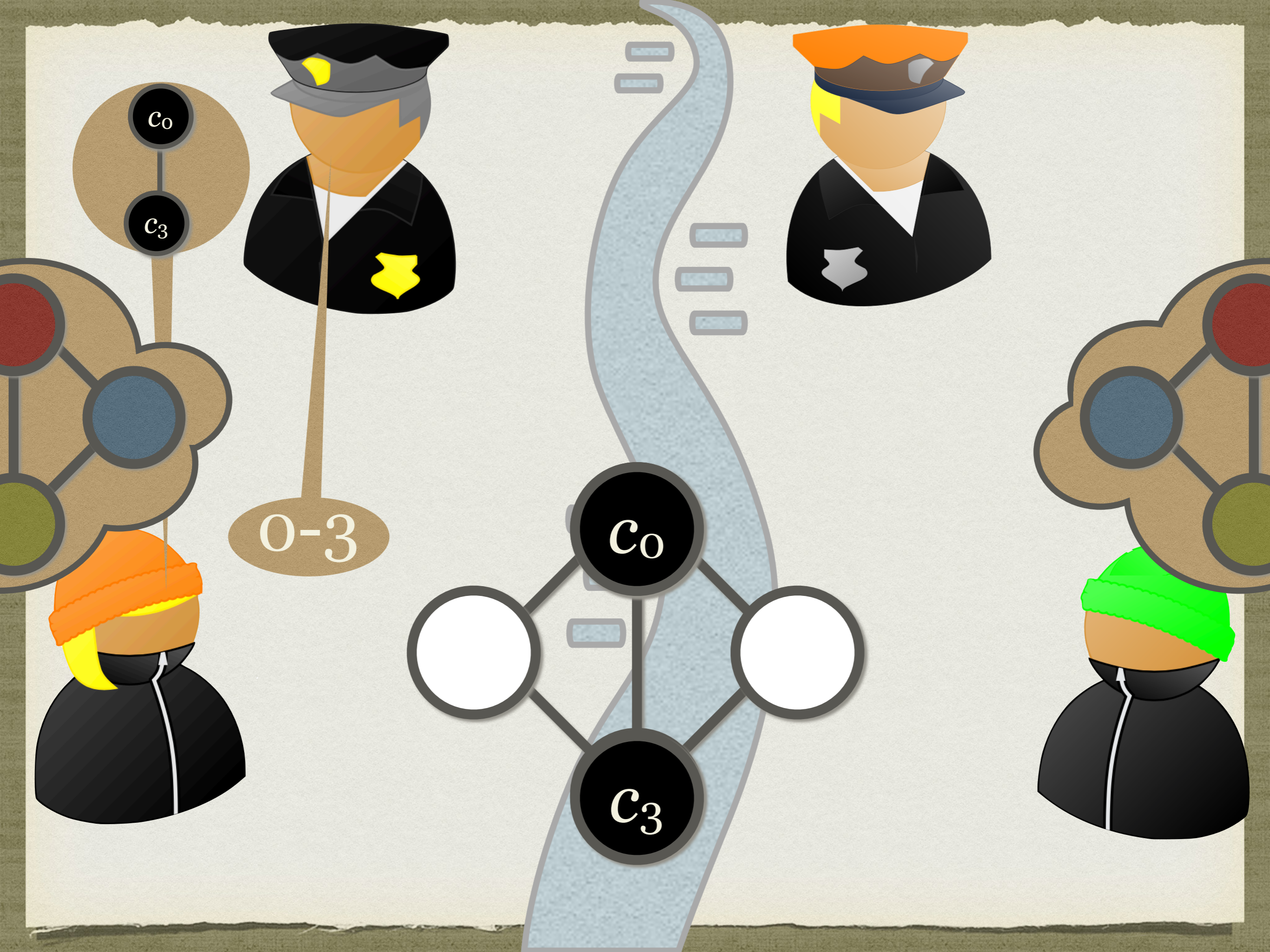
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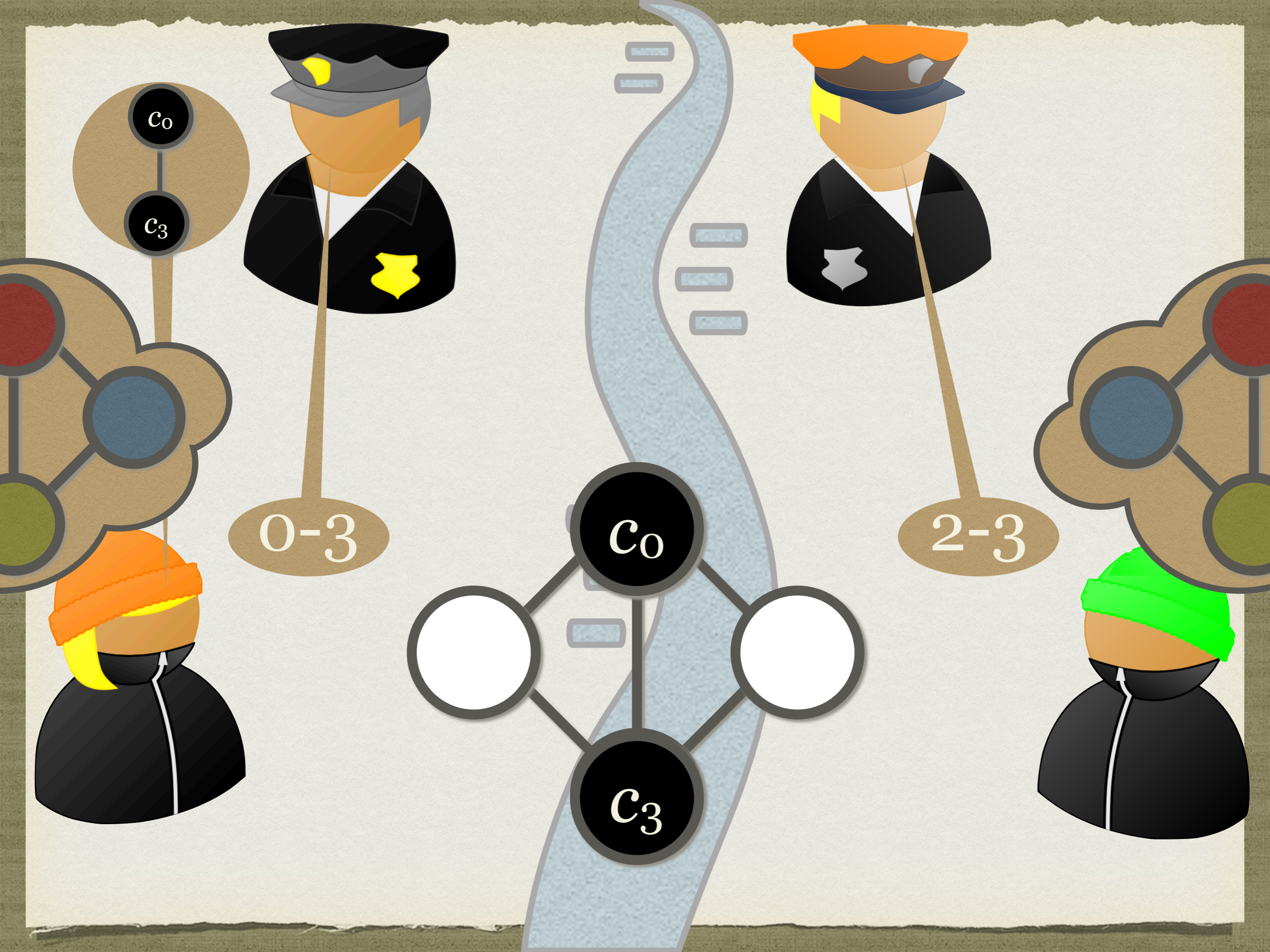


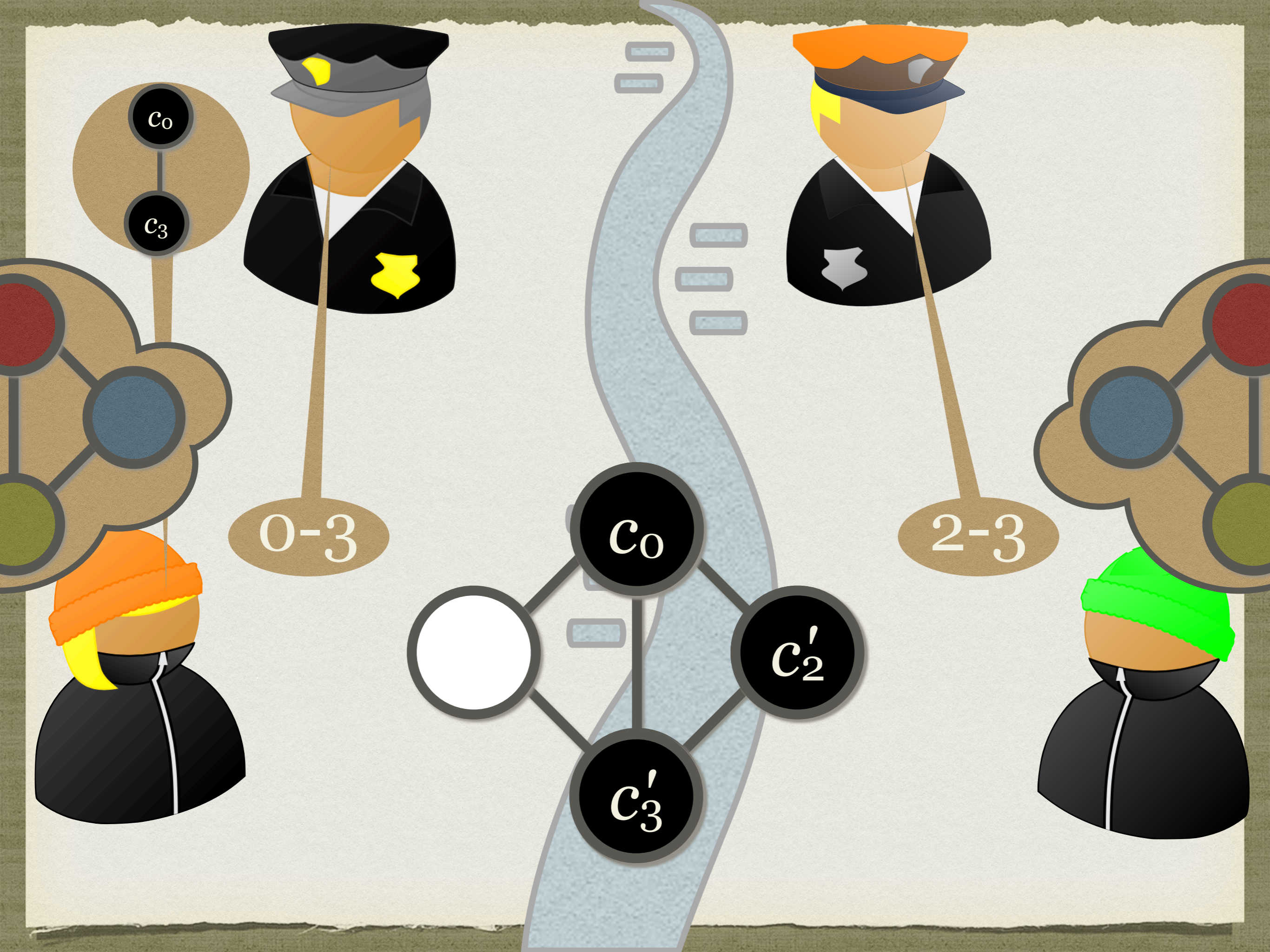


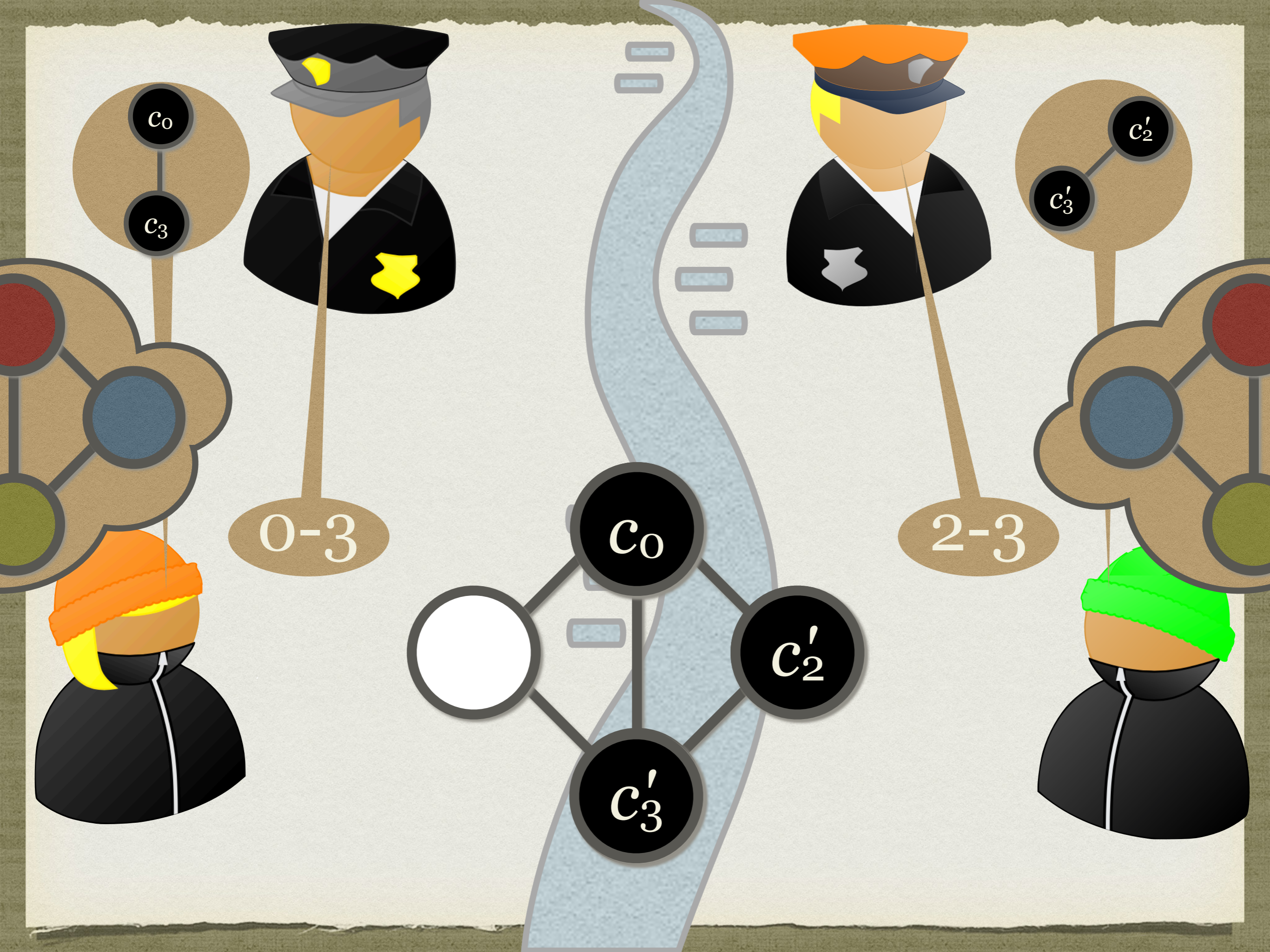
0-3



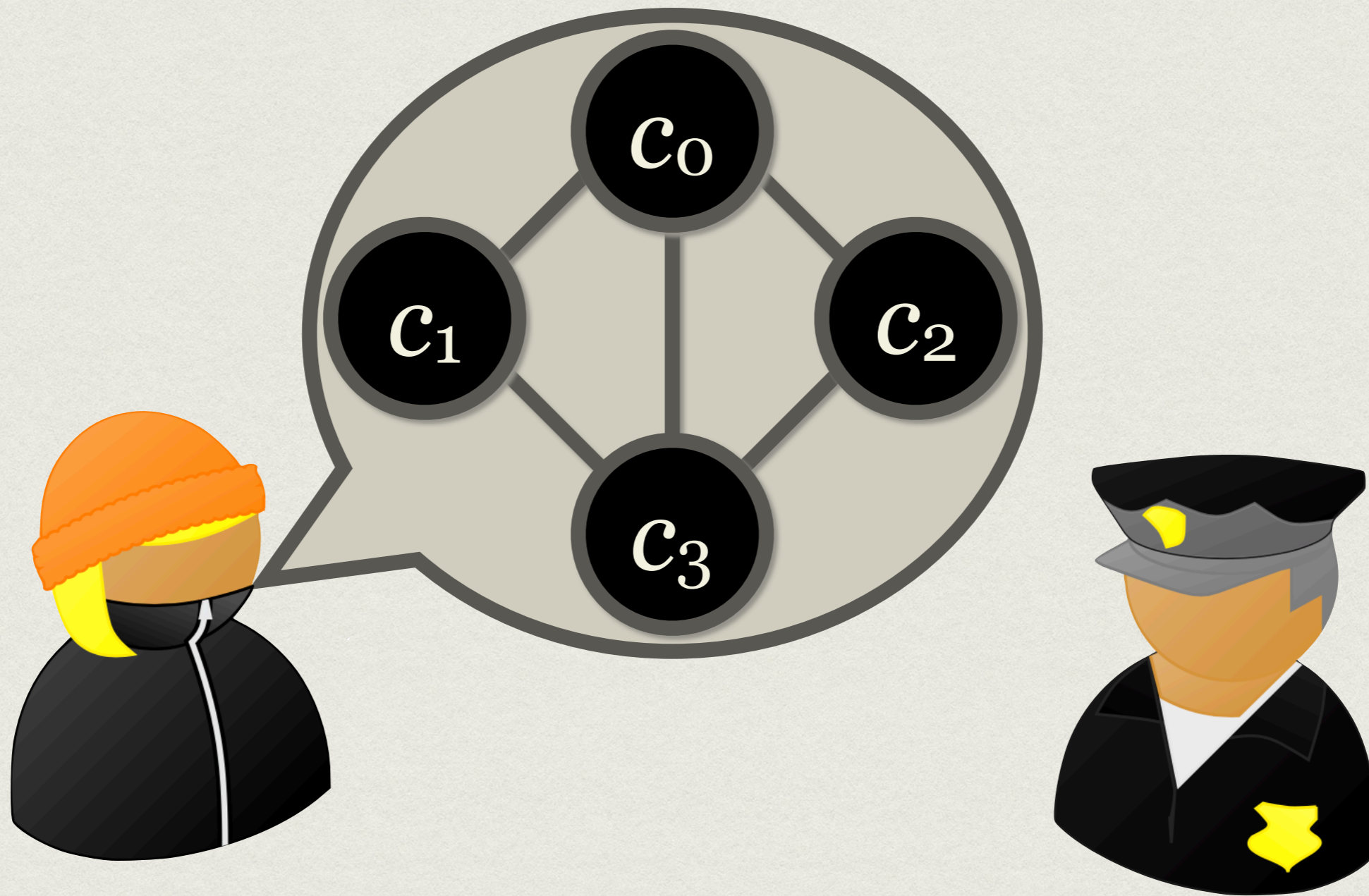








# MISE-EN-GAGE ??

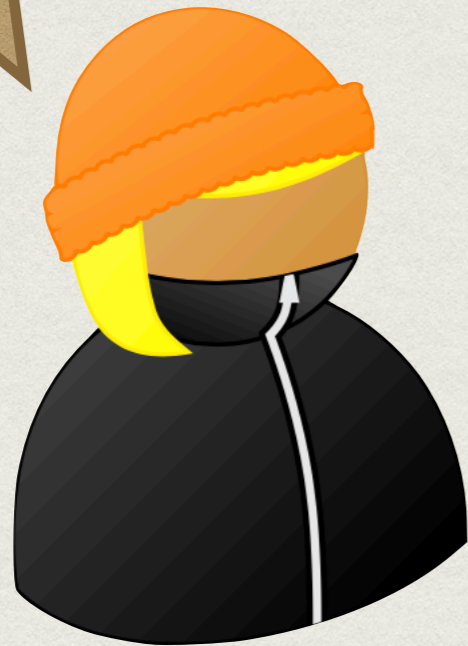


# MISE-EN-GAGE

$r \neq 0$



$b$

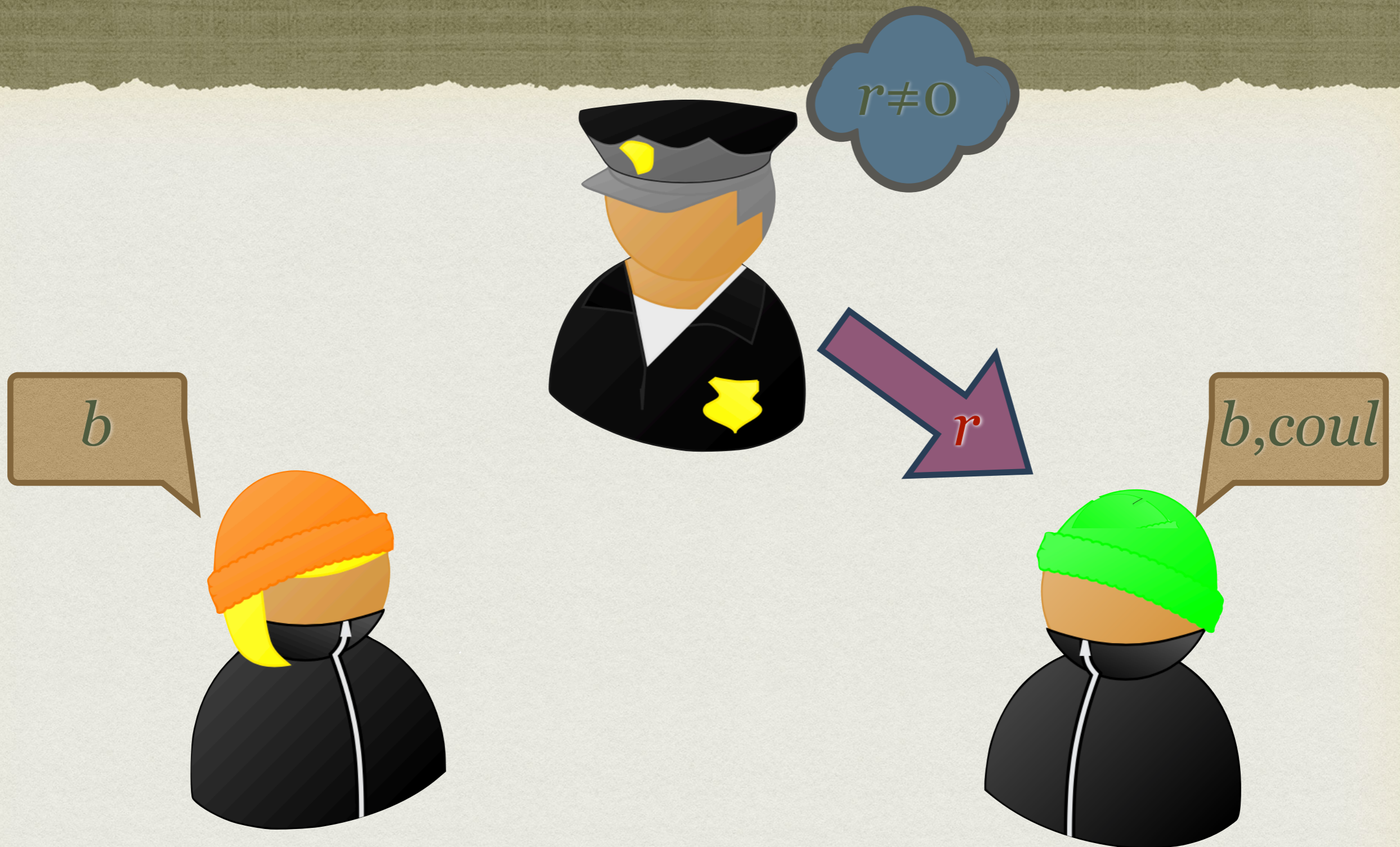


$b, coul$

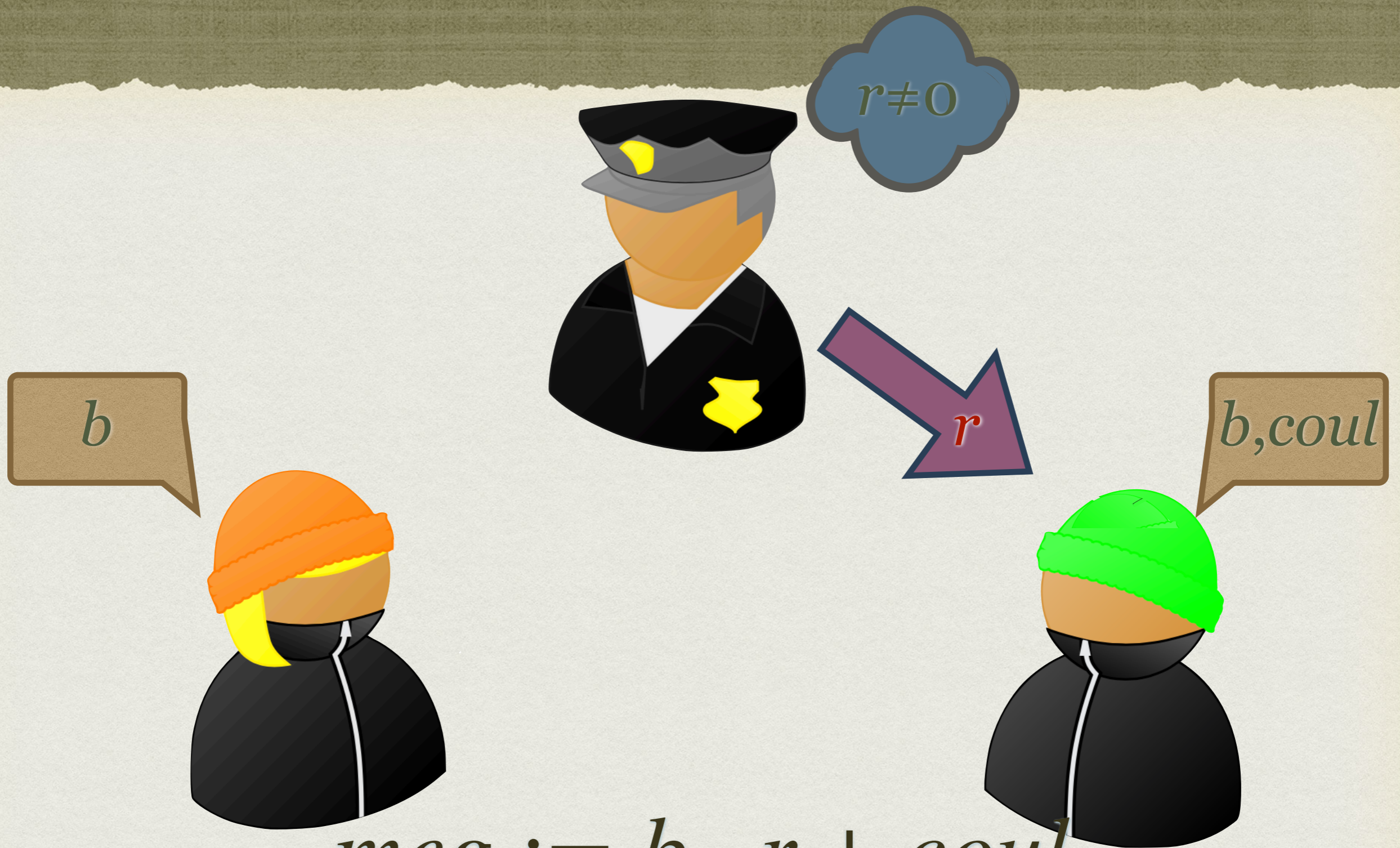




# MISE-EN-GAGE

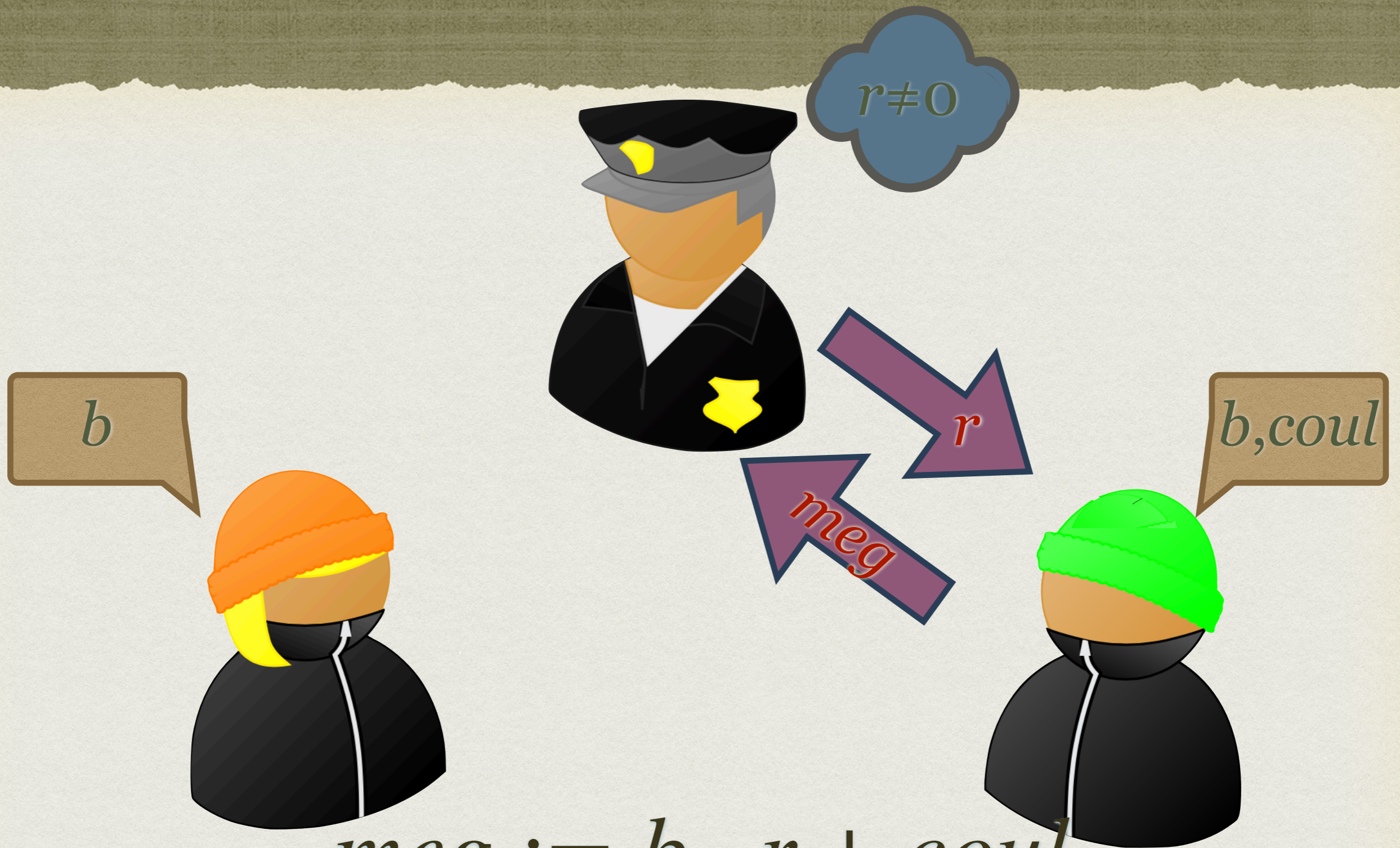


# MISE-EN-GAGE



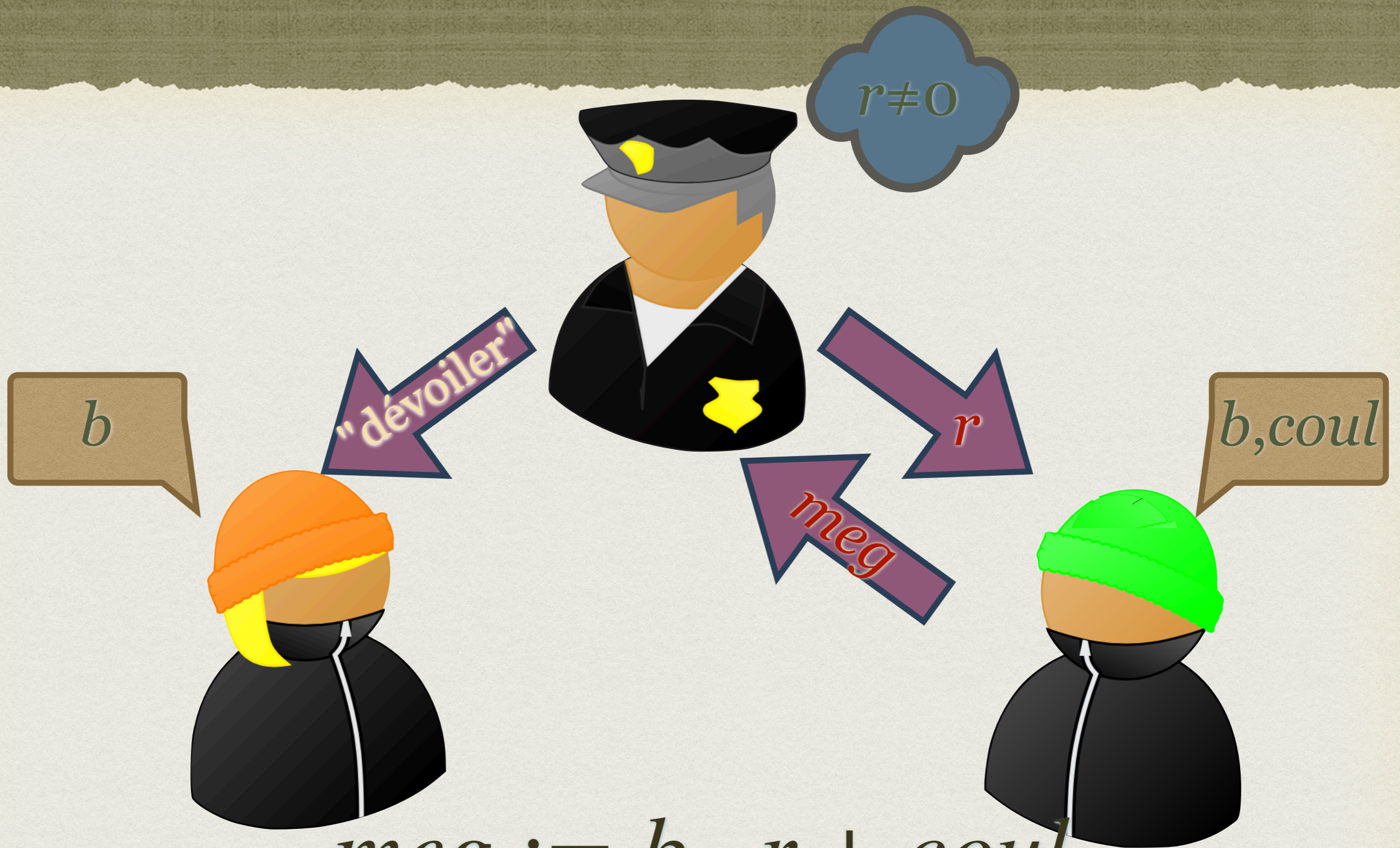
$$meg := b \cdot r + coul$$

# MISE-EN-GAGE



$$meg := b \cdot r + coul$$

# MISE-EN-GAGE



$$meg := b \cdot r + coul$$

# MISE-EN-GAGE



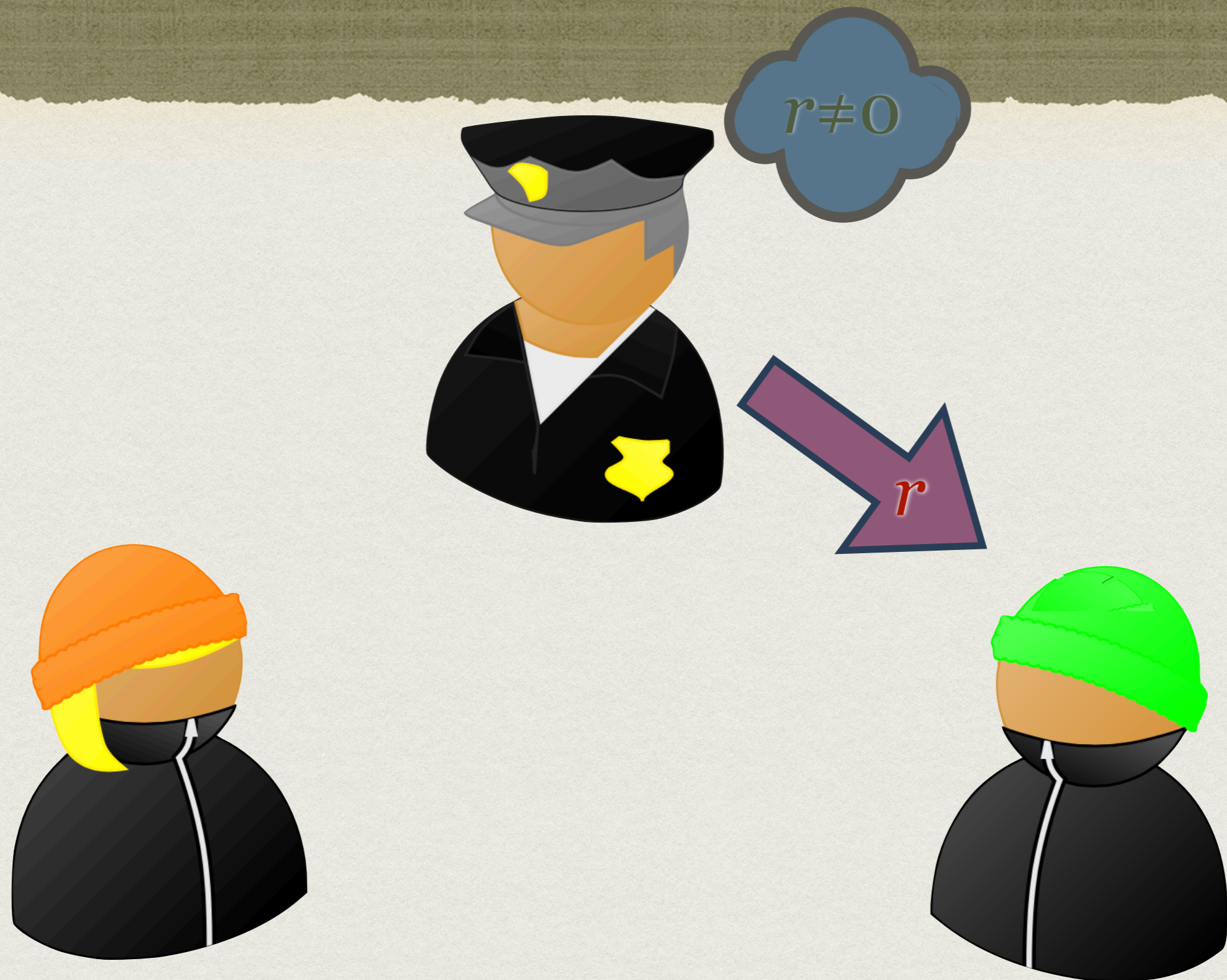
$$meg := b \cdot r + coul$$

# MISE-EN-GAGE

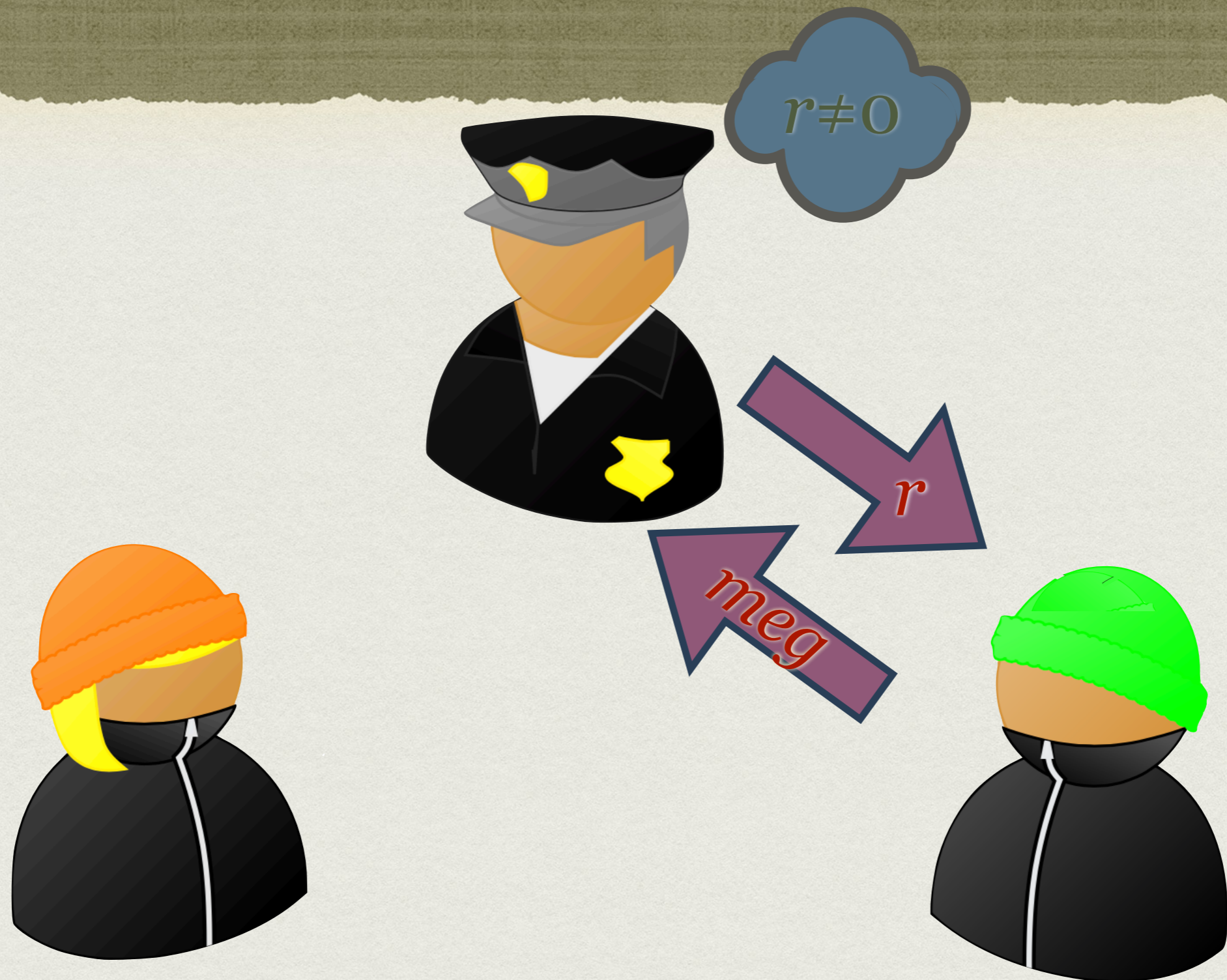
$r \neq 0$



# MISE-EN-GAGE

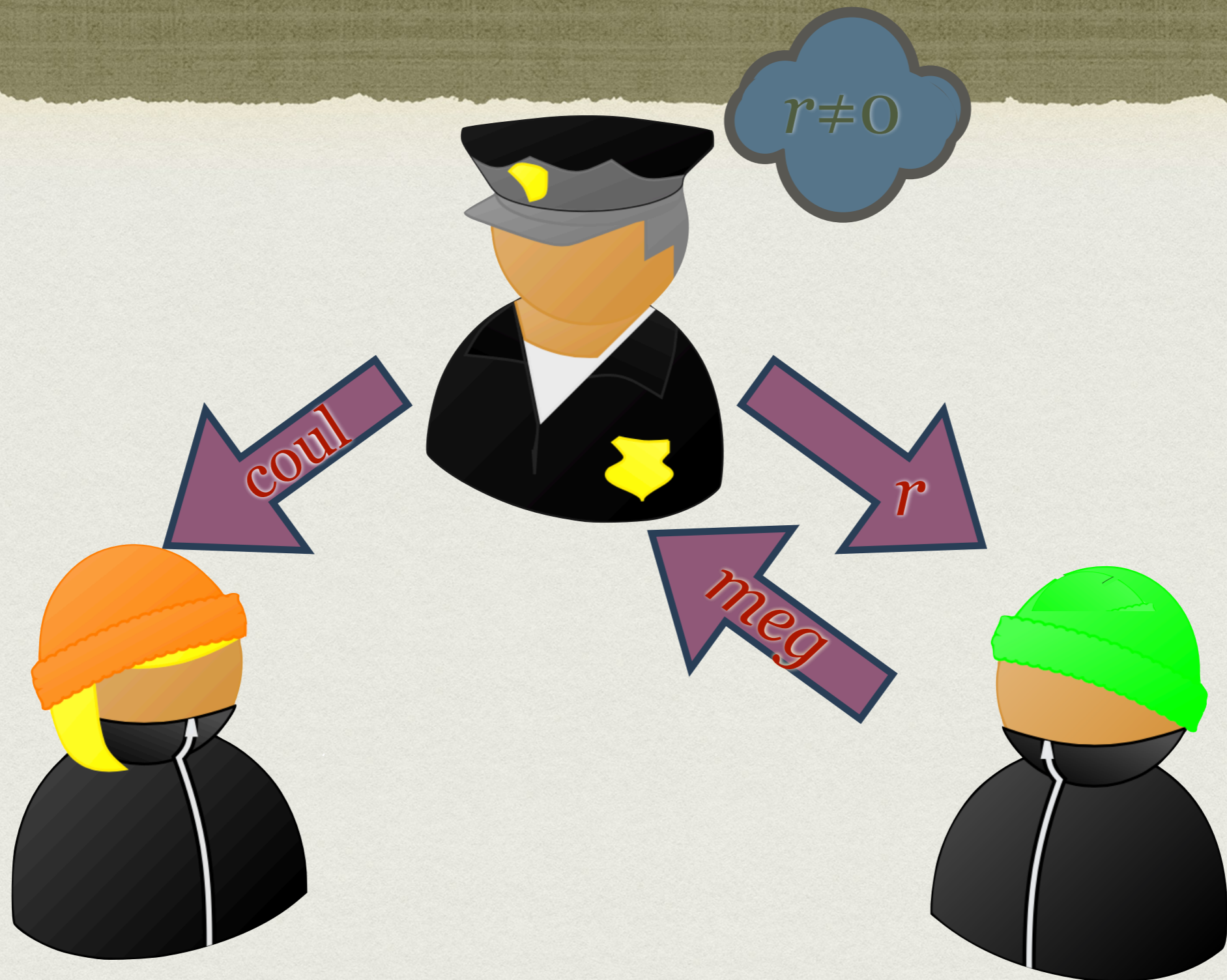


# MISE-EN-GAGE

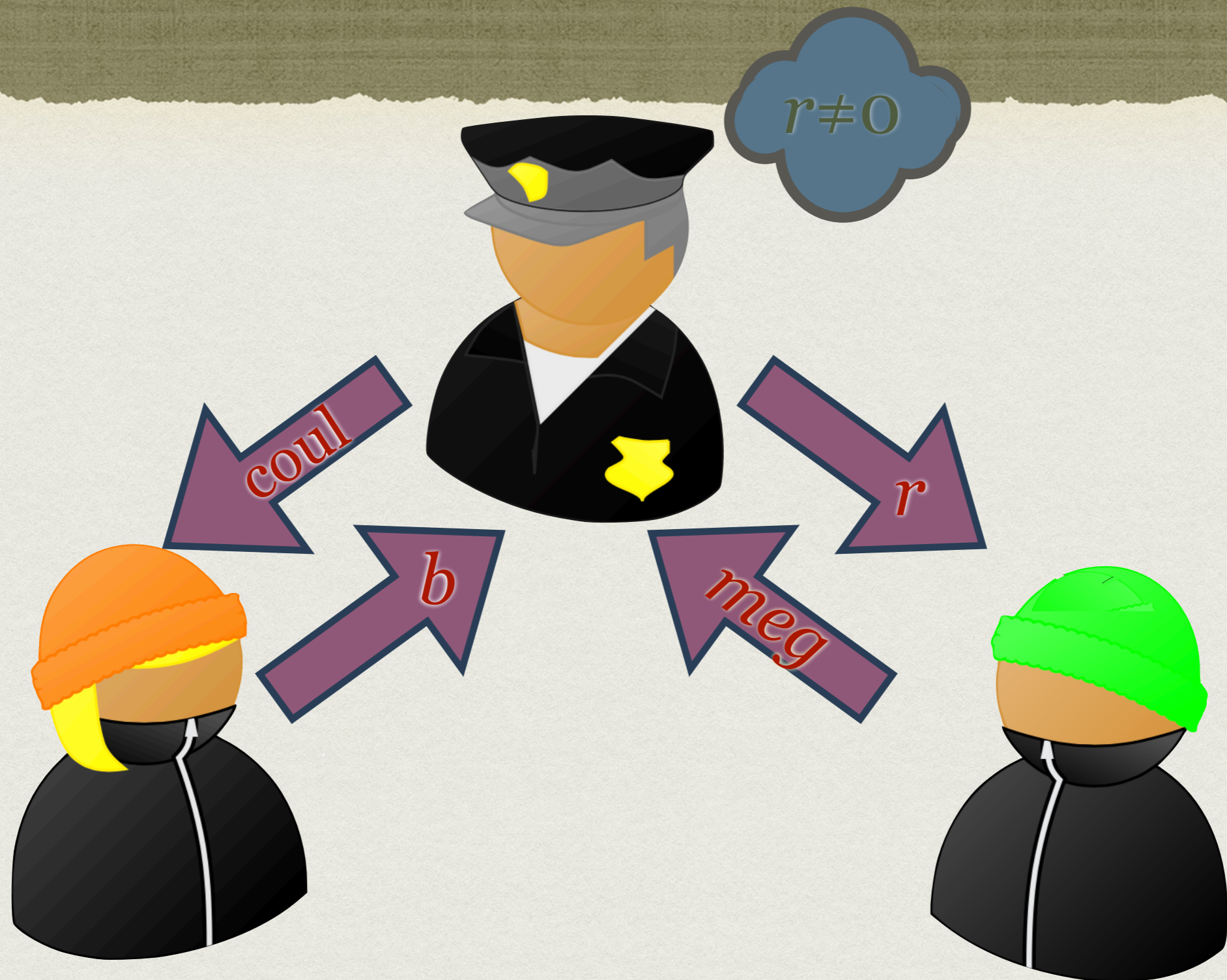




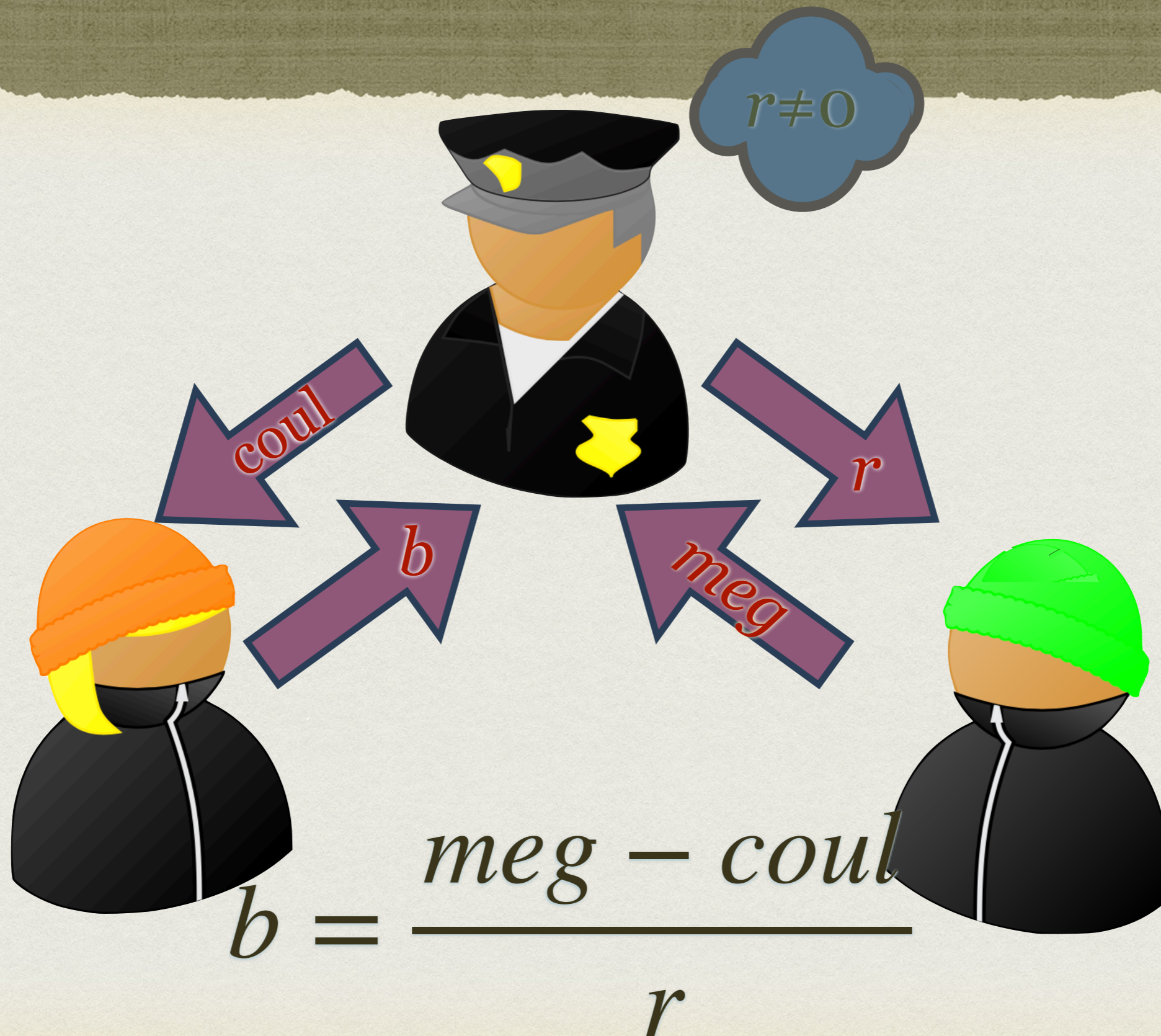
# MISE-EN-GAGE



# MISE-EN-GAGE



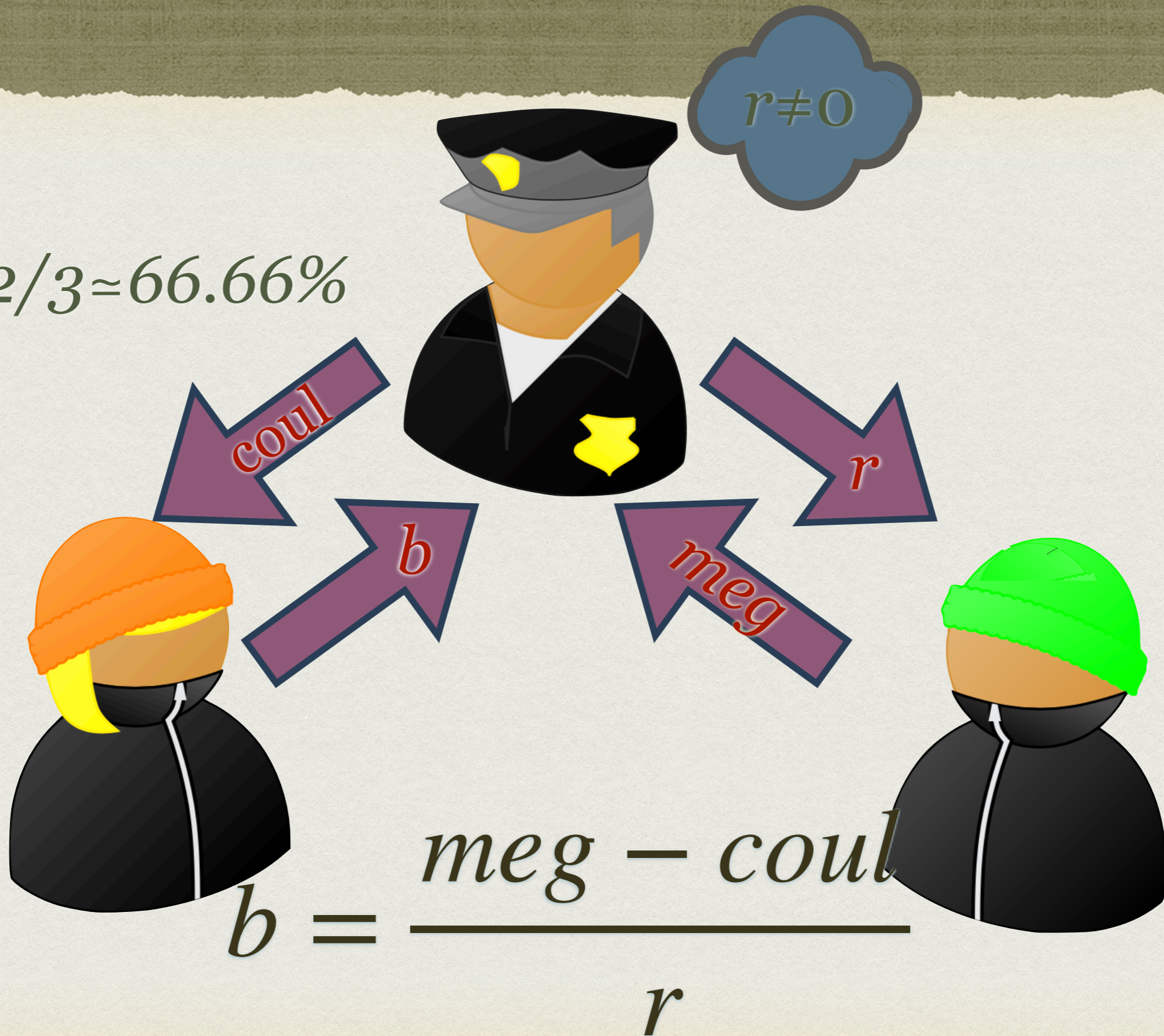
# MISE-EN-GAGE



# MISE-EN-GAGE

$r \neq 0$

$LOC = 2/3 \approx 66.66\%$



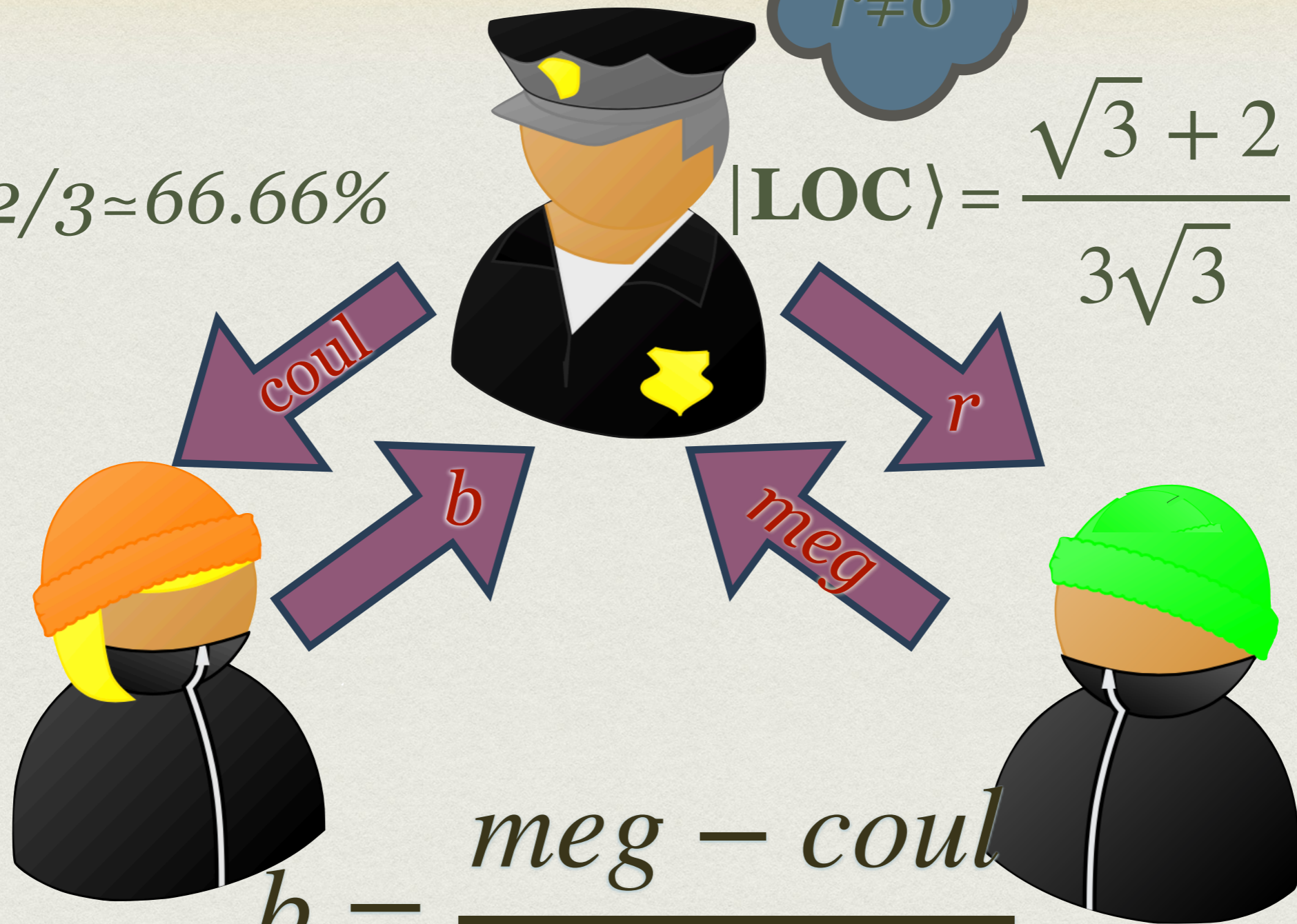
$$b = \frac{meg - coul}{r}$$

# MISE-EN-GAGE

$r \neq 0$

$$\text{LOC} = 2/3 \approx 66.66\%$$

$$|\text{LOC}\rangle = \frac{\sqrt{3} + 2}{3\sqrt{3}} \approx 71,82\%$$



$$b = \frac{meg - coul}{r}$$

# MISE-EN-GAGE

$r \neq 0$



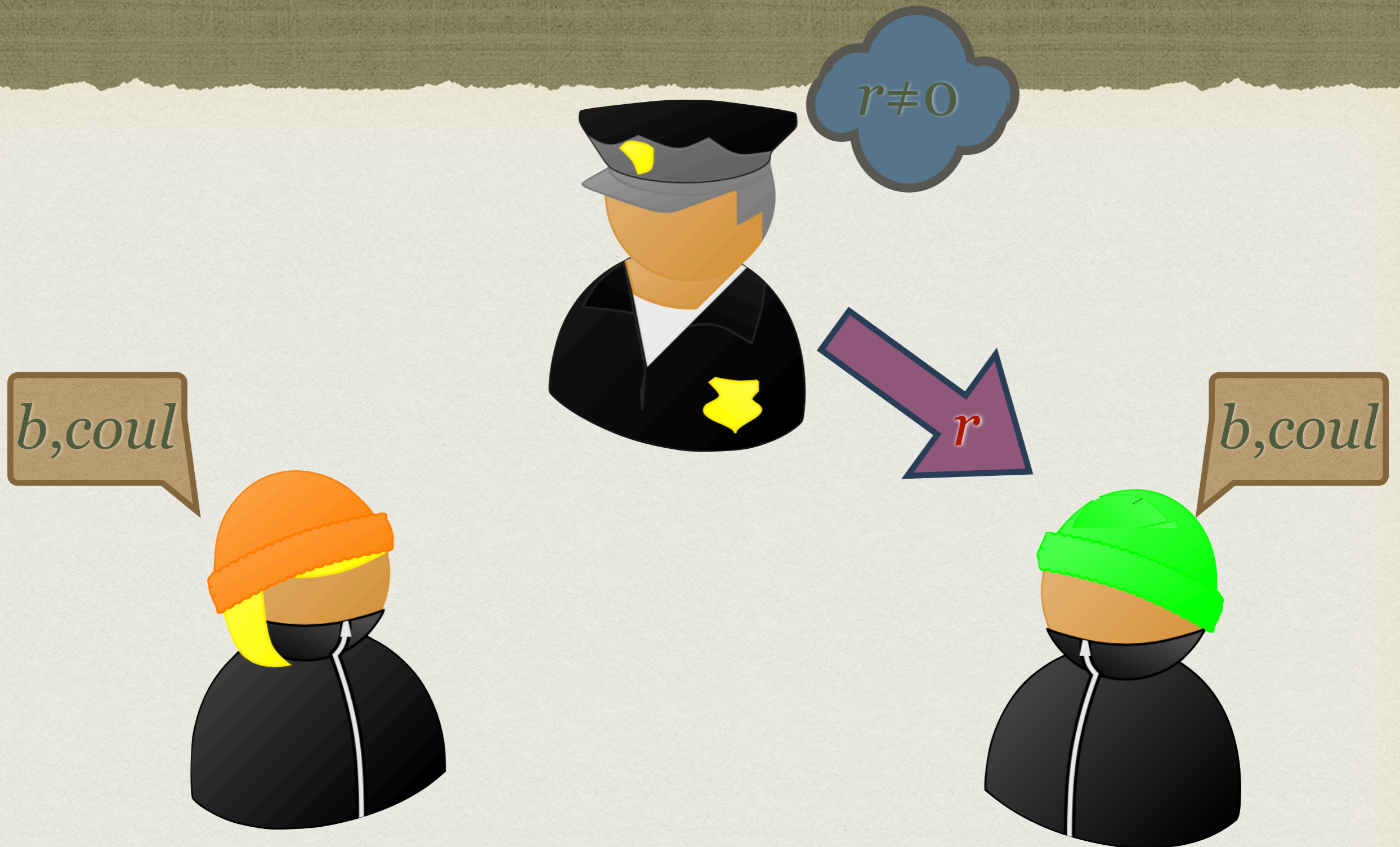
*b, coul*



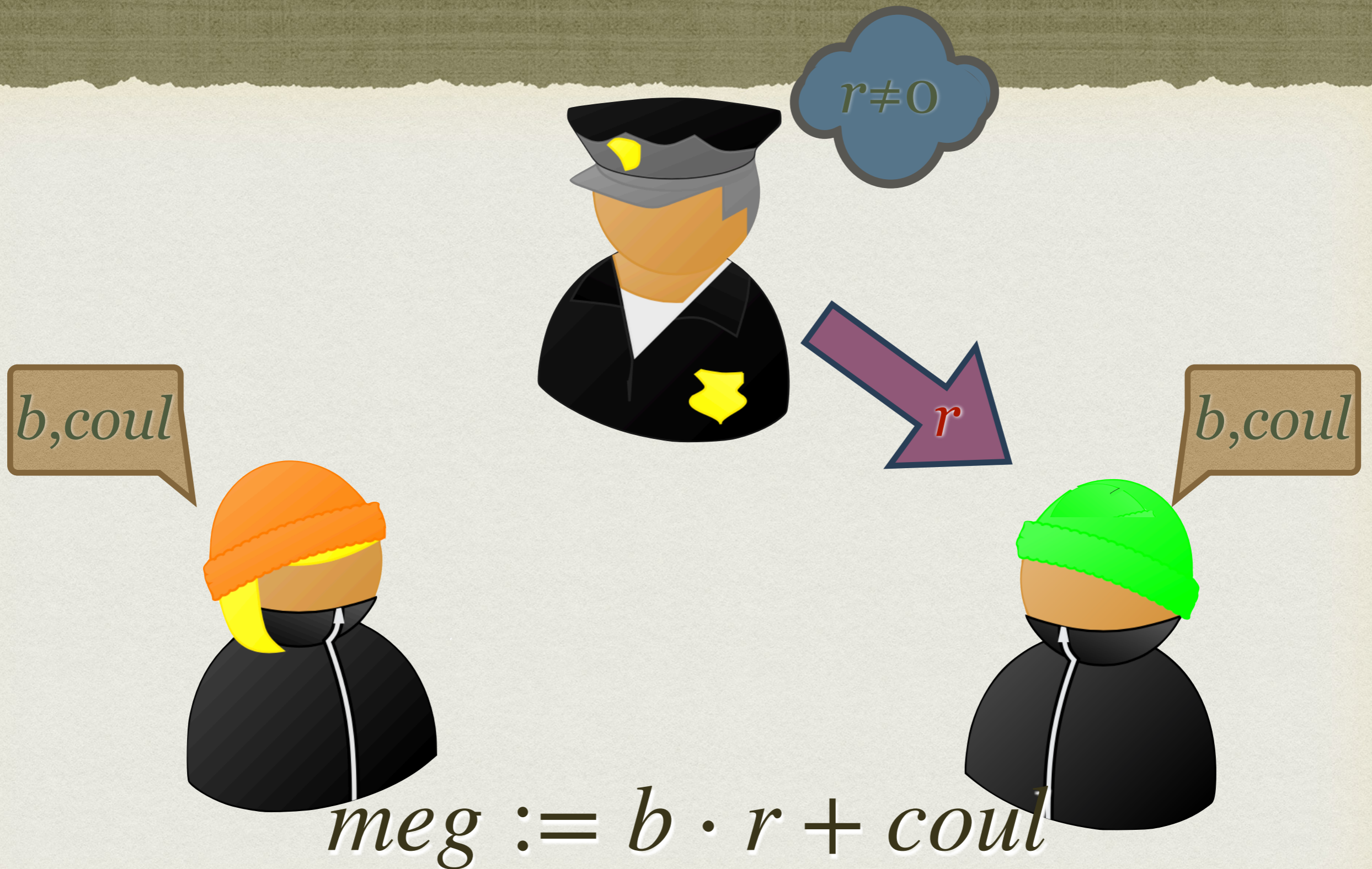
*b, coul*



# MISE-EN-GAGE

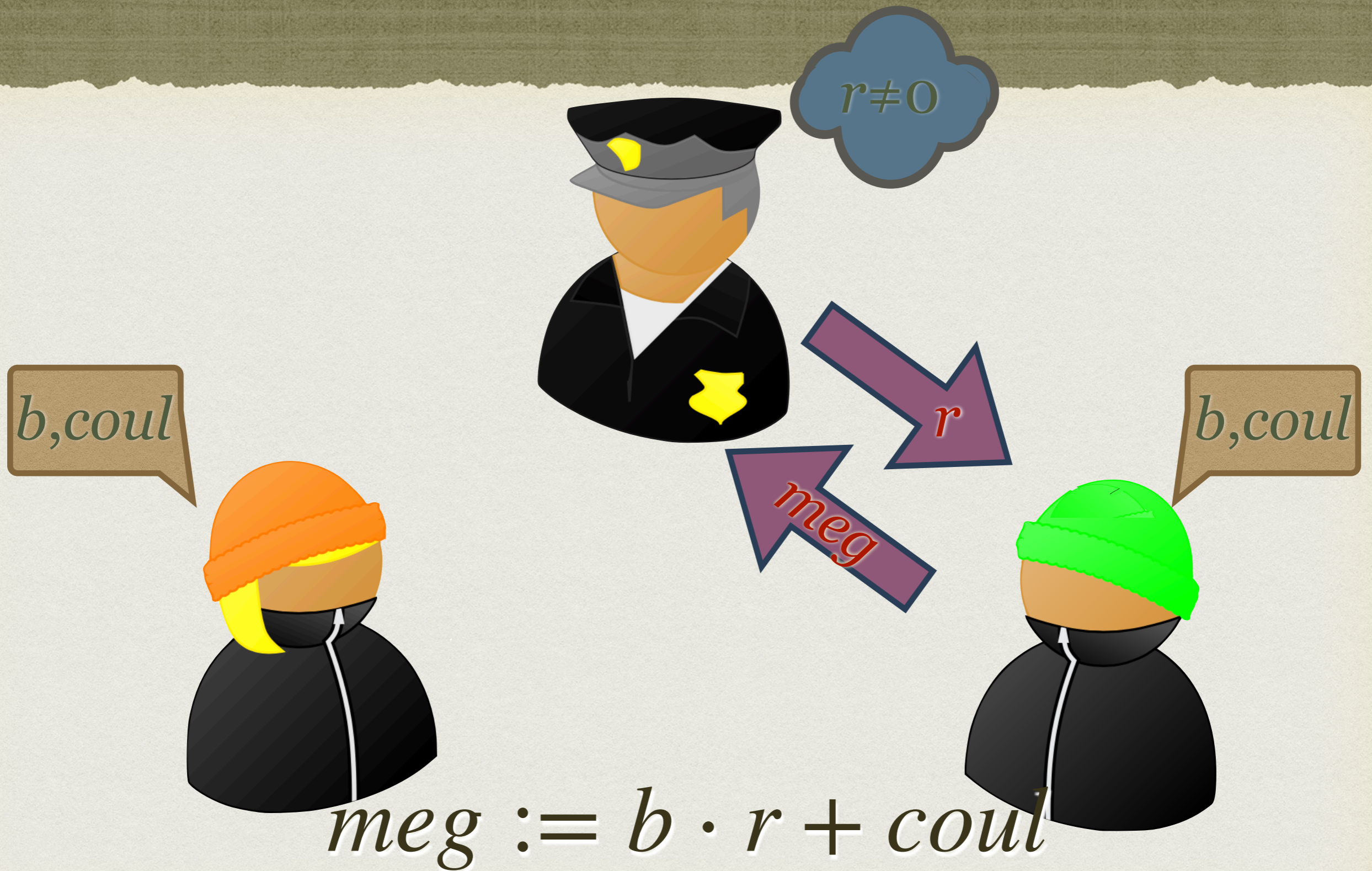


# MISE-EN-GAGE

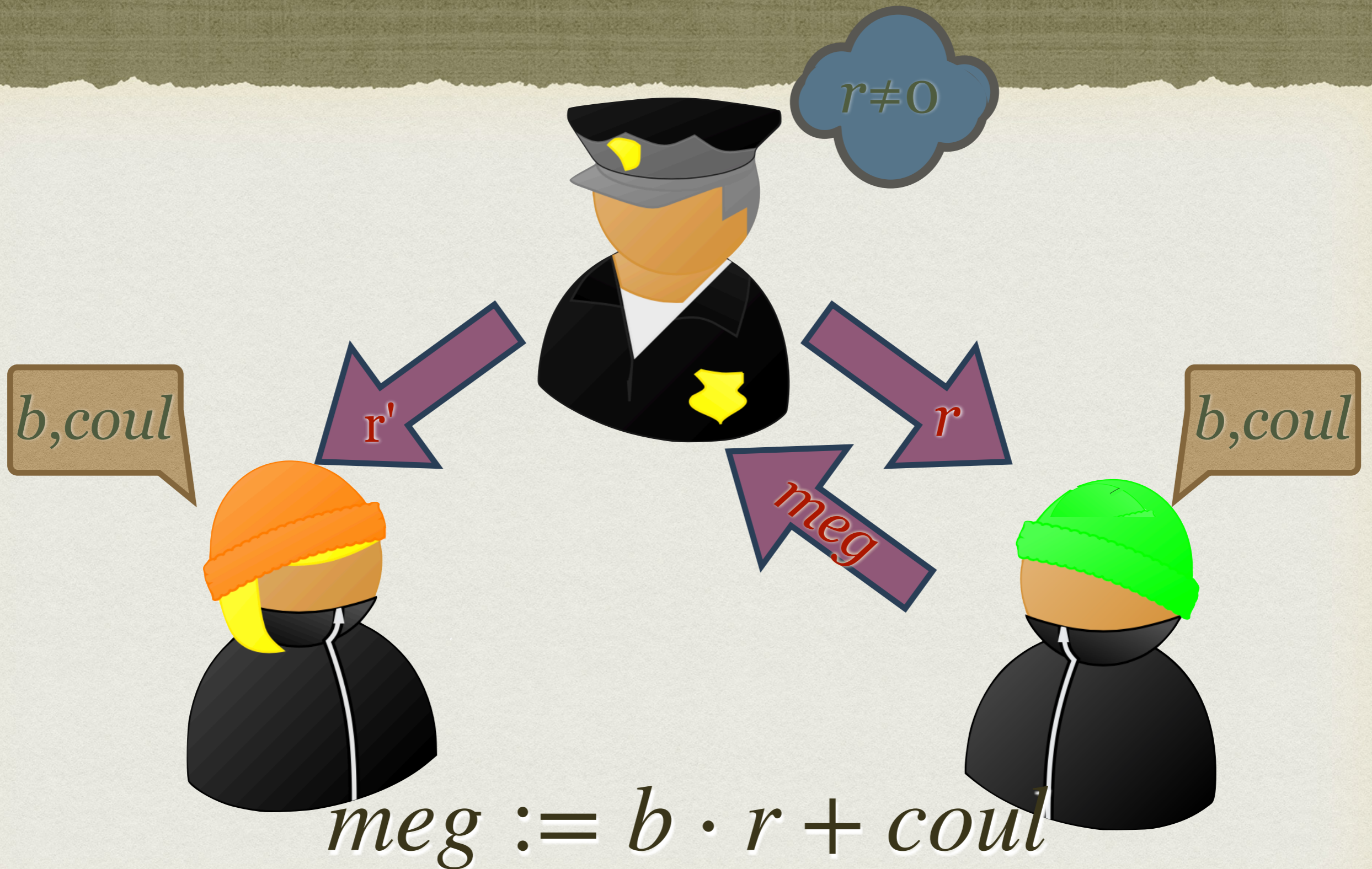




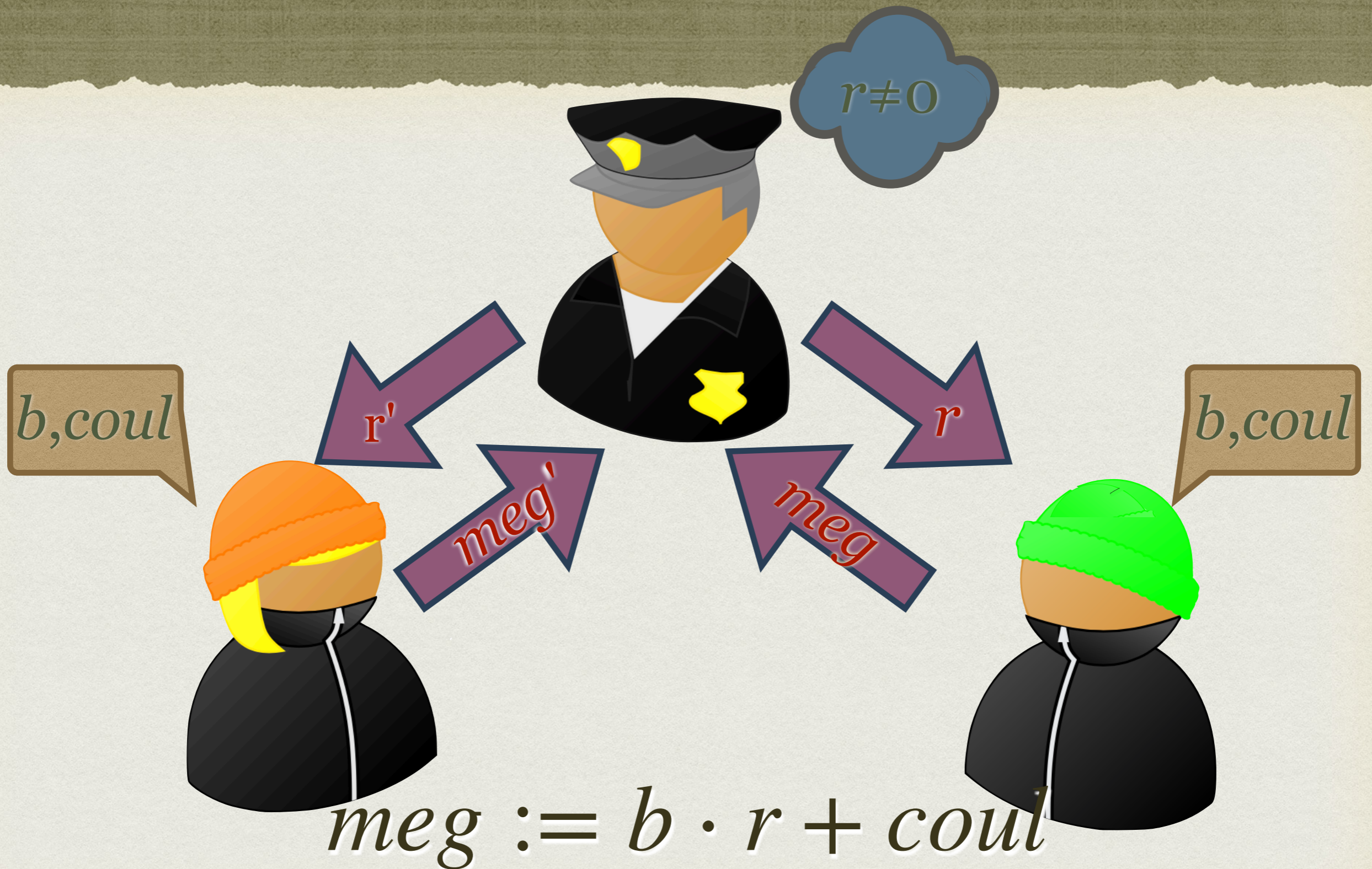
# MISE-EN-GAGE



# MISE-EN-GAGE



# MISE-EN-GAGE



# MISE-EN-GAGE



$$meg := b \cdot r + coul$$
$$meg' := b \cdot r' + coul$$

# MISE-EN-GAGE

$$\text{coul} = \frac{\text{meg} \cdot r' - \text{meg}' \cdot r}{r' - r}$$

$$r \neq 0$$

$b, \text{coul}$



$r'$

$\text{meg}'$



$r$

$\text{meg}$

$b, \text{coul}$



$$\begin{aligned} \text{meg} &::= b \cdot r + \text{coul} \\ \text{meg}' &::= b \cdot r' + \text{coul} \end{aligned}$$

MISE-EN-GAGE

PRINCIPE DE

DÉVOILEMENT VIA M-E-G

MISE-EN-GAGE

PRINCIPE DE

DÉVOILEMENT VIA M-E-G

=

DOUBLE-SPENDING

DETECTION MECHANISM



$P_1$

$(n_1, n_2) \in E$

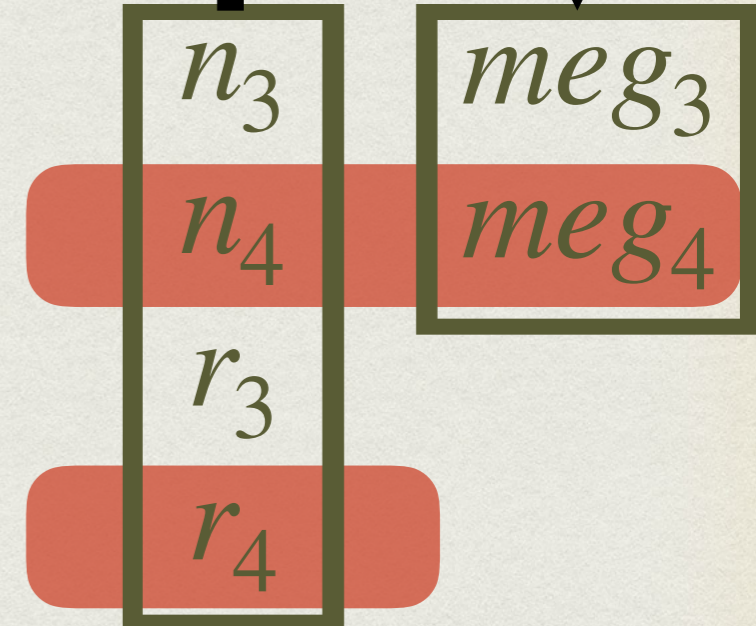
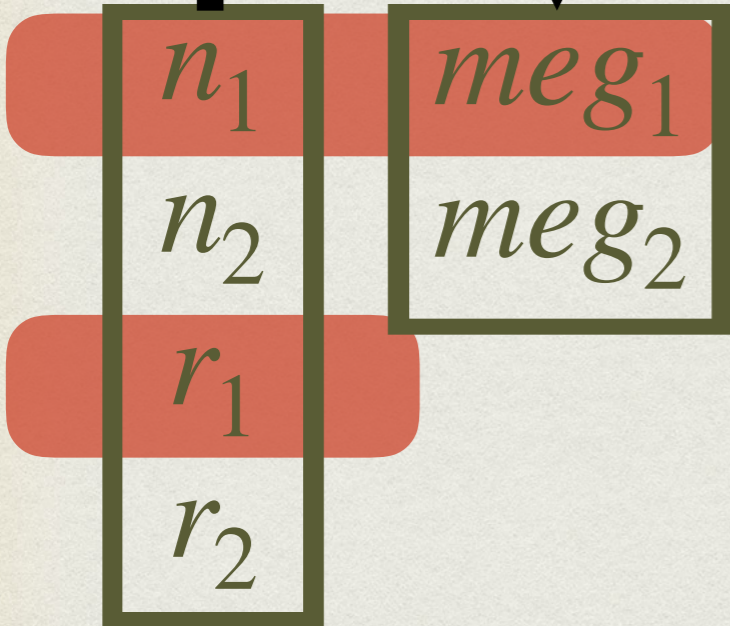
$$meg_i = coul_{n_i} + b_{n_i} r_i$$

$$meg_j = coul_{n_j} + b_{n_j} r_j$$



$P_2$

$(n_3, n_4) \in E$







# P<sub>1</sub>

$(n_1, n_2) \in E$

$$meg_i = coul_{n_i} + b_{n_i} r_i$$

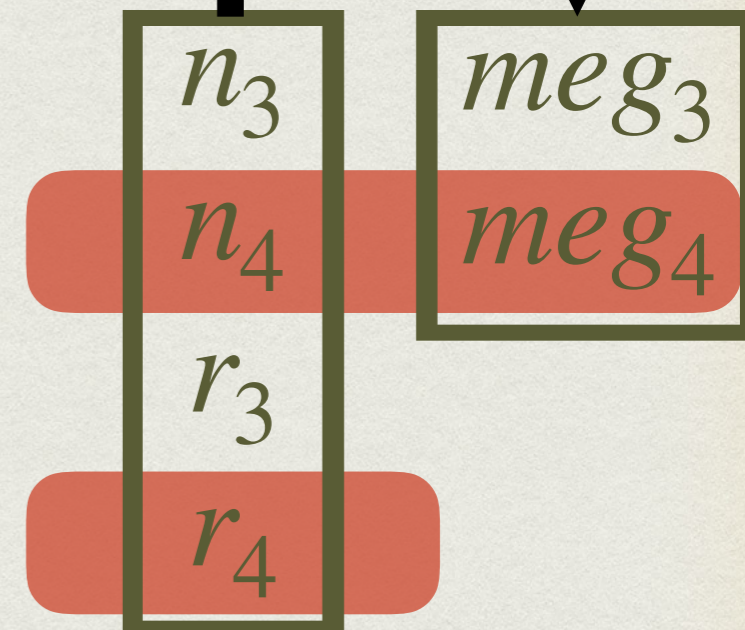
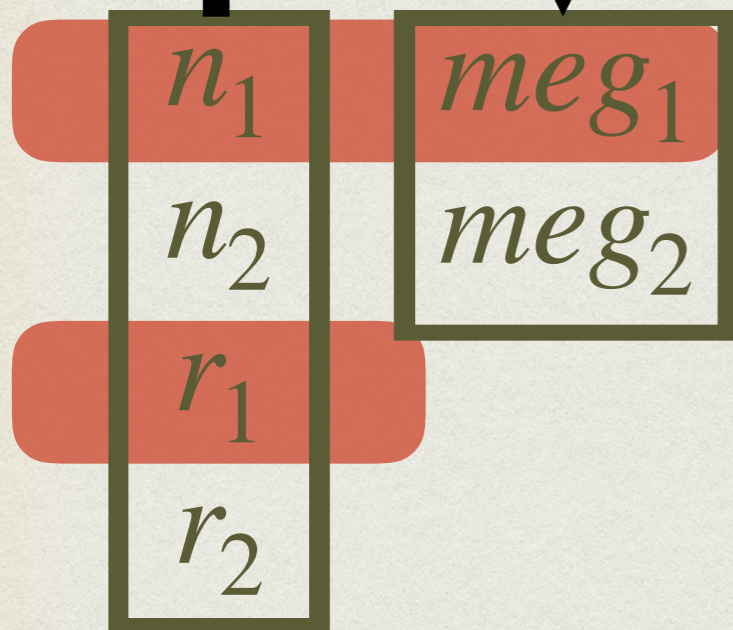
$$meg_j = coul_{n_j} + b_{n_j} r_j$$

Demander à deux  
prouveurs le même  
noeud avec même  $r$   
vérifie la consistance.



# P<sub>2</sub>

$(n_3, n_4) \in E$





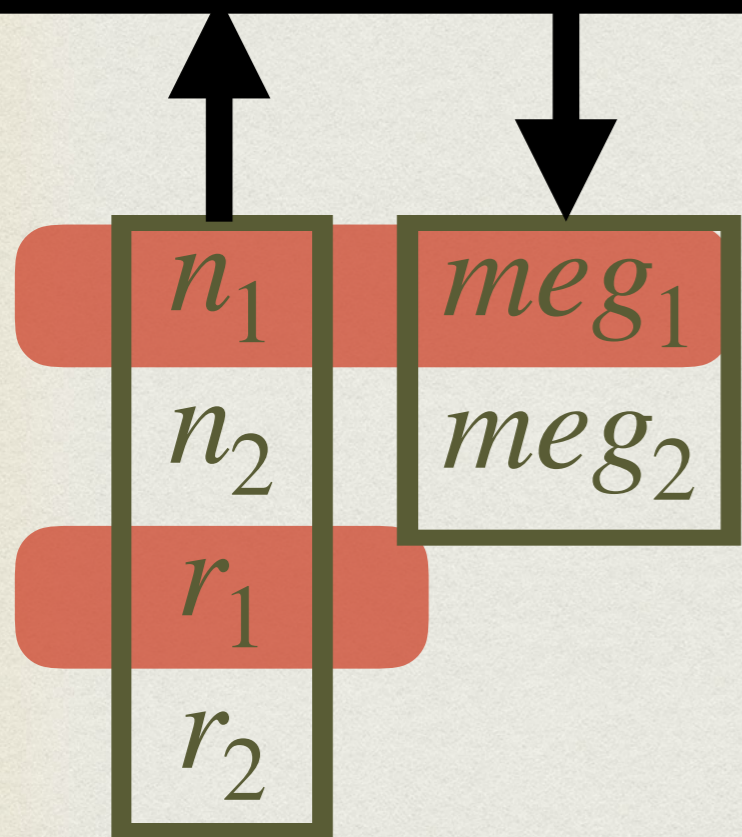
$P_1$

$(n_1, n_2) \in E$

$$meg_i = coul_{n_i} + b_{n_i} r_i$$

$$meg_j = coul_{n_j} + b_{n_j} r_j$$

Demander à deux prouveurs le même noeud avec même  $r$  vérifie la consistance.

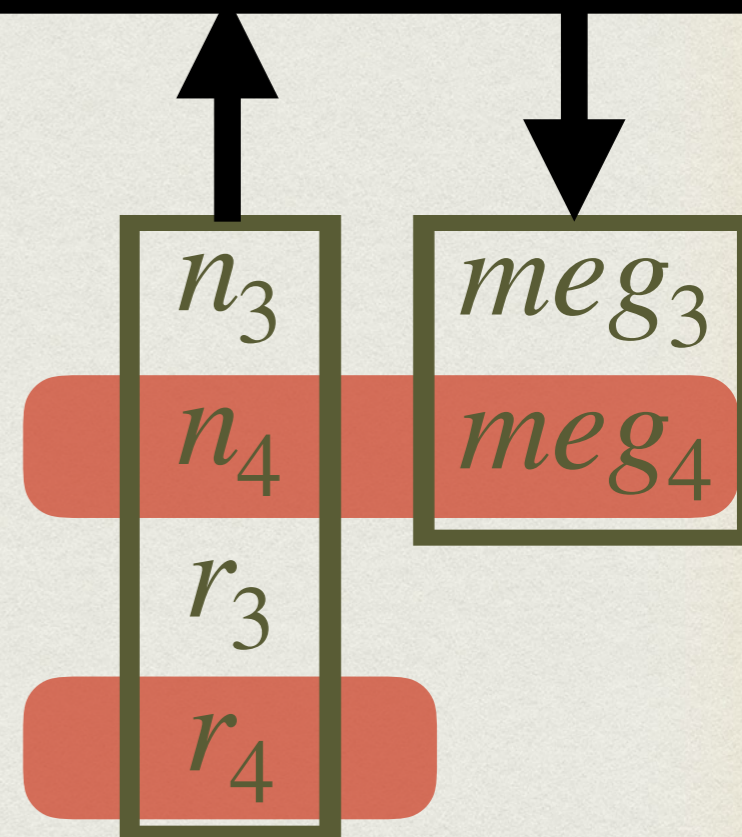


Asking two provers the same node with same  $r$  checks their consistency.

$$n_i = n_j \wedge r_i = r_j \implies meg_i = meg_j$$


$P_2$

$(n_3, n_4) \in E$





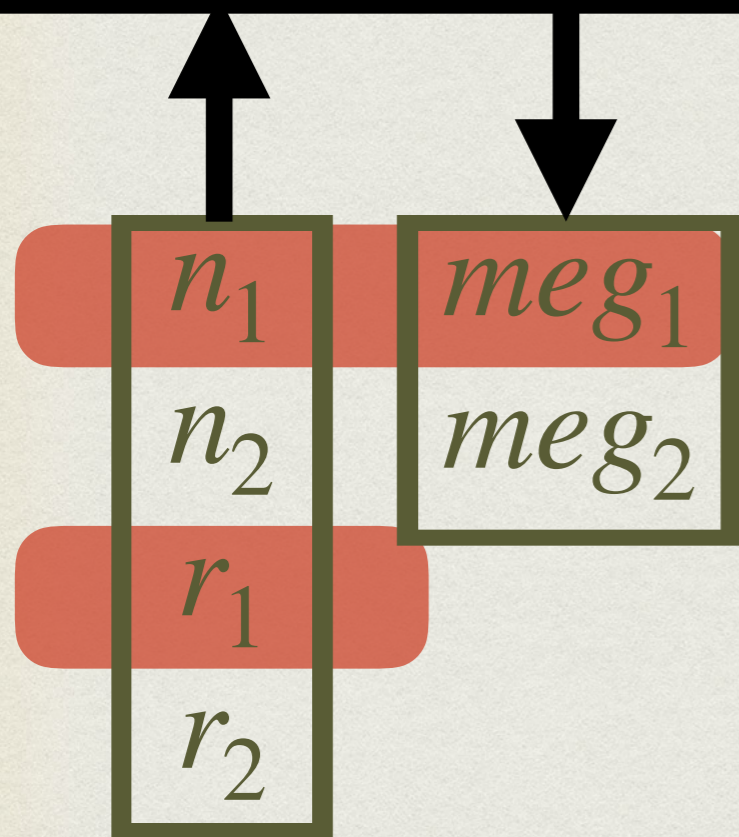
$P_1$

$(n_1, n_2) \in E$

$$meg_i = coul_{n_i} + b_{n_i} r_i$$

$$meg_j = coul_{n_j} + b_{n_j} r_j$$

Demander à deux prouveurs le même noeud avec même  $r$  vérifie la consistance.



Asking two provers the same node with same  $r$  checks their consistency.

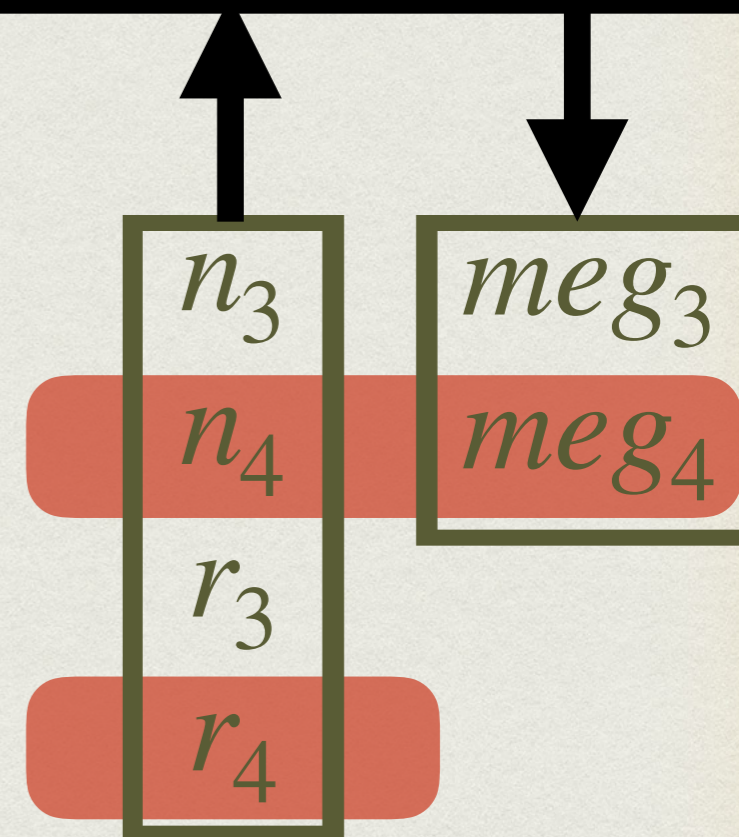
$$n_i = n_j \wedge r_i = r_j \implies meg_i = meg_j$$

Demander à deux prouveurs le même noeud avec deux  $r$ 's donne la couleur.



$P_2$

$(n_3, n_4) \in E$





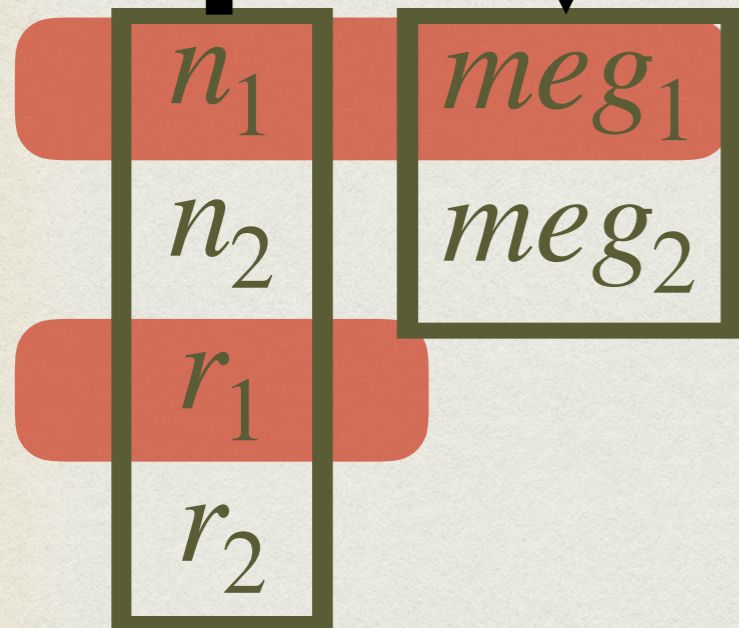
# P<sub>1</sub>

$(n_1, n_2) \in E$

$$meg_i = coul_{n_i} + b_{n_i} r_i$$

$$meg_j = coul_{n_j} + b_{n_j} r_j$$

Demander à deux prouveurs le même noeud avec même  $r$  vérifie la consistance.



Asking two provers the same node with same  $r$  checks their consistency.

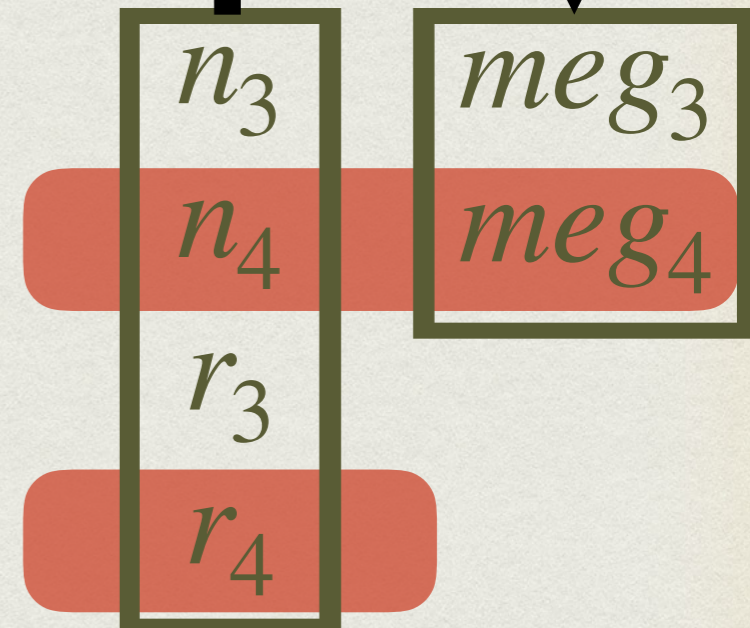
$$n_i = n_j \wedge r_i = r_j \implies meg_i = meg_j$$

Demander à deux prouveurs le même noeud avec deux  $r$ 's donne la couleur.



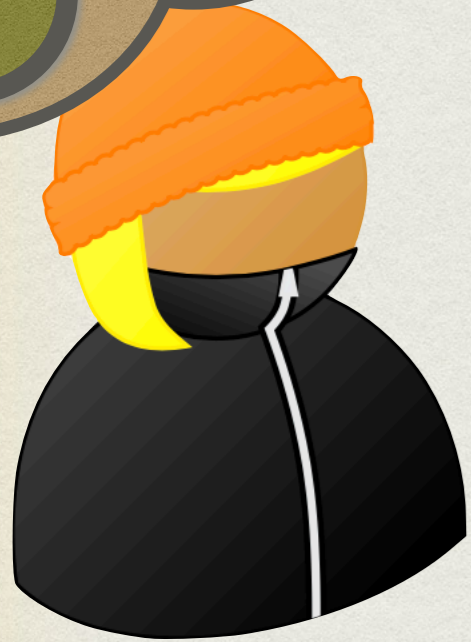
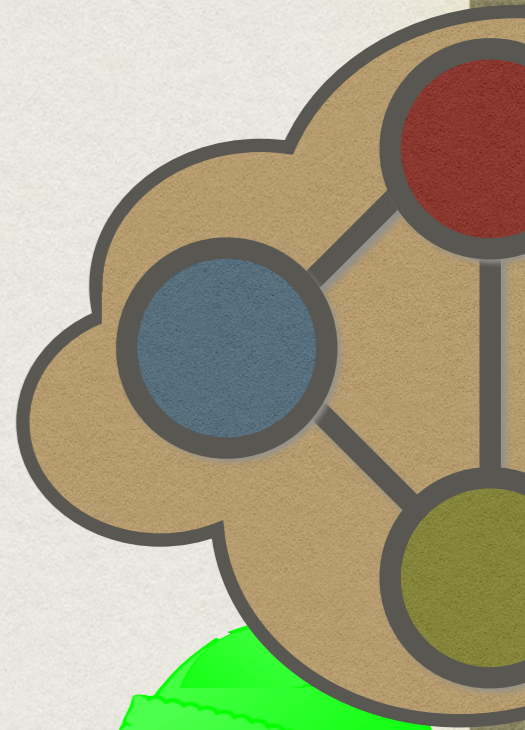
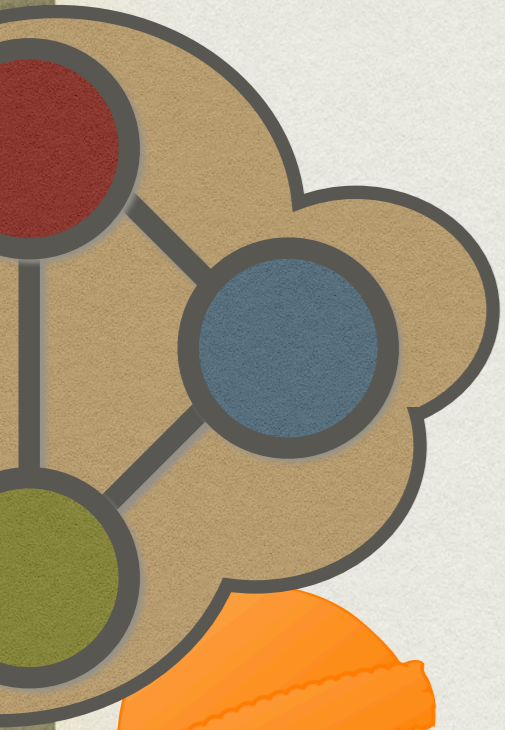
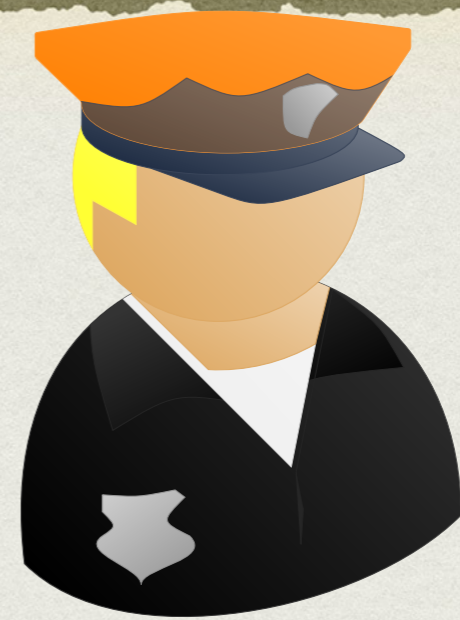
# P<sub>2</sub>

$(n_3, n_4) \in E$

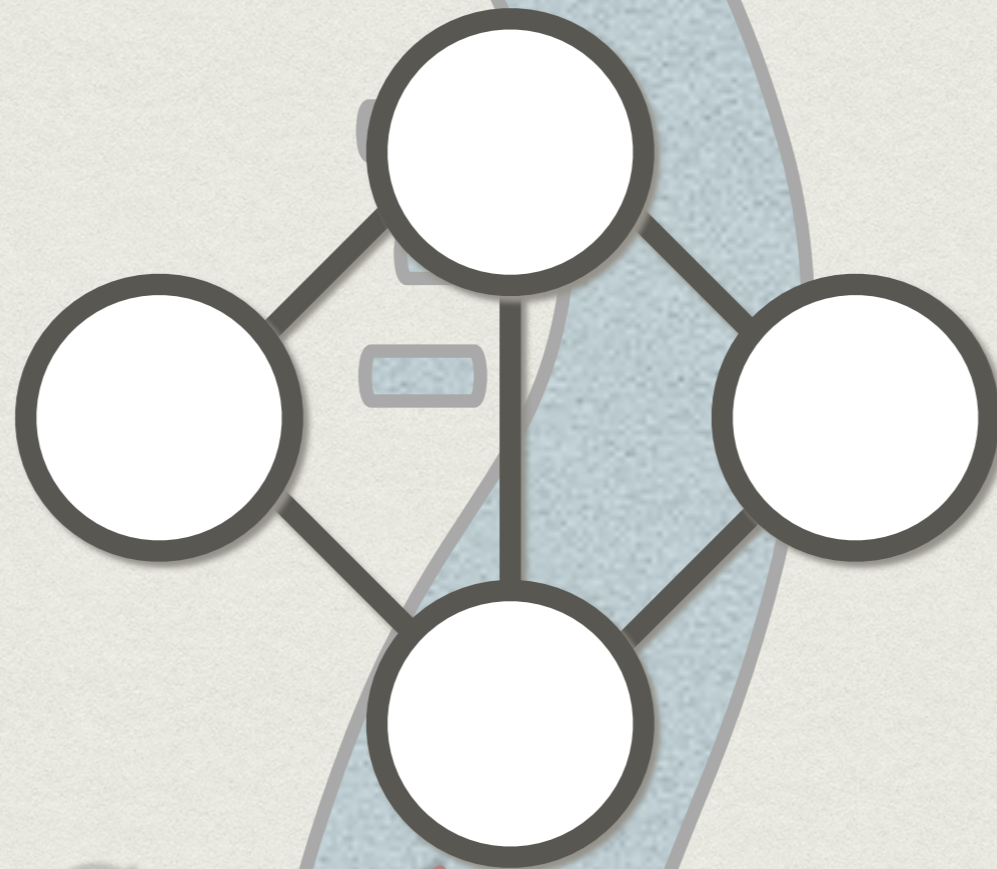


Asking two provers the same node with different  $r$ 's reveals the node colour.

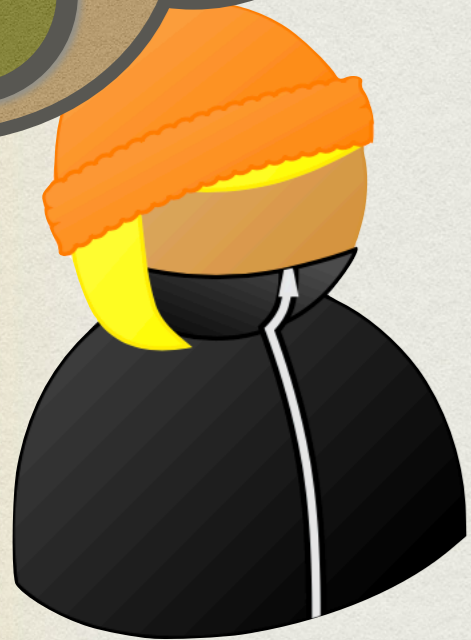
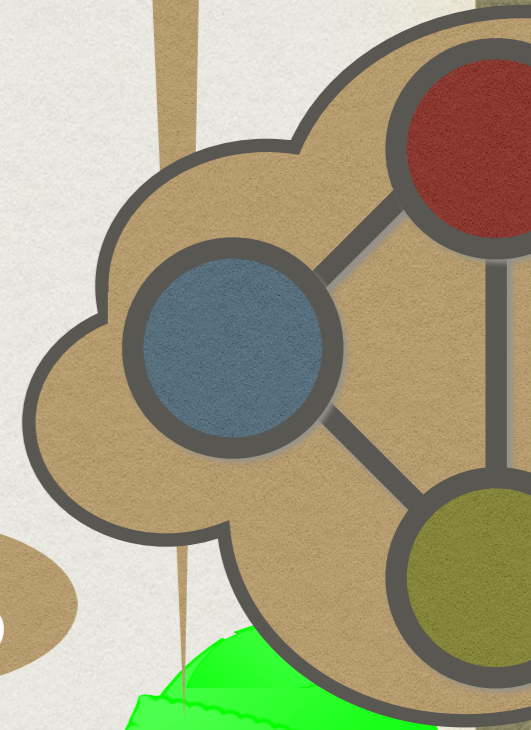
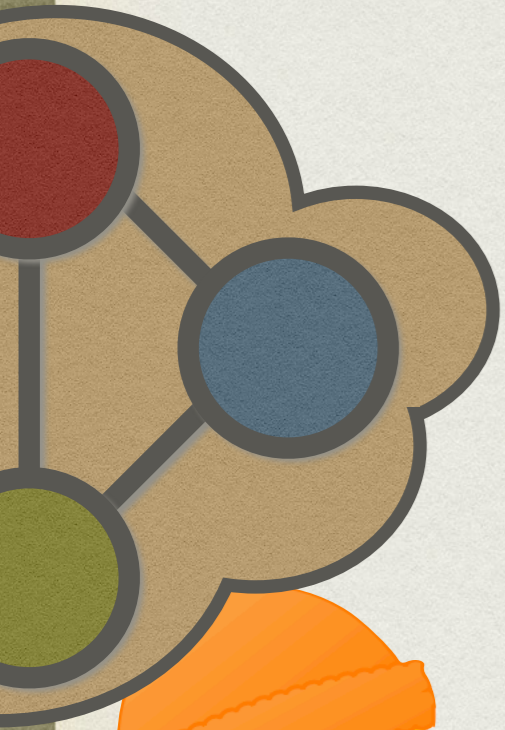
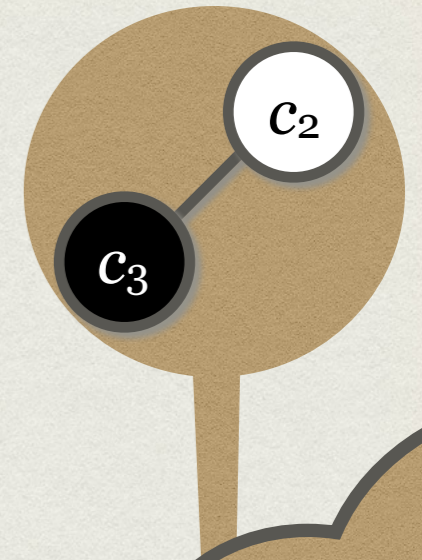
$$n_i = n_j \wedge r_i \neq r_j \implies coul_{n_i} = meg_j + meg_i$$



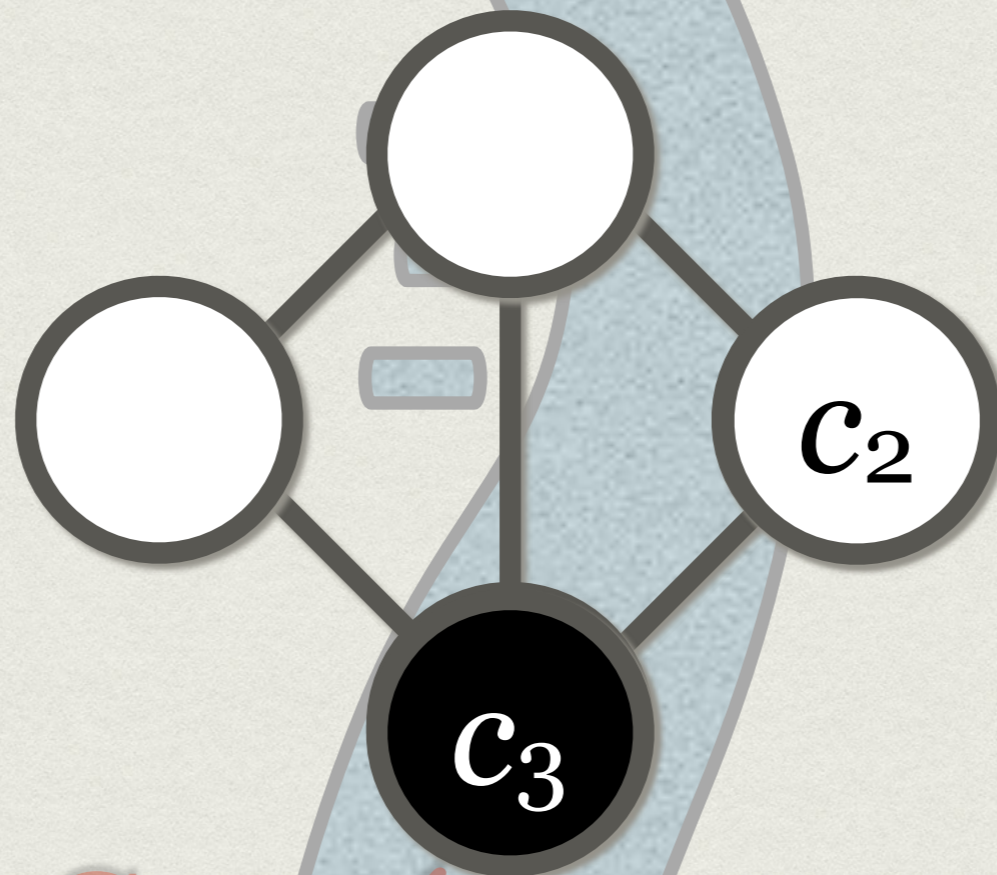
COMPLÉTUDE



COHÉRENCE

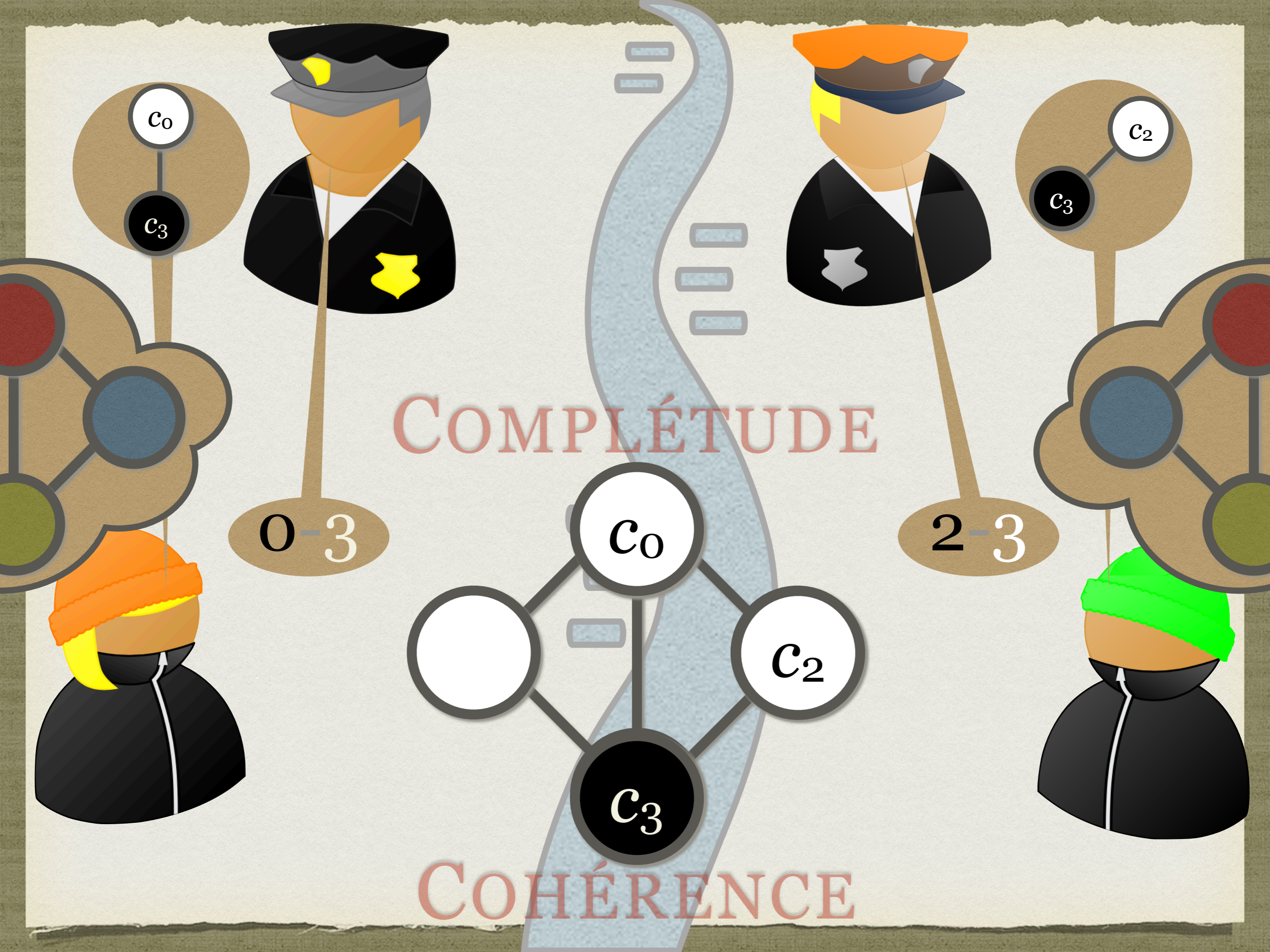


COMPLÉTUDE



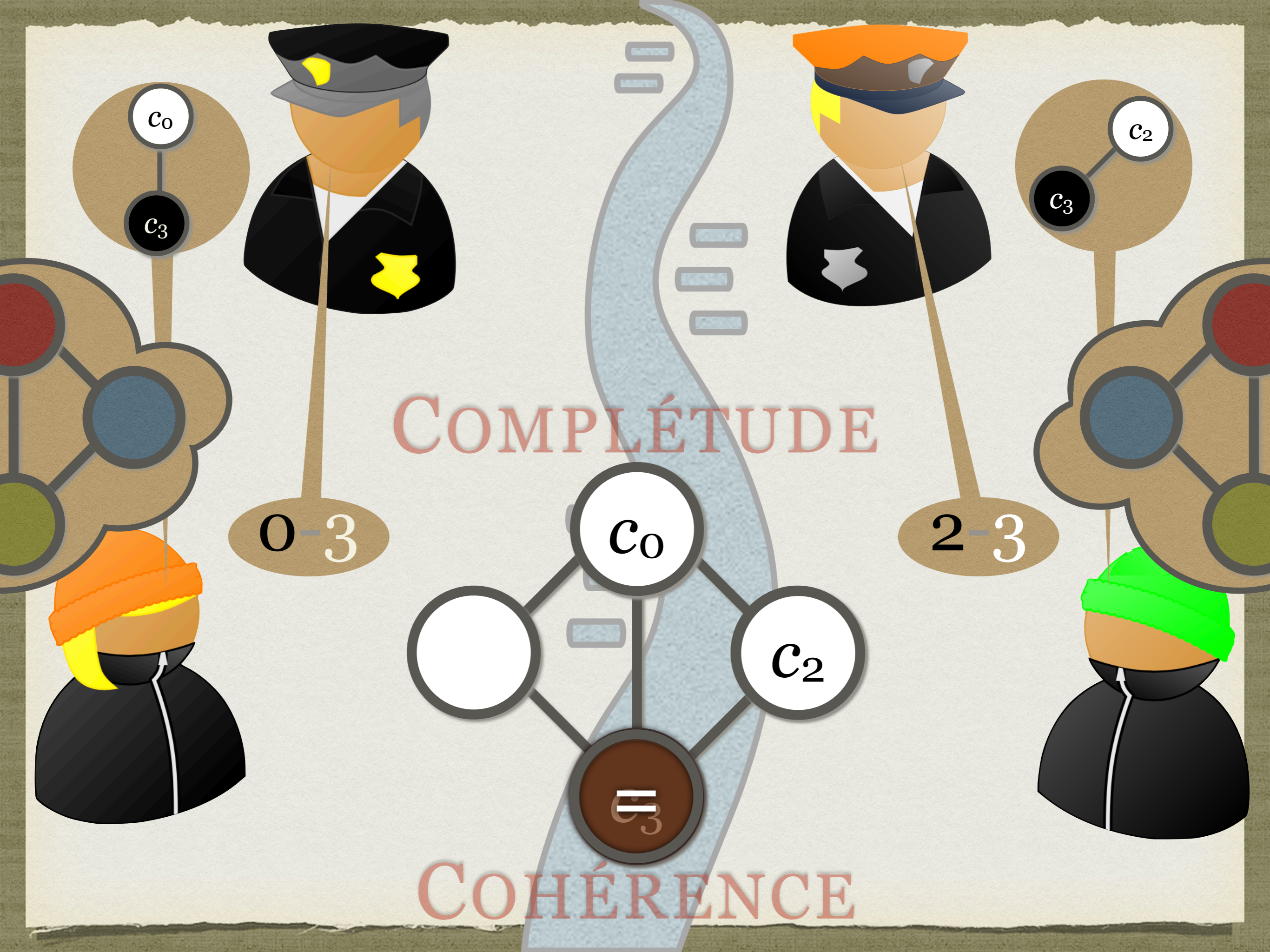
2-3

COHÉRENCE



COMPLÉTUDE

COHÉRENCE



COMPLÉTUDE

COHÉRENCE

$C_0$

$C_3$

0-3

$C_0$

$C_2$

$C_3$

$C_2$

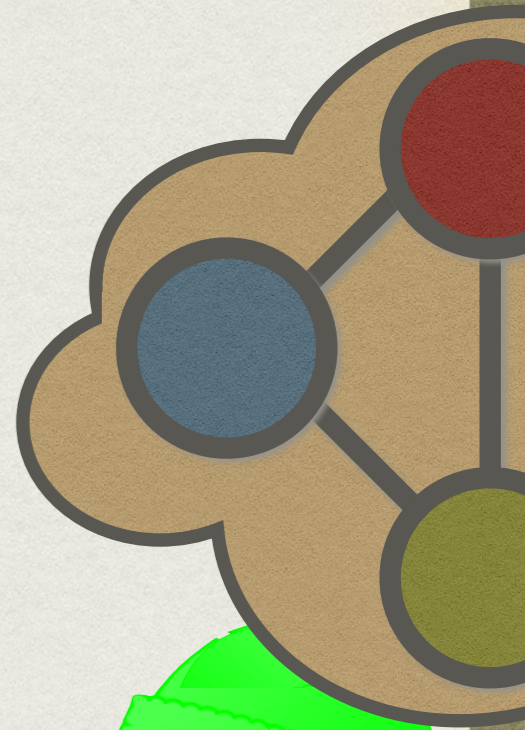
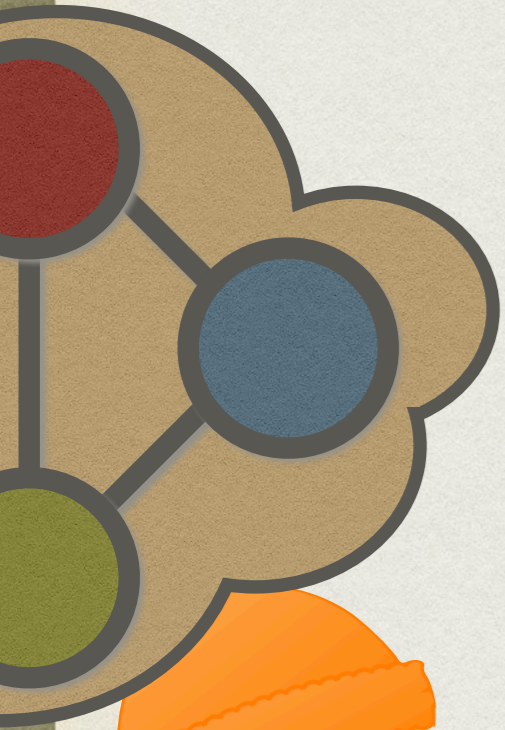
$C_3$

2-3

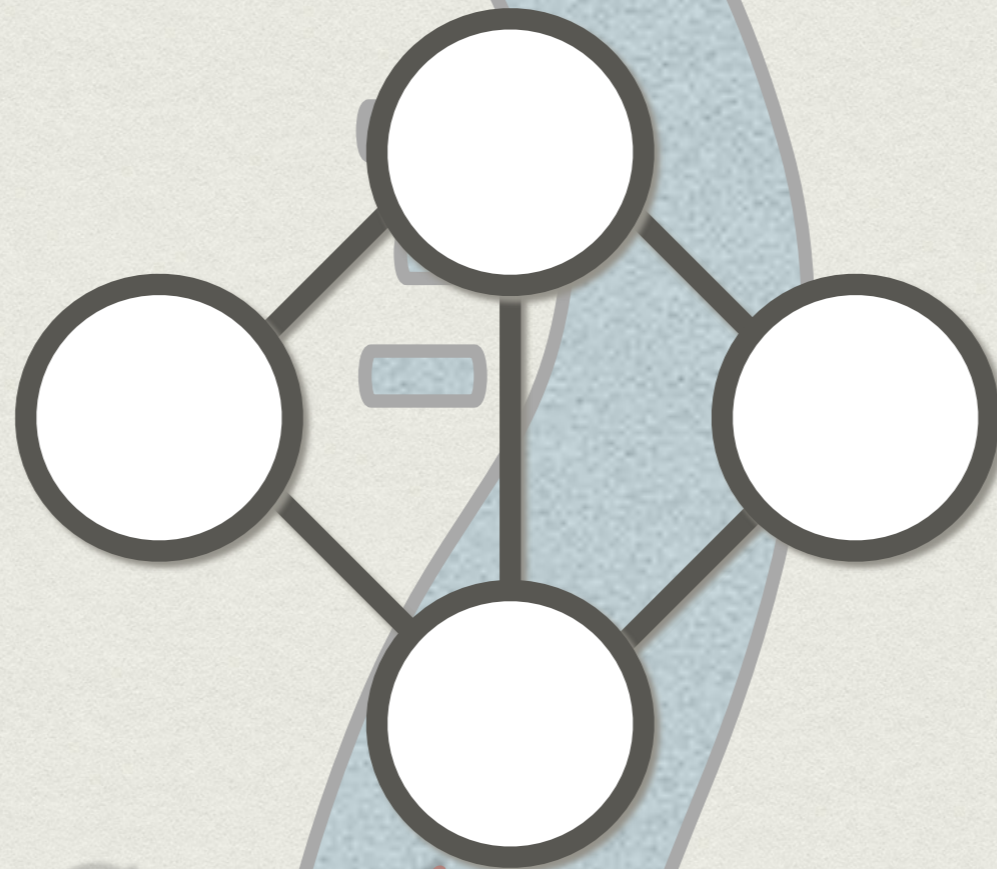
Green beanie

Orange beanie

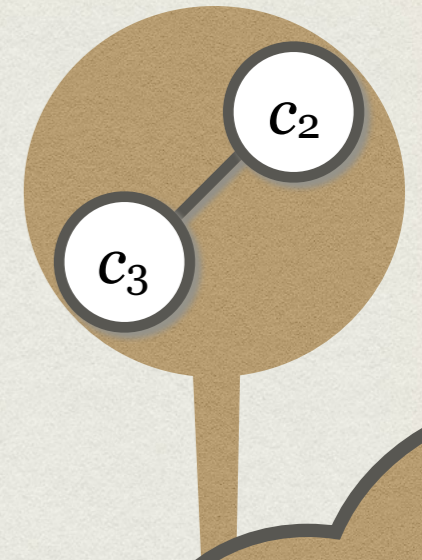
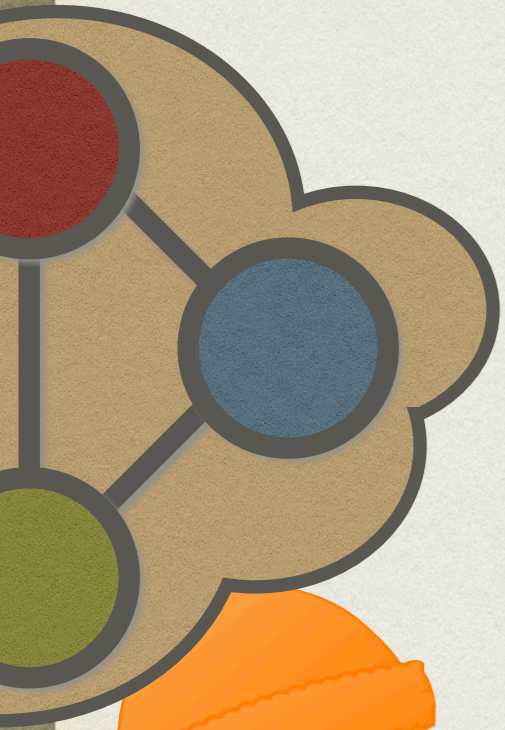




COMPLÉTUDE

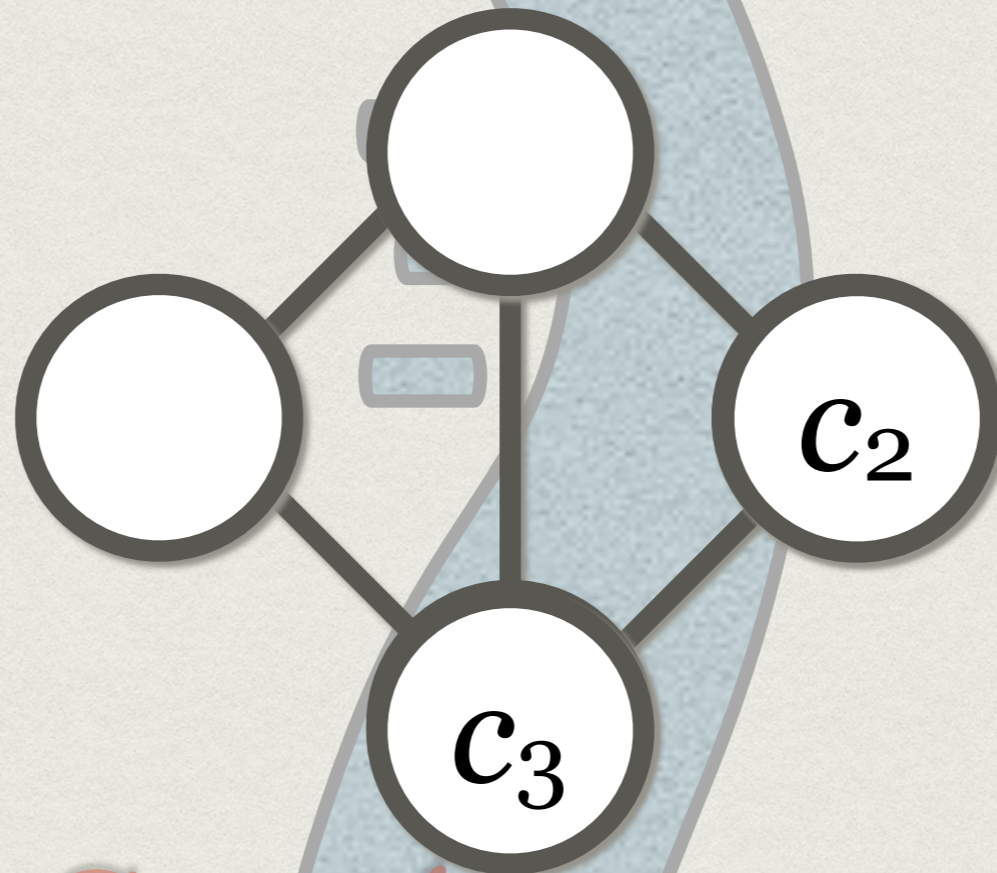
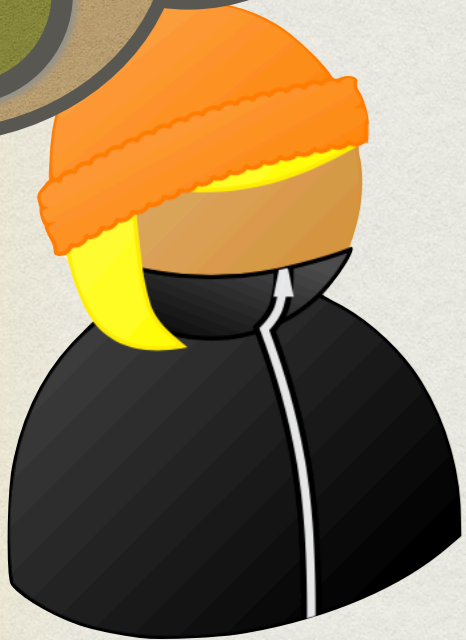


COHÉRENCE

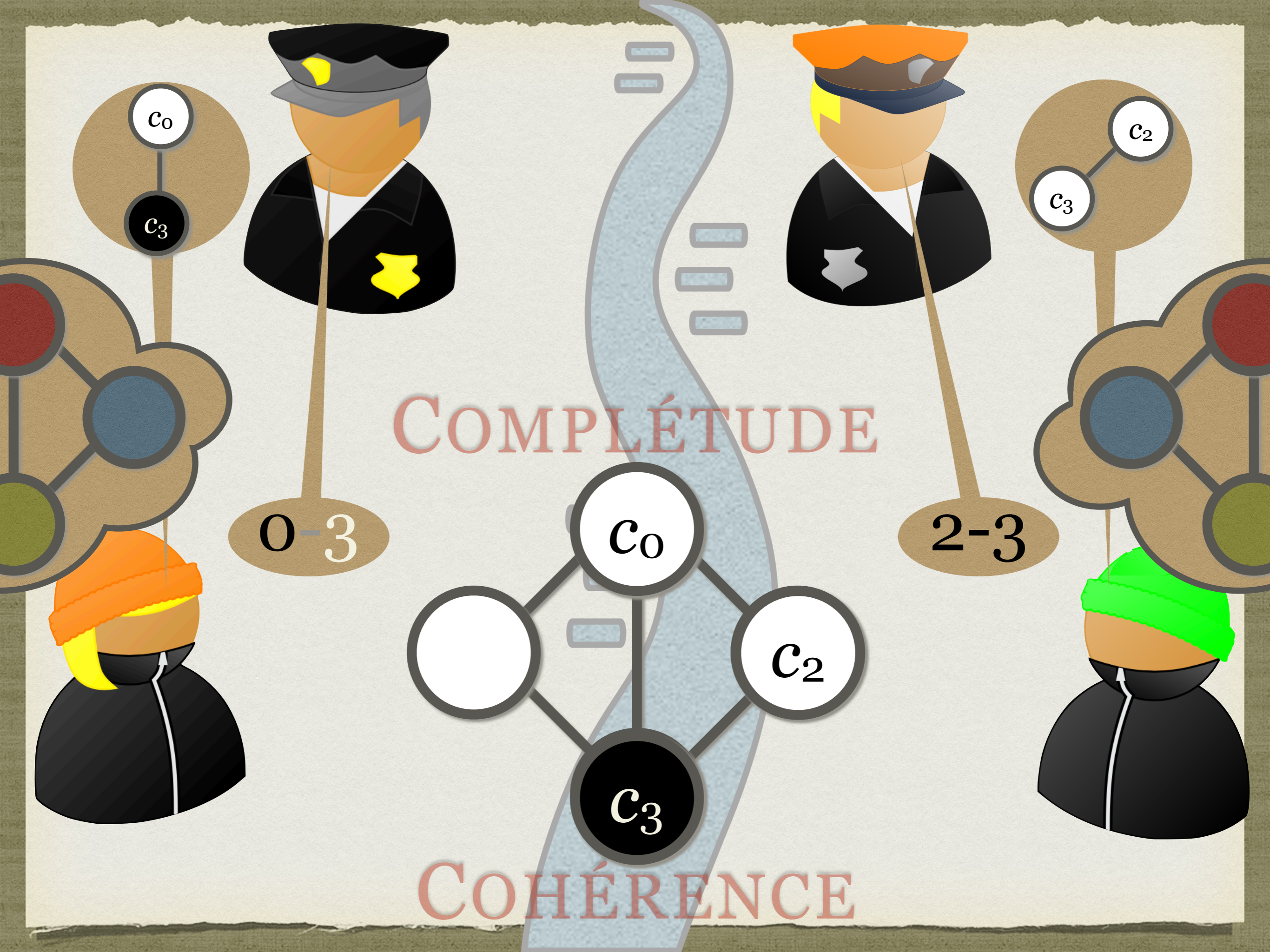


COMPLÉTUDE

2-3

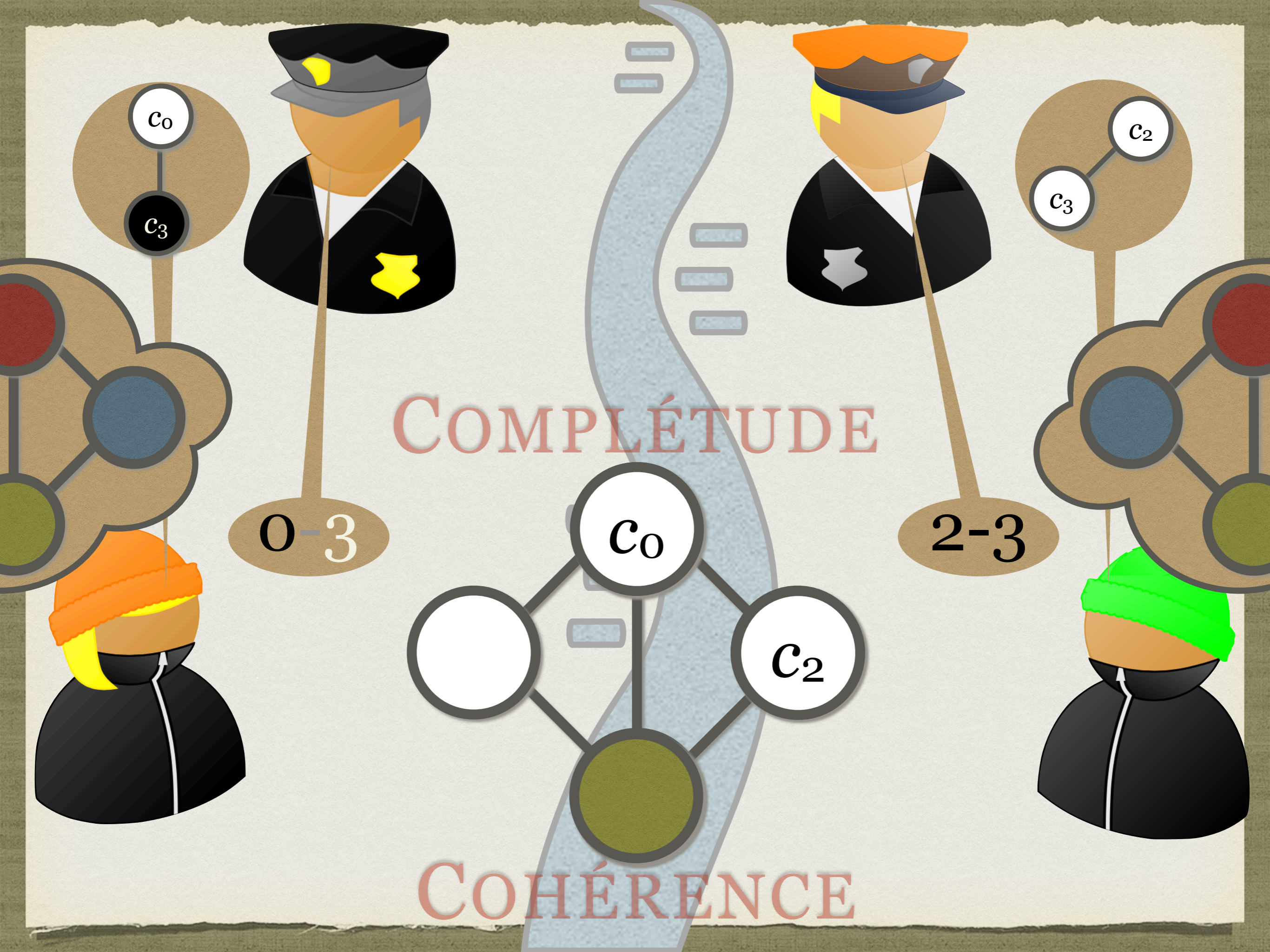


COHÉRENCE



COMPLÉTUDE

COHÉRENCE



COMPLÉTUDE

COHÉRENCE

$C_0$

$C_3$

0-3

$C_0$

$C_2$

2-3

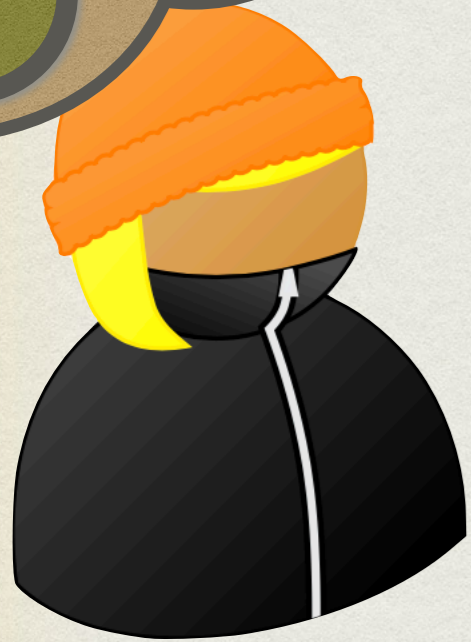
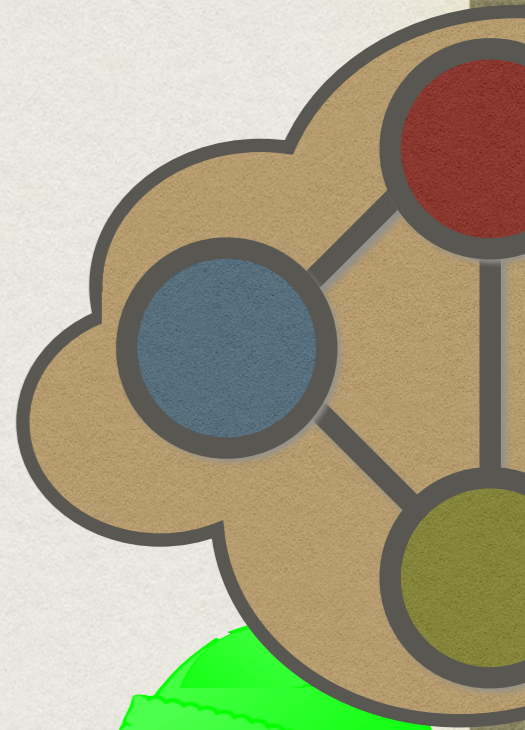
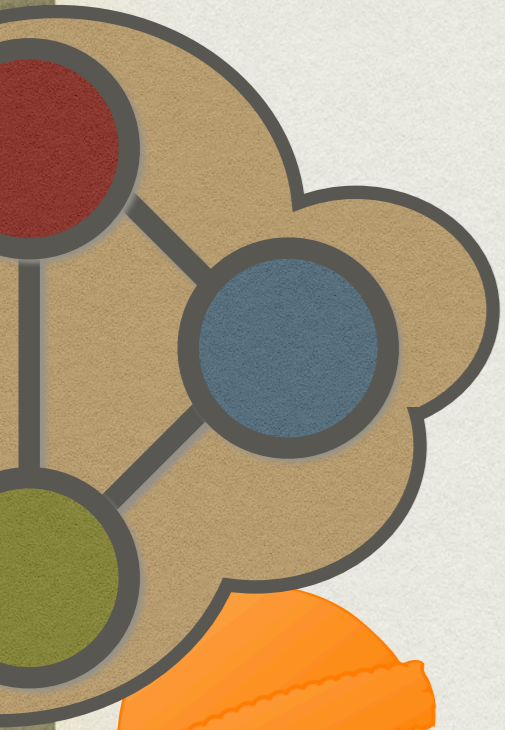
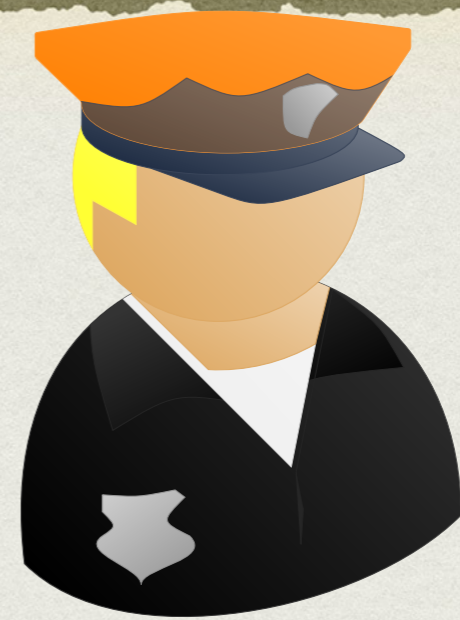
$C_2$

$C_3$

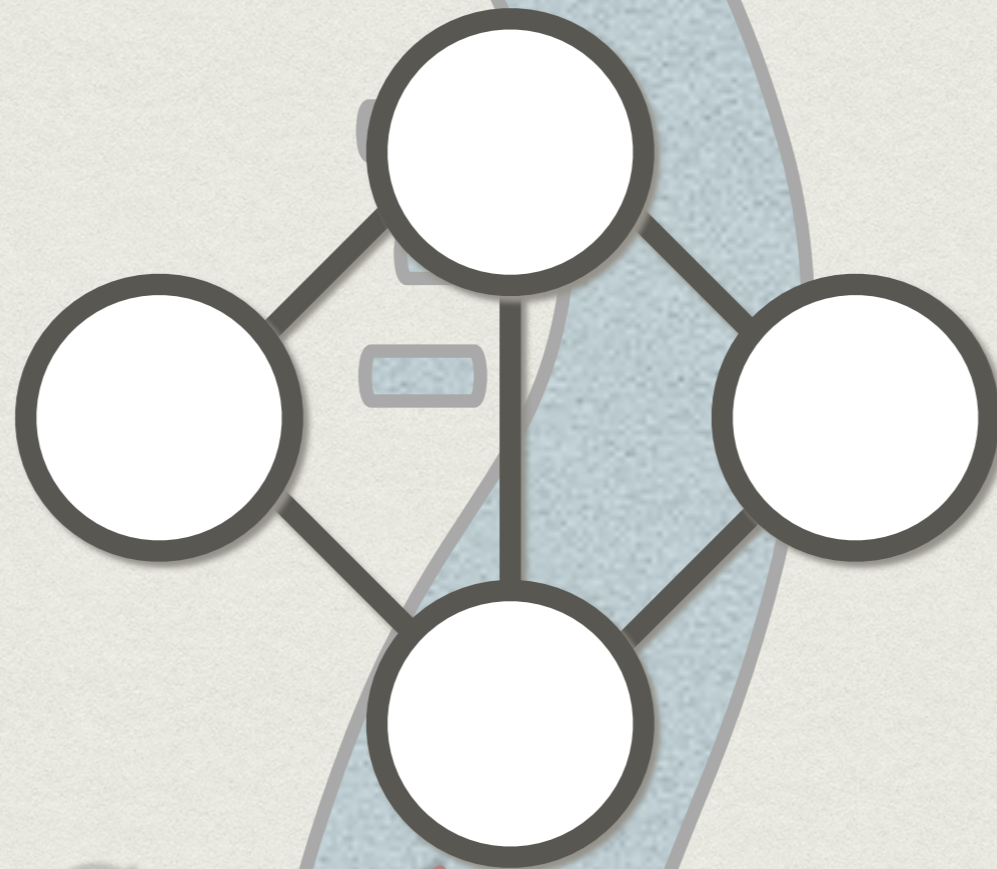
0-3

$C_2$

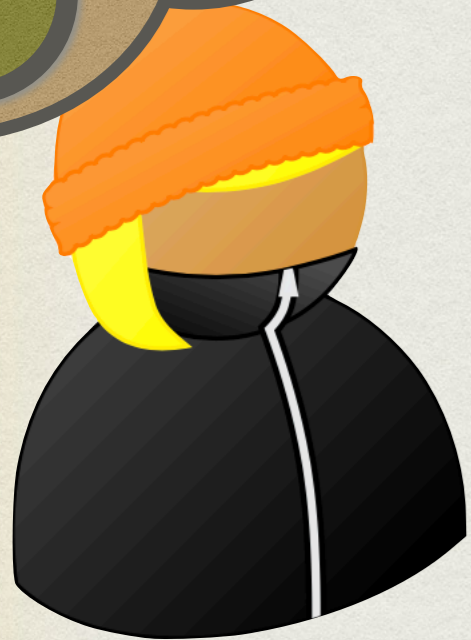
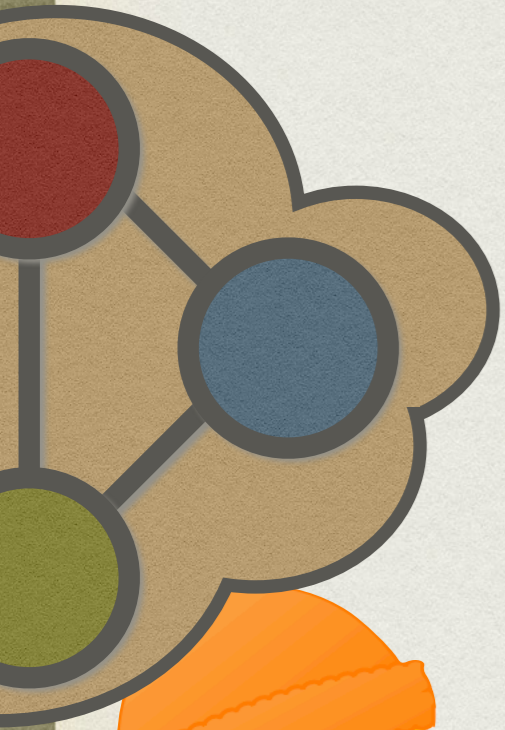
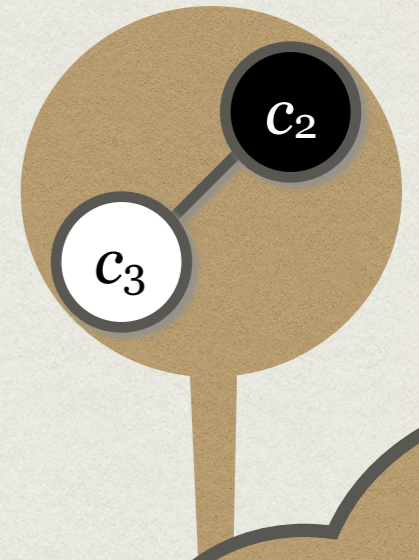
$C_3$



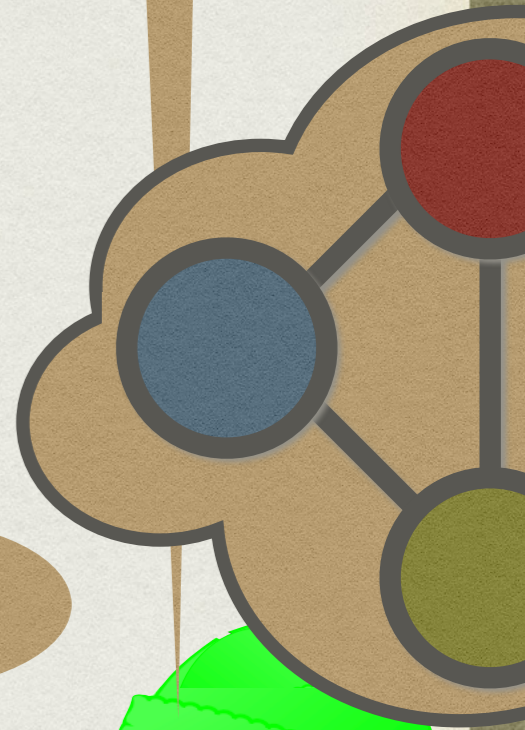
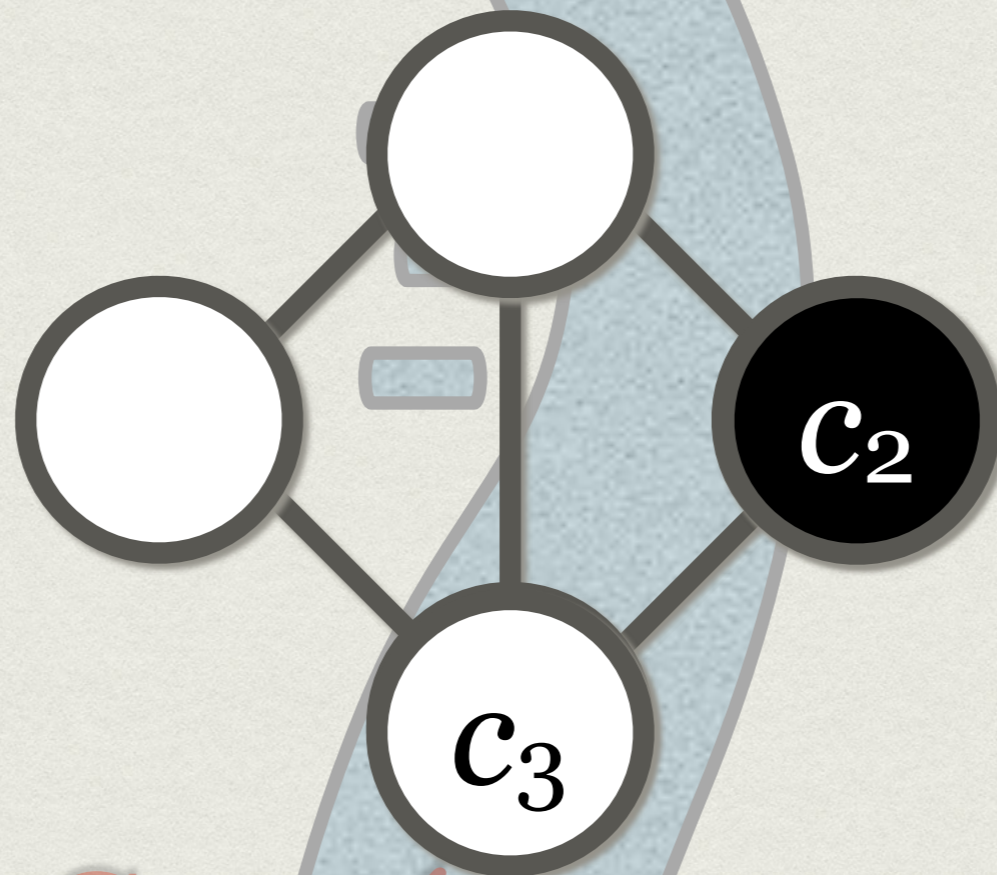
COMPLÉTUDE



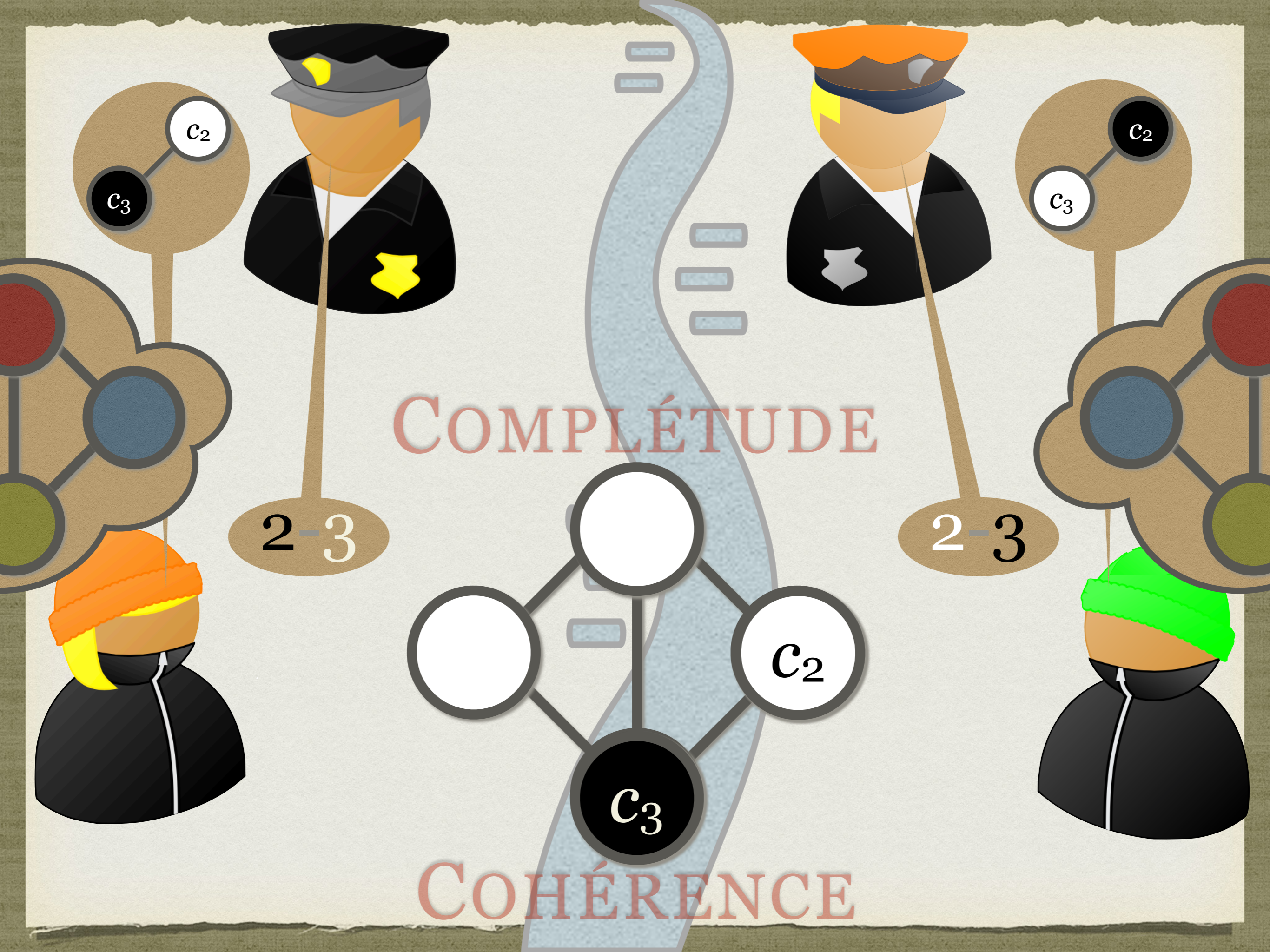
COHÉRENCE



COMPLÉTUDE



COHÉRENCE



COMPLÉTUDE

COHÉRENCE

$C_2$

$C_3$

2-3

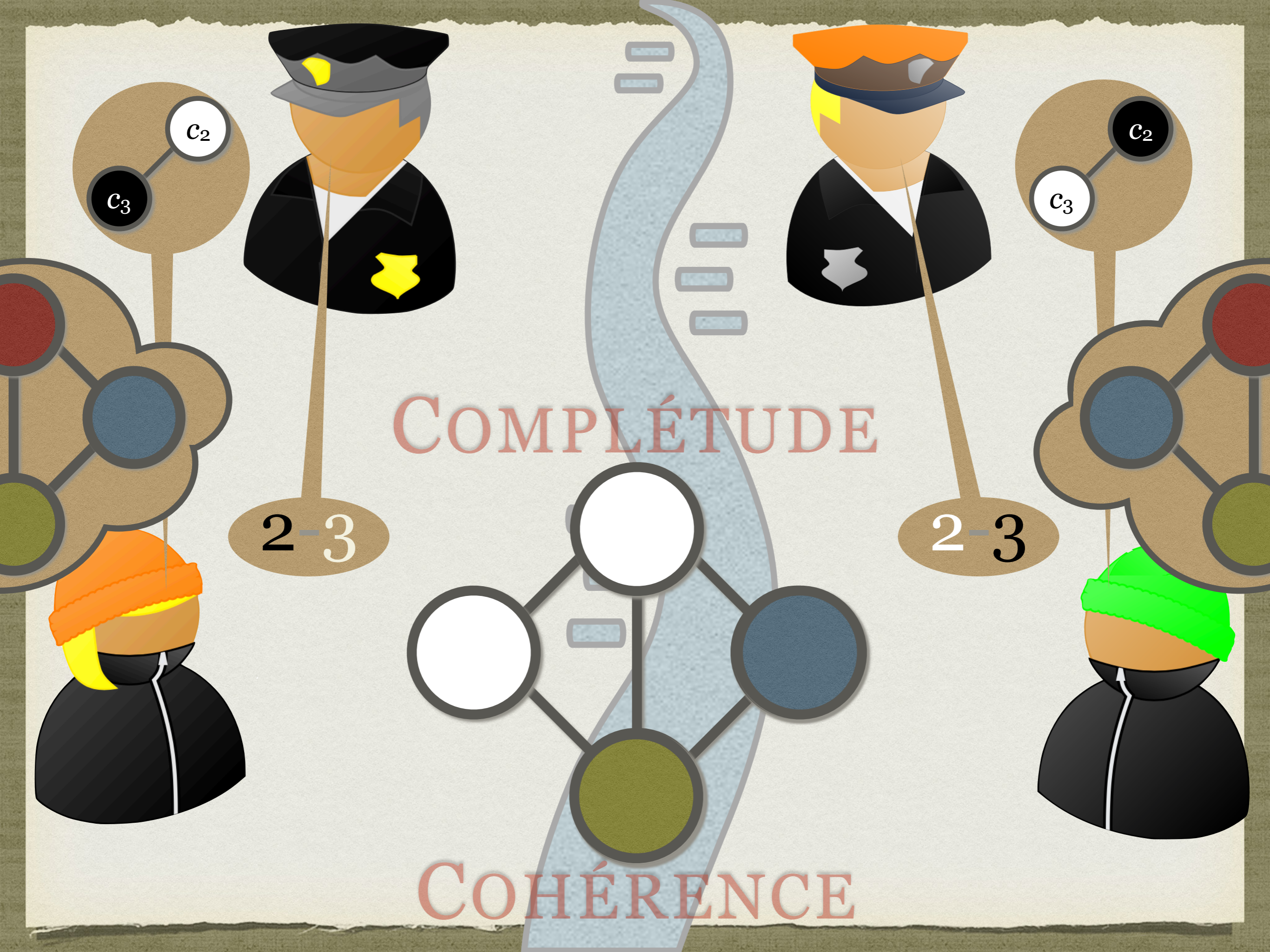
$C_2$

$C_3$

2-3

$C_2$

$C_3$



COMPLÉTUDE

COHÉRENCE

2-3

2-3

C<sub>2</sub>

C<sub>3</sub>

C<sub>2</sub>

C<sub>3</sub>

White circle node

White circle node

Blue circle node

Green circle node



# COHÉRENCE MALGRÉ L'INTRICATION

HONNÊTE:

$$MEG^k[n_i, r_i, n_j, r_j] = (\text{coul}_{n_i} + b_{n_i} r_i, \text{coul}_{n_j} + b_{n_j} r_j)$$



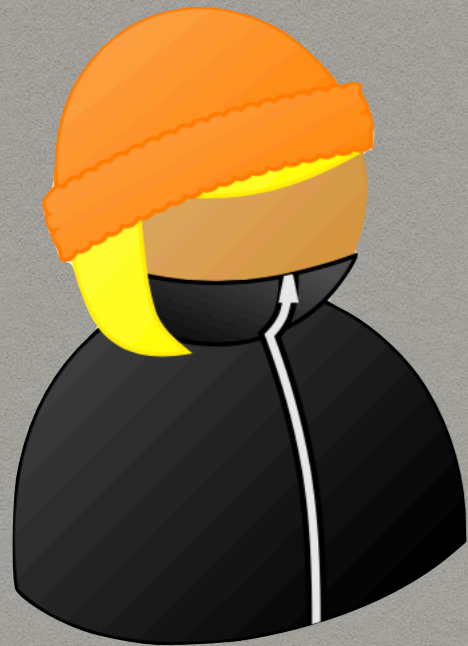
ANALYSE DE CAS

# COHÉRENCE MALGRÉ L'INTRICATION

HONNÊTE:

$$MEG^k[n_i, r_i, n_j, r_j] = (\text{coul}_{n_i} + b_{n_i} r_i, \text{coul}_{n_j} + b_{n_j} r_j)$$

MALHONNÊTE:



ANALYSE DE CAS

# COHÉRENCE MALGRÉ L'INTRICATION

HONNÊTE:

$$MEG^k[n_i, r_i, n_j, r_j] = (coul_{n_i} + b_{n_i} r_i, coul_{n_j} + b_{n_j} r_j)$$

MALHONNÊTE:

$$MEG^k[n_i, r_i, n_j, r_j] = \text{arbitraire}$$



ANALYSE DE CAS

# COHÉRENCE MALGRÉ L'INTRICATION

HONNÊTE:

$$MEG^k[n_i, r_i, n_j, r_j] = (coul_{n_i} + b_{n_i}r_i, coul_{n_j} + b_{n_j}r_j)$$

MALHONNÊTE:


$$MEG^k[n_i, r_i, n_j, r_j] = \text{arbitraire}$$

$$MEG[n_i, r_i] = \text{bien-défini}$$


ANALYSE DE CAS

# COHÉRENCE MALGRÉ L'INTRICATION

HONNÊTE:

$$MEG^k[n_i, r_i, n_j, r_j] = (coul_{n_i} + b_{n_i} r_i, coul_{n_j} + b_{n_j} r_j)$$

MALHONNÊTE:

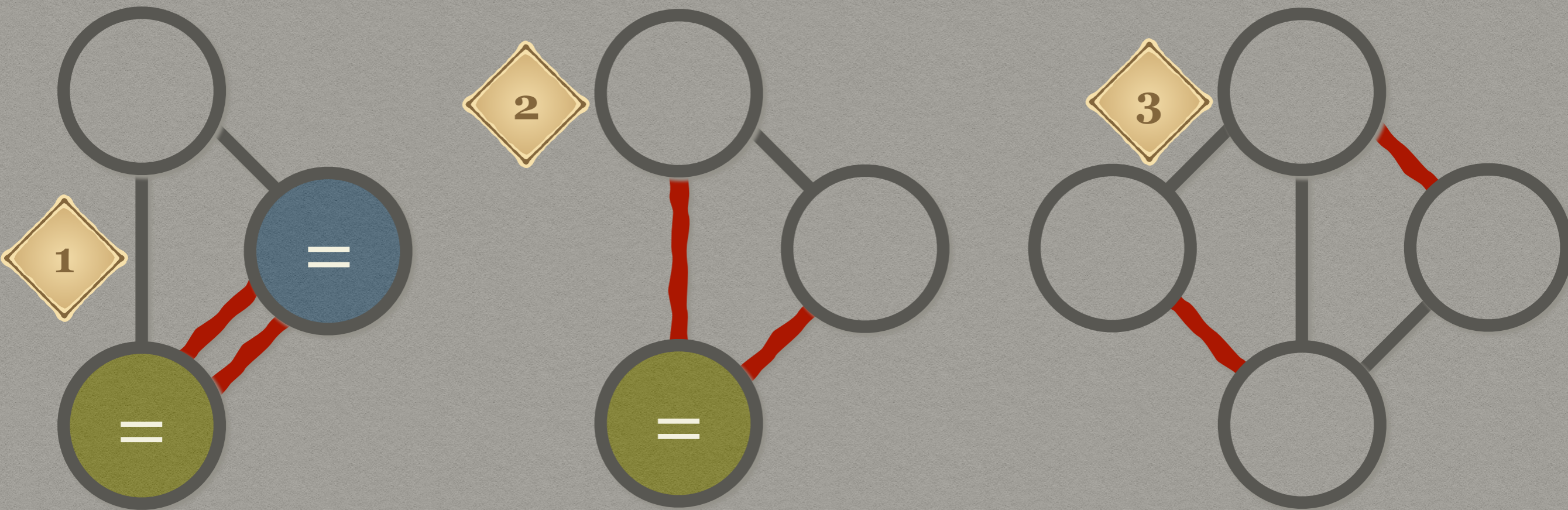

$$MEG^k[n_i, r_i, n_j, r_j] = \text{arbitraire}$$

$$MEG[n_i, r_i] = \text{bien-défini}$$

$$COUL[n_i] = \text{bien-défini}$$

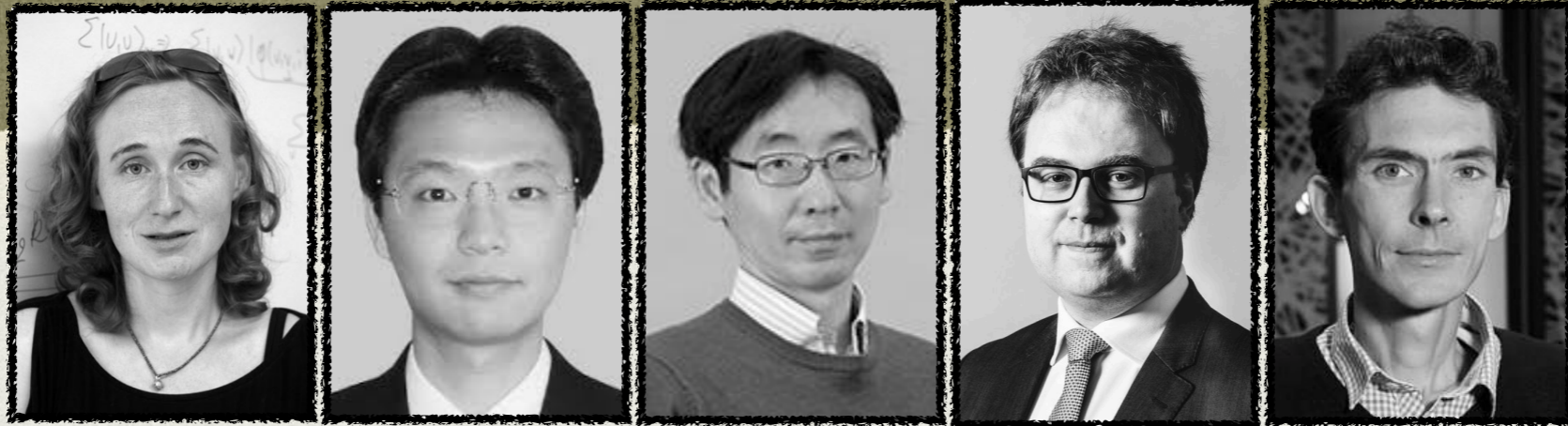

ANALYSE DE CAS

# SIMULATION ZK



ANALYSE DE CAS

# POWERFUL THEOREM



[Julia Kempe](#), [Hirotada Kobayashi](#), [Keiji Matsumoto](#), [Ben Toner](#), and [Thomas Vidick](#)

## Entangled Games Are Hard to Approximate

- Si PI est cohérente face aux prouveurs *locaux* alors PI augmenté grâce à 1 prouveur imitant les premiers est cohérente face aux prouveurs *intriqués*



$P_1$

$(n_1, n_2) \in E$



$P_2$

$(n_3, n_4) \in E$



$P_3$

$(n_5, n_6) \in E$

$n_1$   
 $n_2$   
 $r_1$   
 $r_2$

$meg_1$   
 $meg_2$

$n_3$   
 $n_4$   
 $r_3$   
 $r_4$

$meg_3$   
 $meg_4$

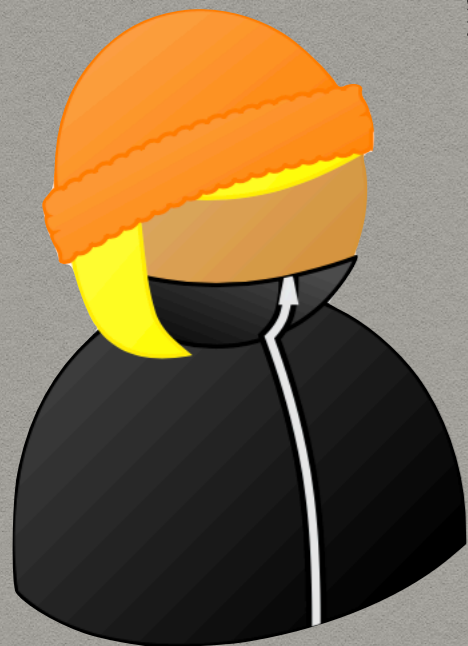
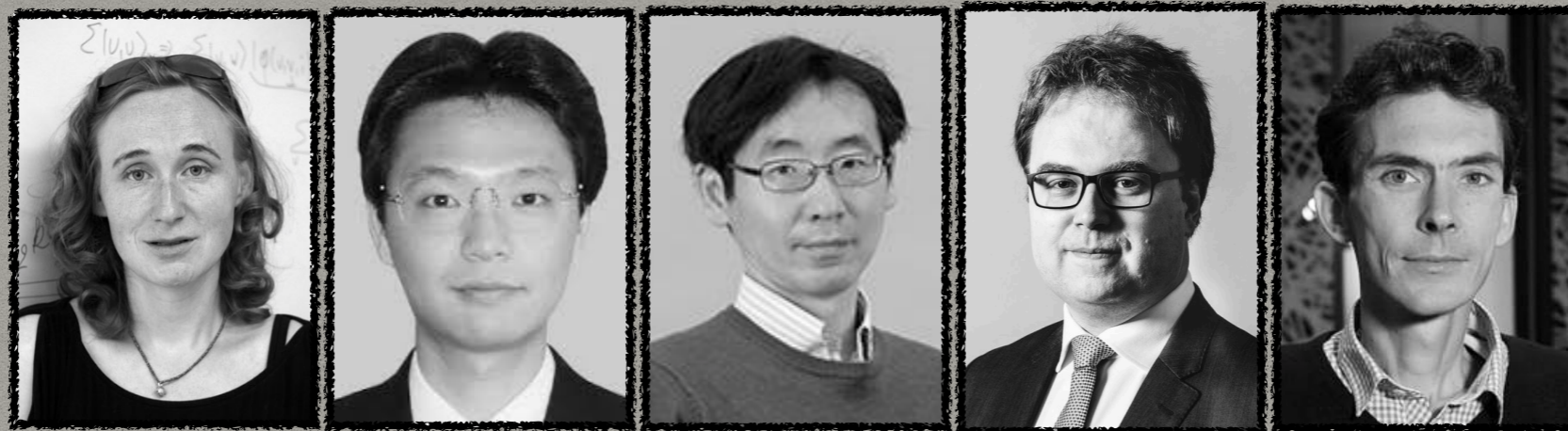
$n_5$   
 $n_6$   
 $r_5$   
 $r_6$

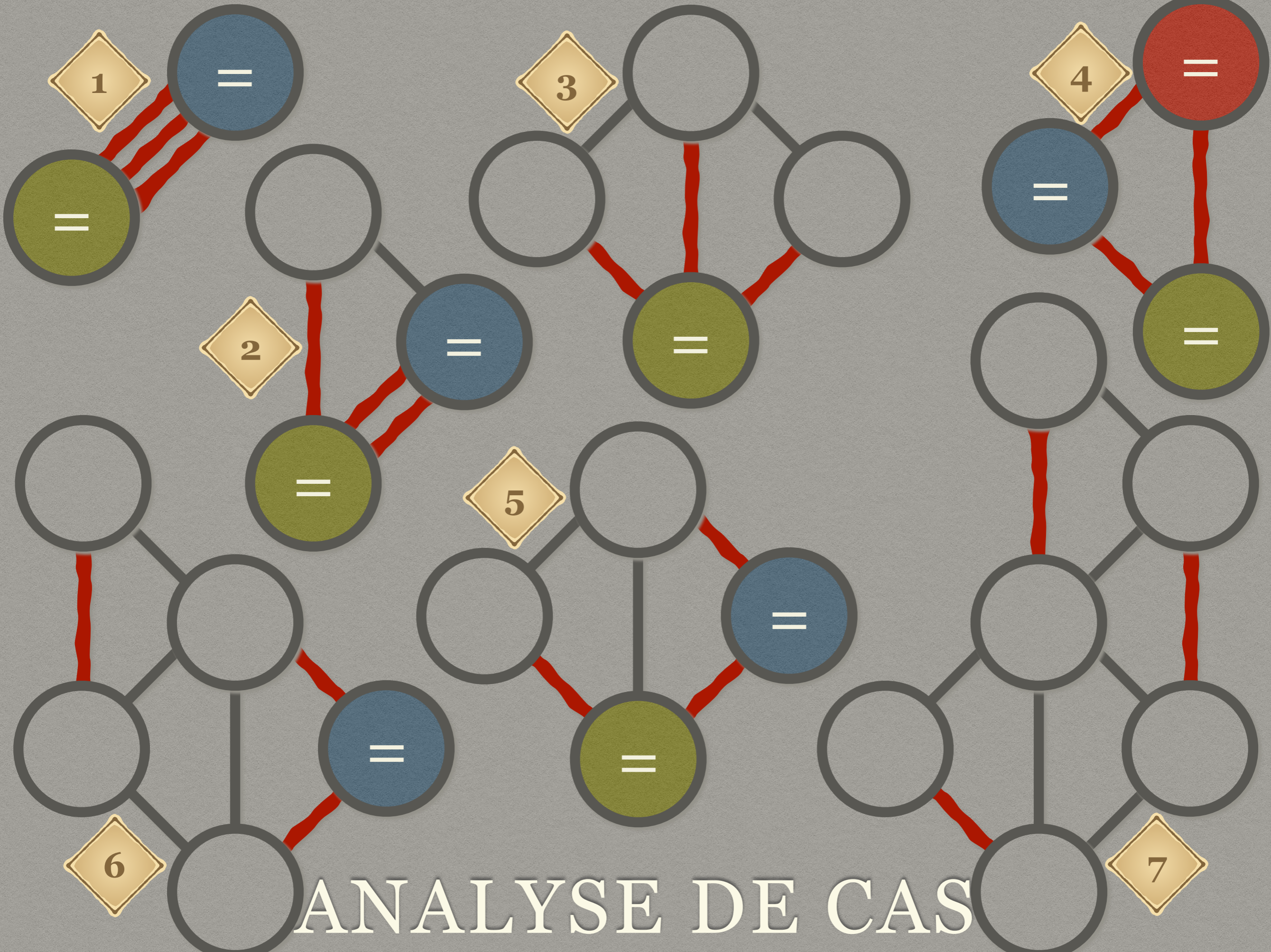
$meg_5$   
 $meg_6$

$$meg_i = b_{n_i} r_i + coul_{n_i}$$



# COHÉRENCE MALGRÉ L'INTRICATION





# ANALYSE DE CAS

# GROUPE TECHNOLOGIES QUANTIQUES UNIVERSITÉ DE GENÈVE



# QUESTIONS OUVERTES: THÉORÈME ANALOGUE?



# QUESTIONS OUVERTES: THÉORÈME ANALOGUE?



- Si PI est cohérente contre prouveurs *locaux/intriqués* alors PI augmenté grâce à  $N$  prouveurs imitant les premiers cohérente face aux prouveurs *Non-Signalants* ?

# QUESTIONS OUVERTES: THÉORÈME ANALOGUE?



- Si PI est cohérente contre prouveurs *locaux/intriqués* alors PI augmenté grâce à  $N$  prouveurs imitant les premiers cohérente face aux prouveurs *Non-Signalants* ?
- Zero-Knowledge ?

Arnaud Yoh Massenet-Oshima

Louis Salvail

Lucas Shigeru Stinchcombe

Nan Yang

PREUVE *ZERO-KNOWLEDGE* POUR NP  
RELATIVISTES ET RÉALISABLES  
(COHÉRENTE MALGRÉ L'INTRICATION)

Claude Crépeau



McGill